

Formally self-dual codes over \mathbb{Z}_4
by J. Yoo, Y. Lee, B. Kim

1. FORMALLY SELF-DUAL CODES OVER \mathbb{Z}_4 OF LENGTHS UP TO 10

We list up the generator matrices and Lee weight enumerators of free and non-free formally self-dual codes over \mathbb{Z}_4 of lengths 2,4,6,8, and 10, up to equivalence, obtained by using construction I,II, and III. The *-marked codes denote the ones with the largest minimum weight. Most of the examples listed below are formally self-dual codes but not self-dual codes.

TABLE 1. Free formally self-dual codes over \mathbb{Z}_4 of length 2

| Code | Generator matrix | Lee weight enumerator |
|-----------------------|--|------------------------|
| $\mathcal{C}_{2,1}$ | $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ | $X^4 + 2X^3Y + X^2Y^2$ |
| $\mathcal{C}_{2,2}^*$ | $\begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$ | $X^4 + 2X^2Y^2 + Y^4$ |
| $\mathcal{C}_{2,3}^*$ | $\begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$ | $X^4 + X^2Y^2 + 2XY^3$ |

TABLE 2. Non-free formally self-dual codes over \mathbb{Z}_4 of length 2

| No. | Generator matrix | Lee weight enumerator |
|-----------------------|--|-----------------------|
| $\mathcal{C}_{2,4}^*$ | $\begin{bmatrix} 2 & 0 \\ 0 & 2 \end{bmatrix}$ | $X^4 + 2X^2Y^2 + Y^4$ |

Note that $\mathcal{C}_{2,4}^*$ is self-dual code over \mathbb{Z}_4 of length 2.

TABLE 3. Free formally self-dual codes over \mathbb{Z}_4 of length 4

| Code | Generator matrix | Lee weight enumerator | construction |
|------------------------|--|--|--------------|
| $\mathcal{C}_{4,1}$ | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$ | $X^8 + 4X^7Y + 6X^6Y^2 + 4X^5Y^3 + X^4Y^4$ | II |
| $\mathcal{C}_{4,2}$ | $\begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$ | $X^8 + 2X^7Y + 3X^6Y^2 + 4X^5Y^3 + 3X^4Y^4 + 2X^3Y^5 + X^2Y^6$ | II |
| $\mathcal{C}_{4,3}$ | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 2 \end{bmatrix}$ | $X^8 + 2X^7Y + 2X^6Y^2 + 4X^5Y^3 + 5X^4Y^4 + 2X^3Y^5$ | II |
| $\mathcal{C}_{4,4}$ | $\begin{bmatrix} 1 & 0 & 2 & 2 \\ 0 & 1 & 2 & 2 \end{bmatrix}$ | $X^8 + 6X^6Y^2 + X^4Y^4 + 4X^3Y^5 + 4XY^7$ | I-(vi) |
| $\mathcal{C}_{4,5}$ | $\begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}$ | $X^8 + 4X^6Y^2 + 6X^4Y^4 + 4X^2Y^6 + Y^8$ | II |
| $\mathcal{C}_{4,6}$ | $\begin{bmatrix} 1 & 0 & 2 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}$ | $X^8 + 3X^6Y^2 + 2X^5Y^3 + 3X^4Y^4 + 4X^3Y^5 + X^2Y^6 + 2XY^7$ | II |
| $\mathcal{C}_{4,7}$ | $\begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 \end{bmatrix}$ | | III |
| $\mathcal{C}_{4,8}$ | $\begin{bmatrix} 1 & 0 & 2 & 0 \\ 0 & 1 & 0 & 2 \end{bmatrix}$ | $X^8 + 2X^6Y^2 + 4X^5Y^3 + X^4Y^4 + 4X^3Y^5 + 4X^2Y^6$ | II,I-(ii) |
| $\mathcal{C}_{4,9}$ | $\begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 1 \end{bmatrix}$ | | III |
| $\mathcal{C}_{4,10}$ | $\begin{bmatrix} 1 & 0 & 2 & 0 \\ 0 & 1 & 2 & 2 \end{bmatrix}$ | $X^8 + 2X^6Y^2 + 2X^5Y^3 + 5X^4Y^4 + 4X^3Y^5 + 2XY^7$ | I-(iii) |
| $\mathcal{C}_{4,11}$ | $\begin{bmatrix} 1 & 0 & 1 & 2 \\ 0 & 1 & 0 & 1 \end{bmatrix}$ | $X^8 + 2X^6Y^2 + 10X^4Y^4 + 2X^2Y^6 + Y^8$ | III |
| $\mathcal{C}_{4,12}$ | $\begin{bmatrix} 1 & 0 & 1 & 2 \\ 0 & 1 & 2 & 0 \end{bmatrix}$ | $X^8 + X^6Y^2 + 4X^5Y^3 + 3X^4Y^4 + 4X^3Y^5 + 3X^2Y^6$ | I-(i) |
| $\mathcal{C}_{4,13}$ | $\begin{bmatrix} 1 & 0 & 1 & 2 \\ 0 & 1 & 2 & 2 \end{bmatrix}$ | | |
| $\mathcal{C}_{4,14}$ | $\begin{bmatrix} 1 & 0 & 1 & 2 \\ 0 & 1 & 1 & 1 \end{bmatrix}$ | $X^8 + 4X^5Y^3 + 5X^4Y^4 + 4X^3Y^5 + 2X^2Y^6$ | III |
| $\mathcal{C}_{4,15}$ | $\begin{bmatrix} 1 & 0 & 1 & 3 \\ 0 & 1 & 1 & 1 \end{bmatrix}$ | | |
| $\mathcal{C}_{4,16}^*$ | $\begin{bmatrix} 1 & 0 & 2 & 1 \\ 0 & 1 & 1 & 2 \end{bmatrix}$ | $X^8 + 14X^4Y^4 + Y^8$ | III |

TABLE 4. Non-free formally self-dual codes over \mathbb{Z}_4 of length 4

| No. | Generator matrix | Lee weight enumerator | construction |
|------------|---|--|--------------|
| $C_{4,16}$ | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 2 & 0 \end{bmatrix}$ | $X^8 + 2X^7Y + 3X^6Y^2 + 4X^5Y^3 + 3X^4Y^4 + 2X^3Y^5 + X^2Y^6$ | II |
| $C_{4,17}$ | $\begin{bmatrix} 1 & 0 & 0 & 1 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 2 & 0 \end{bmatrix}$ | $X^8 + 4X^6Y^2 + 6X^4Y^4 + 4X^2Y^6 + Y^8$ | II |
| $C_{4,18}$ | $\begin{bmatrix} 1 & 0 & 0 & 2 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 2 & 0 \end{bmatrix}$ | $X^8 + 3X^6Y^2 + 2X^5Y^3 + 3X^4Y^4 + 4X^3Y^5 + X^2Y^6 + 2XY^7$ | II |

 TABLE 5. Free formally self-dual codes over \mathbb{Z}_4 of length 6

| No. | Generator Matrix | Lee weight enumerator | Construction |
|-----|--|---|----------------|
| 1 | $I_3 \mid \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ | $X^{12} + 6X^{11}Y + 15X^{10}Y^2 + 20X^9Y^3 + 15X^8Y^4 + 6X^7Y^5 + X^6Y^6$ | II |
| 2 | $I_3 \mid \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ | $X^{12} + 4X^{11}Y + 8X^{10}Y^2 + 12X^9Y^3 + 14X^8Y^4 + 12X^7Y^5 + 8X^6Y^6 + 4X^5Y^7 + X^4Y^8$ | II |
| 3 | $I_3 \mid \begin{bmatrix} 2 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ | $X^{12} + 4X^{11}Y + 7X^{10}Y^2 + 10X^9Y^3 + 15X^8Y^4 + 16X^7Y^5 + 9X^6Y^6 + 2X^5Y^7$ | II |
| 4 | $I_3 \mid \begin{bmatrix} 0 & 0 & 0 \\ 0 & 2 & 2 \\ 0 & 2 & 2 \end{bmatrix}$ | $X^{12} + 2X^{11}Y + 7X^{10}Y^2 + 12X^9Y^3 + 7X^8Y^4 + 6X^7Y^5 + 9X^6Y^6 + 8X^5Y^7 + 8X^4Y^8 + 4X^3Y^9$ | II |
| 5 | $I_3 \mid \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ | $X^{12} + 2X^{11}Y + 5X^{10}Y^2 + 8X^9Y^3 + 10X^8Y^4 + 12X^7Y^5 + 10X^6Y^6 + 8X^5Y^7 + 5X^4Y^8 + 2X^3Y^9 + X^2Y^{10}$ | II |
| 6 | $I_3 \mid \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 2 \end{bmatrix}$ | $X^{12} + 2X^{11}Y + 4X^{10}Y^2 + 8X^9Y^3 + 10X^8Y^4 + 12X^7Y^5 + 12X^6Y^6 + 8X^5Y^7 + 5X^4Y^8 + 2X^3Y^9$ | II |
| 7 | $I_3 \mid \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{bmatrix}$ | $X^{12} + 2X^{11}Y + 3X^{10}Y^2 + 8X^9Y^3 + 11X^8Y^4 + 10X^7Y^5 + 13X^6Y^6 + 12X^5Y^7 + 4X^4Y^8$ | II |
| 8 | $I_3 \mid \begin{bmatrix} 0 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 2 \end{bmatrix}$ | | |
| 9 | $I_3 \mid \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 1 \end{bmatrix}$ | $X^{12} + 2X^{11}Y + 3X^{10}Y^2 + 4X^9Y^3 + 12X^8Y^4 + 20X^7Y^5 + 12X^6Y^6 + 4X^5Y^7 + 3X^4Y^8 + 2X^3Y^9 + X^2Y^{10}$ | II |
| 10 | $I_3 \mid \begin{bmatrix} 0 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 2 & 2 \end{bmatrix}$ | | |
| 11 | $I_3 \mid \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$ | $X^{12} + 2X^{11}Y + 3X^{10}Y^2 + 4X^9Y^3 + 12X^8Y^4 + 20X^7Y^5 + 12X^6Y^6 + 4X^5Y^7 + 3X^4Y^8 + 2X^3Y^9 + X^2Y^{10}$ | II |
| 12 | $I_3 \mid \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 2 & 0 \end{bmatrix}$ | | |
| 13 | $I_3 \mid \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 2 & 2 \end{bmatrix}$ | $X^{12} + 2X^{11}Y + 2X^{10}Y^2 + 6X^9Y^3 + 12X^8Y^4 + 14X^7Y^5 + 14X^6Y^6 + 10X^5Y^7 + 3X^4Y^8$ | II |
| 14 | $I_3 \mid \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 1 & 1 \end{bmatrix}$ | | |
| 15 | $I_3 \mid \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 3 \\ 0 & 1 & 1 \end{bmatrix}$ | $X^{12} + 2X^{11}Y + X^{10}Y^2 + 4X^9Y^3 + 13X^8Y^4 + 18X^7Y^5 + 15X^6Y^6 + 8X^5Y^7 + 2X^4Y^8$ | II |
| 16 | $I_3 \mid \begin{bmatrix} 0 & 0 & 0 \\ 0 & 2 & 1 \\ 0 & 1 & 2 \end{bmatrix}$ | | |
| 17 | $I_3 \mid \begin{bmatrix} 2 & 2 & 2 \\ 2 & 2 & 2 \\ 2 & 2 & 2 \end{bmatrix}$ | $X^{12} + 15X^{10}Y^2 + 15X^8Y^4 + X^6Y^6 + 6X^5Y^7 + 20X^3Y^9 + 6XY^{11}$ | I-(v) |
| 18 | $I_3 \mid \begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 2 \\ 0 & 2 & 2 \end{bmatrix}$ | $X^{12} + 8X^{10}Y^2 + 14X^8Y^4 + 4X^7Y^5 + 8X^6Y^6 + 12X^5Y^7 + X^4Y^8 + 12X^3Y^9 + 4XY^{11}$ | II, I-(iv),(v) |
| 19 | $I_3 \mid \begin{bmatrix} 2 & 0 & 0 \\ 2 & 2 & 2 \\ 2 & 0 & 0 \end{bmatrix}$ | $X^{12} + 7X^{10}Y^2 + 4X^9Y^3 + 7X^8Y^4 + 10X^7Y^5 + X^6Y^6 + 16X^5Y^7 + 8X^4Y^8 + 2X^3Y^9 + 8X^2Y^{10}$ | I-(ii) |
| 20 | $I_3 \mid \begin{bmatrix} 2 & 2 & 2 \\ 2 & 0 & 0 \\ 2 & 0 & 0 \end{bmatrix}$ | $X^{12} + 7X^{10}Y^2 + 4X^9Y^3 + 7X^8Y^4 + 8X^7Y^5 + 9X^6Y^6 + 6X^5Y^7 + 8X^4Y^8 + 12X^3Y^9 + 2XY^{11}$ | I-(iv) |

Table 5. Free formally self-dual codes over \mathbb{Z}_4 of length 6 (cont'd.)

| No. | Generator Matrix | Lee weight enumerator | Construction | Even |
|-----|---|---|---------------------------|--------------|
| 21 | $I_3 \left \begin{array}{ccc} 2 & 0 & 0 \\ 0 & 2 & 2 \\ 0 & 2 & 2 \end{array} \right.$ | $X^{12} + 7X^{10}Y^2 + 2X^9Y^3 + 7X^8Y^4 + 16X^7Y^5 + X^6Y^6 + 10X^5Y^7 + 8X^4Y^8 + 4X^3Y^9 + 8X^2Y^{10}$ | II | |
| 22 | $I_3 \left \begin{array}{ccc} 2 & 2 & 0 \\ 2 & 2 & 2 \\ 2 & 2 & 2 \end{array} \right.$ | $X^{12} + 7X^{10}Y^2 + 15X^8Y^4 + 2X^7Y^5 + 9X^6Y^6 + 16X^5Y^7 + 10X^3Y^9 + 4XY^{11}$ | I-(v) | |
| 23 | $I_3 \left \begin{array}{ccc} 1 & 2 & 2 \\ 2 & 0 & 0 \\ 2 & 0 & 0 \end{array} \right.$ | $X^{12} + 6X^{10}Y^2 + 8X^9Y^3 + 2X^8Y^4 + 8X^7Y^5 + 8X^6Y^6 + 8X^5Y^7 + 13X^4Y^8 + 8X^3Y^9 + 2X^2Y^{10}$ | I-(i) | |
| 24 | $I_3 \left \begin{array}{ccc} 1 & 2 & 2 \\ 2 & 2 & 2 \\ 2 & 2 & 2 \end{array} \right.$ | | | |
| 25 | $I_3 \left \begin{array}{ccc} 0 & 0 & 1 \\ 0 & 0 & 1 \\ 1 & 1 & 0 \end{array} \right.$ | $X^{12} + 6X^{10}Y^2 + 2X^9Y^3 + 9X^8Y^4 + 12X^7Y^5 + X^6Y^6 + 18X^5Y^7 + 6X^4Y^8 + 9X^2Y^{10}$ | III | |
| 26 | $I_3 \left \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{array} \right.$ | $X^{12} + 6X^{10}Y^2 + 15X^8Y^4 + 20X^6Y^6 + 15X^4Y^8 + 6X^2Y^{10} + Y^{12}$ | II | \bigcirc |
| 27 | $I_3 \left \begin{array}{ccc} 0 & 0 & 1 \\ 0 & 0 & 1 \\ 1 & 1 & 1 \end{array} \right.$ | | | |
| 28 | $I_3 \left \begin{array}{ccc} 0 & 0 & 1 \\ 0 & 0 & 1 \\ 1 & 1 & 2 \end{array} \right.$ | $X^{12} + 6X^{10}Y^2 + 9X^8Y^4 + 18X^7Y^5 + X^6Y^6 + 12X^5Y^7 + 6X^4Y^8 + 2X^3Y^9 + 9X^2Y^{10}$ | I | |
| 29 | $I_3 \left \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 1 \end{array} \right.$ | $X^{12} + 5X^{10}Y^2 + 2X^9Y^3 + 10X^8Y^4 + 8X^7Y^5 + 10X^6Y^6 + 12X^5Y^7 + 5X^4Y^8 + 8X^3Y^9 + X^2Y^{10} + 2XY^{11}$ | II | |
| 30 | $I_3 \left \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{array} \right.$ | $X^{12} + 4X^{10}Y^2 + 4X^9Y^3 + 6X^8Y^4 + 12X^7Y^5 + 8X^6Y^6 + 12X^5Y^7 + 9X^4Y^8 + 4X^3Y^9 + 4X^2Y^{10}$ | II | |
| 31 | $I_3 \left \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 2 \end{array} \right.$ | | | I-(ii),(iii) |
| 32 | $I_3 \left \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 1 \end{array} \right.$ | | | II |
| 33 | $I_3 \left \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 2 & 2 \end{array} \right.$ | $X^{12} + 4X^{10}Y^2 + 2X^9Y^3 + 10X^8Y^4 + 8X^7Y^5 + 12X^6Y^6 + 12X^5Y^7 + 5X^4Y^8 + 8X^3Y^9 + 2XY^{11}$ | II, I-(ii),(iii),(iv),(v) | |
| 34 | $I_3 \left \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{array} \right.$ | $X^{12} + 4X^{10}Y^2 + 15X^8Y^4 + 24X^6Y^6 + 15X^4Y^8 + 4X^2Y^{10} + Y^{12}$ | II | \bigcirc |
| 35 | $I_3 \left \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 2 \\ 2 & 0 & 0 \end{array} \right.$ | $X^{12} + 3X^{10}Y^2 + 8X^9Y^3 + 6X^8Y^4 + 10X^6Y^6 + 24X^5Y^7 + 9X^4Y^8 + 3X^2Y^{10}$ | III | |
| 36 | $I_3 \left \begin{array}{ccc} 0 & 0 & 1 \\ 0 & 0 & 2 \\ 2 & 1 & 2 \end{array} \right.$ | $X^{12} + 3X^{10}Y^2 + 8X^9Y^3 + 4X^8Y^4 + 4X^7Y^5 + 12X^6Y^6 + 16X^5Y^7 + 11X^4Y^8 + 4X^3Y^9 + X^2Y^{10}$ | III | |
| 37 | $I_3 \left \begin{array}{ccc} 2 & 0 & 2 \\ 0 & 2 & 2 \\ 2 & 2 & 0 \end{array} \right.$ | $X^{12} + 3X^{10}Y^2 + 8X^9Y^3 + 3X^8Y^4 + 6X^7Y^5 + 13X^6Y^6 + 12X^5Y^7 + 12X^4Y^8 + 6X^3Y^9$ | I-(iii) | |
| 38 | $I_3 \left \begin{array}{ccc} 2 & 1 & 1 \\ 0 & 2 & 2 \\ 2 & 1 & 1 \end{array} \right.$ | | | I-(ii) |
| 39 | $I_3 \left \begin{array}{ccc} 0 & 0 & 2 \\ 2 & 1 & 1 \\ 0 & 0 & 1 \end{array} \right.$ | | | I-(ii),(iii) |
| 40 | $I_3 \left \begin{array}{ccc} 2 & 0 & 2 \\ 0 & 2 & 2 \\ 2 & 2 & 0 \end{array} \right.$ | | | III |
| 41 | $I_3 \left \begin{array}{ccc} 2 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 0 & 1 \end{array} \right.$ | $X^{12} + 3X^{10}Y^2 + 6X^9Y^3 + 3X^8Y^4 + 12X^7Y^5 + 13X^6Y^6 + 6X^5Y^7 + 12X^4Y^8 + 8X^3Y^9$ | II | |
| 42 | $I_3 \left \begin{array}{ccc} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 2 \end{array} \right.$ | | | |
| 43 | $I_3 \left \begin{array}{ccc} 2 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 1 \end{array} \right.$ | | | |

Table 5. Free formally self-dual codes over \mathbb{Z}_4 of length 6 (cont'd.)

| No. | Generator Matrix | Lee weight enumerator | Construction | Even |
|-----|---|---|--------------|------|
| 44 | $I_3 \left \begin{array}{ccc} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 2 & 2 \end{array} \right.$ | $X^{12} + 3X^{10}Y^2 + 4X^9Y^3 + 7X^8Y^4 + 10X^7Y^5 + 9X^6Y^6 + 16X^5Y^7 + 8X^4Y^8 + 2X^3Y^9 + 4X^2Y^{10}$ | II | |
| 45 | $I_3 \left \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 2 & 0 \end{array} \right.$ | $X^{12} + 3X^{10}Y^2 + 4X^9Y^3 + 6X^8Y^4 + 12X^7Y^5 + 10X^6Y^6 + 12X^5Y^7 + 9X^4Y^8 + 4X^3Y^9 + 3X^2Y^{10}$ | II, I-(i) | |
| 46 | $I_3 \left \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 2 & 2 \end{array} \right.$ | | | |
| 47 | $I_3 \left \begin{array}{ccc} 0 & 0 & 1 \\ 0 & 2 & 2 \\ 1 & 2 & 2 \end{array} \right.$ | $X^{12} + 3X^{10}Y^2 + 4X^9Y^3 + 4X^8Y^4 + 16X^7Y^5 + 12X^6Y^6 + 4X^5Y^7 + 11X^4Y^8 + 8X^3Y^9 + X^2Y^{10}$ | III | |
| 48 | $I_3 \left \begin{array}{ccc} 2 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{array} \right.$ | $X^{12} + 3X^{10}Y^2 + 2X^9Y^3 + 12X^8Y^4 + 4X^7Y^5 + 12X^6Y^6 + 20X^5Y^7 + 3X^4Y^8 + 4X^3Y^9 + X^2Y^{10} + 2XY^{11}$ | II | |
| 49 | $I_3 \left \begin{array}{ccc} 2 & 2 & 2 \\ 2 & 0 & 2 \\ 2 & 0 & 0 \end{array} \right.$ | $X^{12} + 3X^{10}Y^2 + 2X^9Y^3 + 11X^8Y^4 + 6X^7Y^5 + 13X^6Y^6 + 16X^5Y^7 + 4X^4Y^8 + 6X^3Y^9 + 2XY^{11}$ | I-(iv) | |
| 50 | $I_3 \left \begin{array}{ccc} 0 & 0 & 2 \\ 0 & 2 & 2 \\ 2 & 2 & 0 \end{array} \right.$ | | IV) | |
| 51 | $I_3 \left \begin{array}{ccc} 2 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 2 & 0 \end{array} \right.$ | | II | |
| 52 | $I_3 \left \begin{array}{ccc} 2 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 2 & 2 \end{array} \right.$ | $X^{12} + 3X^{10}Y^2 + 2X^9Y^3 + 7X^8Y^4 + 16X^7Y^5 + 9X^6Y^6 + 10X^5Y^7 + 8X^4Y^8 + 4X^3Y^9 + 4X^2Y^{10}$ | | |
| 53 | $I_3 \left \begin{array}{ccc} 2 & 0 & 2 \\ 0 & 2 & 2 \\ 2 & 0 & 0 \end{array} \right.$ | | I-(ii) | |
| 54 | $I_3 \left \begin{array}{ccc} 2 & 2 & 0 \\ 0 & 2 & 2 \\ 2 & 2 & 2 \end{array} \right.$ | | I-(iii) | |
| 55 | $I_3 \left \begin{array}{ccc} 2 & 2 & 2 \\ 2 & 1 & 1 \\ 2 & 1 & 1 \end{array} \right.$ | $X^{12} + 3X^{10}Y^2 + 11X^8Y^4 + 12X^7Y^5 + 13X^6Y^6 + 10X^5Y^7 + 4X^4Y^8 + 8X^3Y^9 + 2XY^{11}$ | I-(iv) | |
| 56 | $I_3 \left \begin{array}{ccc} 2 & 0 & 2 \\ 2 & 1 & 1 \\ 0 & 0 & 1 \end{array} \right.$ | | I-(iv),(v) | |
| 57 | $I_3 \left \begin{array}{ccc} 2 & 2 & 2 \\ 2 & 0 & 2 \\ 0 & 1 & 2 \end{array} \right.$ | | | |
| 58 | $I_3 \left \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 2 \\ 2 & 0 & 2 \end{array} \right.$ | $X^{12} + 3X^{10}Y^2 + 6X^8Y^4 + 24X^7Y^5 + 10X^6Y^6 + 9X^4Y^8 + 8X^3Y^9 + 3X^2Y^{10}$ | III | |
| 59 | $I_3 \left \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \end{array} \right.$ | | | |
| 60 | $I_3 \left \begin{array}{ccc} 1 & 1 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 1 \end{array} \right.$ | | III | |
| 61 | $I_3 \left \begin{array}{ccc} 1 & 1 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \end{array} \right.$ | $X^{12} + 2X^{10}Y^2 + 6X^9Y^3 + 5X^8Y^4 + 8X^7Y^5 + 13X^6Y^6 + 14X^5Y^7 + 10X^4Y^8 + 4X^3Y^9 + X^2Y^{10}$ | | |
| 62 | $I_3 \left \begin{array}{ccc} 0 & 0 & 2 \\ 2 & 2 & 0 \\ 0 & 1 & 2 \end{array} \right.$ | | | |
| 63 | $I_3 \left \begin{array}{ccc} 0 & 0 & 2 \\ 2 & 2 & 2 \\ 0 & 1 & 2 \end{array} \right.$ | | I-(iv),(v) | |
| 64 | $I_3 \left \begin{array}{ccc} 2 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 2 & 0 \end{array} \right.$ | | | |
| 65 | $I_3 \left \begin{array}{ccc} 2 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 2 & 2 \end{array} \right.$ | $X^{12} + 2X^{10}Y^2 + 6X^9Y^3 + 4X^8Y^4 + 10X^7Y^5 + 14X^6Y^6 + 10X^5Y^7 + 11X^4Y^8 + 6X^3Y^9$ | III | |
| 66 | $I_3 \left \begin{array}{ccc} 1 & 2 & 0 \\ 2 & 0 & 2 \\ 0 & 2 & 0 \end{array} \right.$ | | | |
| 67 | $I_3 \left \begin{array}{ccc} 1 & 2 & 0 \\ 2 & 2 & 2 \\ 0 & 2 & 0 \end{array} \right.$ | | | |

Table 5. Free formally self-dual codes over \mathbb{Z}_4 of length 6 (cont'd.)

| No. | Generator Matrix | Lee weight enumerator | Construction | Even |
|-----|--|---|--------------|------|
| 68 | $[I_3 \mid \begin{matrix} 1 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 1 & 1 \end{matrix}]$ | | II | |
| 69 | $[I_3 \mid \begin{matrix} 1 & 0 & 0 \\ 0 & 1 & 3 \\ 0 & 1 & 1 \end{matrix}]$ | | | |
| 70 | $[I_3 \mid \begin{matrix} 1 & 2 & 2 \\ 2 & 0 & 2 \\ 2 & 0 & 0 \end{matrix}]$ | $X^{12} + 2X^{10}Y^2 + 4X^9Y^3 + 6X^8Y^4 + 12X^7Y^5 + 12X^6Y^6 + 12X^5Y^7 + 9X^4Y^8 + 4X^3Y^9 + 2X^2Y^{10}$ | | |
| 71 | $[I_3 \mid \begin{matrix} 3 & 2 & 2 \\ 2 & 3 & 0 \\ 2 & 2 & 2 \end{matrix}]$ | | I-(i) | |
| 72 | $[I_3 \mid \begin{matrix} 1 & 2 & 2 \\ 2 & 2 & 2 \\ 2 & 2 & 0 \end{matrix}]$ | | | |
| 73 | $[I_3 \mid \begin{matrix} 1 & 2 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{matrix}]$ | | | |
| 74 | $[I_3 \mid \begin{matrix} 1 & 2 & 3 \\ 1 & 1 & 3 \\ 3 & 3 & 1 \end{matrix}]$ | $X^{12} + 2X^{10}Y^2 + 4X^9Y^3 + 5X^8Y^4 + 14X^7Y^5 + 13X^6Y^6 + 8X^5Y^7 + 10X^4Y^8 + 6X^3Y^9 + X^2Y^{10}$ | III | |
| 75 | $[I_3 \mid \begin{matrix} 1 & 3 & 0 \\ 1 & 1 & 1 \\ 0 & 1 & 0 \end{matrix}]$ | | | |
| 76 | $[I_3 \mid \begin{matrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 2 \end{matrix}]$ | $X^{12} + 2X^{10}Y^2 + 2X^9Y^3 + 9X^8Y^4 + 12X^7Y^5 + 9X^6Y^6 + 18X^5Y^7 + 6X^4Y^8 + 5X^2Y^{10}$ | III | |
| 77 | $[I_3 \mid \begin{matrix} 1 & 0 & 0 \\ 0 & 2 & 1 \\ 0 & 1 & 2 \end{matrix}]$ | | II | |
| 78 | $[I_3 \mid \begin{matrix} 1 & 0 & 0 \\ 0 & 1 & 2 \\ 2 & 0 & 1 \end{matrix}]$ | $X^{12} + 2X^{10}Y^2 + 15X^8Y^4 + 28X^6Y^6 + 15X^4Y^8 + 2X^2Y^{10} + Y^{12}$ | | ○ |
| 79 | $[I_3 \mid \begin{matrix} 0 & 0 & 1 \\ 0 & 2 & 1 \\ 1 & 1 & 1 \end{matrix}]$ | | III | |
| 80 | $[I_3 \mid \begin{matrix} 2 & 0 & 2 \\ 2 & 2 & 0 \\ 0 & 1 & 2 \end{matrix}]$ | $X^{12} + 2X^{10}Y^2 + 12X^8Y^4 + 10X^7Y^5 + 14X^6Y^6 + 14X^5Y^7 + 3X^4Y^8 + 6X^3Y^9 + 2XY^{11}$ | I-(iv),(v) | |
| 81 | $[I_3 \mid \begin{matrix} 2 & 0 & 2 \\ 0 & 1 & 2 \\ 2 & 2 & 2 \end{matrix}]$ | | III | |
| 82 | $[I_3 \mid \begin{matrix} 1 & 2 & 2 \\ 2 & 0 & 2 \\ 2 & 2 & 0 \end{matrix}]$ | | I-(i) | |
| 83 | $[I_3 \mid \begin{matrix} 1 & 2 & 2 \\ 2 & 1 & 1 \\ 2 & 1 & 1 \end{matrix}]$ | $X^{12} + 2X^{10}Y^2 + 10X^8Y^4 + 16X^7Y^5 + 8X^6Y^6 + 16X^5Y^7 + 5X^4Y^8 + 6X^2Y^{10}$ | | |
| 84 | $[I_3 \mid \begin{matrix} 1 & 0 & 2 \\ 2 & 1 & 1 \\ 0 & 0 & 1 \end{matrix}]$ | | I-(i) | |
| 85 | $[I_3 \mid \begin{matrix} 0 & 0 & 1 \\ 0 & 2 & 1 \\ 1 & 1 & 2 \end{matrix}]$ | $X^{12} + 2X^{10}Y^2 + 9X^8Y^4 + 18X^7Y^5 + 9X^6Y^6 + 12X^5Y^7 + 6X^4Y^8 + 2X^3Y^9 + 5X^2Y^{10}$ | III | |
| 86 | $[I_3 \mid \begin{matrix} 2 & 2 & 1 \\ 2 & 2 & 1 \\ 1 & 1 & 2 \end{matrix}]$ | | | |
| 87 | $[I_3 \mid \begin{matrix} 2 & 1 & 2 \\ 1 & 2 & 2 \\ 2 & 2 & 2 \end{matrix}]$ | $X^{12} + X^{10}Y^2 + 8X^9Y^3 + 6X^8Y^4 + 14X^6Y^6 + 24X^5Y^7 + 9X^4Y^8 + X^2Y^{10}$ | III | |
| 88 | $[I_3 \mid \begin{matrix} 2 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 1 & 1 \end{matrix}]$ | | II | |
| 89 | $[I_3 \mid \begin{matrix} 2 & 0 & 0 \\ 0 & 1 & 3 \\ 0 & 1 & 1 \end{matrix}]$ | $X^{12} + X^{10}Y^2 + 6X^9Y^3 + 5X^8Y^4 + 8X^7Y^5 + 15X^6Y^6 + 14X^5Y^7 + 10X^4Y^8 + 4X^3Y^9$ | | |
| 90 | $[I_3 \mid \begin{matrix} 2 & 0 & 2 \\ 0 & 1 & 1 \\ 2 & 1 & 2 \end{matrix}]$ | | III | |
| 91 | $[I_3 \mid \begin{matrix} 2 & 0 & 2 \\ 0 & 1 & 1 \\ 2 & 1 & 3 \end{matrix}]$ | | | |

Table 5. Free formally self-dual codes over \mathbb{Z}_4 of length 6 (cont'd.)

| No. | Generator Matrix | Lee weight enumerator | Construction | Even |
|-----|---|--|--------------|------|
| 92 | $I_3 \left \begin{array}{ccc} 2 & 0 & 0 \\ 0 & 1 & 2 \\ 1 & 2 & 0 \end{array} \right.$ | $X^{12} + X^{10}Y^2 + 4X^9Y^3 + 8X^8Y^4 + 8X^7Y^5 + 12X^6Y^6 + 20X^5Y^7 + 7X^4Y^8 + 3X^2Y^{10}$ | III | |
| 93 | $I_3 \left \begin{array}{ccc} 2 & 0 & 0 \\ 0 & 1 & 2 \\ 1 & 1 & 0 \end{array} \right.$ | $X^{12} + X^{10}Y^2 + 4X^9Y^3 + 7X^8Y^4 + 10X^7Y^5 + 13X^6Y^6 + 16X^5Y^7 + 8X^4Y^8 + 2X^3Y^9 + 2X^2Y^{10}$ | III | |
| 94 | $I_3 \left \begin{array}{ccc} 0 & 0 & 2 \\ 0 & 2 & 1 \\ 2 & 1 & 0 \end{array} \right.$ | $X^{12} + X^{10}Y^2 + 4X^9Y^3 + 6X^8Y^4 + 12X^7Y^5 + 14X^6Y^6 + 12X^5Y^7 + 9X^4Y^8 + 4X^3Y^9 + X^2Y^{10}$ | III | |
| 95 | $I_3 \left \begin{array}{ccc} 2 & 2 & 0 \\ 2 & 2 & 1 \\ 0 & 1 & 2 \end{array} \right.$ | | | |
| 96 | $I_3 \left \begin{array}{ccc} 2 & 1 & 1 \\ 0 & 2 & 2 \\ 2 & 1 & 3 \end{array} \right.$ | | I-(ii) | |
| 97 | $I_3 \left \begin{array}{ccc} 0 & 2 & 0 \\ 2 & 1 & 1 \\ 0 & 1 & 2 \end{array} \right.$ | $X^{12} + X^{10}Y^2 + 4X^9Y^3 + 5X^8Y^4 + 14X^7Y^5 + 15X^6Y^6 + 8X^5Y^7 + 10X^4Y^8 + 6X^3Y^9$ | I-(ii),(iii) | |
| 98 | $I_3 \left \begin{array}{ccc} 1 & 3 & 2 \\ 1 & 1 & 0 \\ 2 & 0 & 0 \end{array} \right.$ | | III | |
| 99 | $I_3 \left \begin{array}{ccc} 1 & 2 & 2 \\ 1 & 1 & 2 \\ 2 & 2 & 0 \end{array} \right.$ | | | |
| 100 | $I_3 \left \begin{array}{ccc} 2 & 0 & 0 \\ 0 & 2 & 1 \\ 0 & 1 & 2 \end{array} \right.$ | $X^{12} + X^{10}Y^2 + 2X^9Y^3 + 14X^8Y^4 + 14X^6Y^6 + 28X^5Y^7 + X^4Y^8 + X^2Y^{10} + 2XY^{11}$ | II | |
| 101 | $I_3 \left \begin{array}{ccc} 2 & 0 & 2 \\ 0 & 1 & 1 \\ 2 & 1 & 0 \end{array} \right.$ | $X^{12} + X^{10}Y^2 + 2X^9Y^3 + 7X^8Y^4 + 16X^7Y^5 + 13X^6Y^6 + 10X^5Y^7 + 8X^4Y^8 + 4X^3Y^9 + 2X^2Y^{10}$ | III | |
| 102 | $I_3 \left \begin{array}{ccc} 2 & 0 & 2 \\ 0 & 1 & 1 \\ 2 & 1 & 1 \end{array} \right.$ | | | |
| 103 | $I_3 \left \begin{array}{ccc} 2 & 2 & 2 \\ 2 & 1 & 1 \\ 2 & 1 & 3 \end{array} \right.$ | $X^{12} + X^{10}Y^2 + 13X^8Y^4 + 8X^7Y^5 + 15X^6Y^6 + 18X^5Y^7 + 2X^4Y^8 + 4X^3Y^9 + 2XY^{11}$ | I-(iv) | |
| 104 | $I_3 \left \begin{array}{ccc} 2 & 2 & 0 \\ 2 & 1 & 1 \\ 0 & 1 & 2 \end{array} \right.$ | | I-(iv),(v) | |
| 105 | $I_3 \left \begin{array}{ccc} 1 & 0 & 2 \\ 0 & 1 & 2 \\ 2 & 2 & 0 \end{array} \right.$ | $X^{12} + X^{10}Y^2 + 10X^8Y^4 + 16X^7Y^5 + 10X^6Y^6 + 16X^5Y^7 + 5X^4Y^8 + 5X^2Y^{10}$ | I | |
| 106 | $I_3 \left \begin{array}{ccc} 1 & 0 & 2 \\ 0 & 1 & 2 \\ 2 & 2 & 2 \end{array} \right.$ | | | |
| 107 | $I_3 \left \begin{array}{ccc} 1 & 2 & 0 \\ 2 & 0 & 2 \\ 0 & 1 & 2 \end{array} \right.$ | $X^{12} + X^{10}Y^2 + 8X^8Y^4 + 20X^7Y^5 + 12X^6Y^6 + 8X^5Y^7 + 7X^4Y^8 + 4X^3Y^9 + 3X^2Y^{10}$ | III | |
| 108 | $I_3 \left \begin{array}{ccc} 2 & 0 & 2 \\ 0 & 1 & 2 \\ 2 & 2 & 1 \end{array} \right.$ | $X^{12} + X^{10}Y^2 + 6X^8Y^4 + 24X^7Y^5 + 14X^6Y^6 + 9X^4Y^8 + 8X^3Y^9 + X^2Y^{10}$ | III | |
| 109 | $I_3 \left \begin{array}{ccc} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \end{array} \right.$ | $X^{12} + 8X^9Y^3 + 6X^8Y^4 + 16X^6Y^6 + 24X^5Y^7 + 9X^4Y^8$ | III | |
| 110 | $I_3 \left \begin{array}{ccc} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 0 \end{array} \right.$ | $X^{12} + 6X^9Y^3 + 6X^8Y^4 + 6X^7Y^5 + 16X^6Y^6 + 18X^5Y^7 + 9X^4Y^8 + 2X^3Y^9$ | III | |
| 111 | $I_3 \left \begin{array}{ccc} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 2 \end{array} \right.$ | | | |
| 112 | $I_3 \left \begin{array}{ccc} 2 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 0 \end{array} \right.$ | $X^{12} + 4X^9Y^3 + 7X^8Y^4 + 10X^7Y^5 + 15X^6Y^6 + 16X^5Y^7 + 8X^4Y^8 + 2X^3Y^9 + X^2Y^{10}$ | III | |
| 113 | $I_3 \left \begin{array}{ccc} 2 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 1 \end{array} \right.$ | | | |
| 114 | $I_3 \left \begin{array}{ccc} 1 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 3 \end{array} \right.$ | $X^{12} + 4X^9Y^3 + 6X^8Y^4 + 12X^7Y^5 + 16X^6Y^6 + 12X^5Y^7 + 9X^4Y^8 + 4X^3Y^9$ | III | |

Table 5. Free formally self-dual codes over \mathbb{Z}_4 of length 6 (cont'd.)

| No. | Generator Matrix | Lee weight enumerator | Construction | Even |
|------|---|--|--------------|------|
| 115 | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 0 & 1 \\ 0 & 1 & 2 \\ 2 & 1 & 0 \end{matrix} \end{bmatrix}$ | | | |
| 116 | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 0 & 1 \\ 0 & 1 & 2 \\ 2 & 1 & 1 \end{matrix} \end{bmatrix}$ | $X^{12} + 2X^9Y^3 + 9X^8Y^4 + 12X^7Y^5 + 13X^6Y^6 + 18X^5Y^7 + 6X^4Y^8 + 3X^2Y^{10}$ | III | |
| 117 | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 0 & 1 \\ 0 & 1 & 2 \\ 2 & 1 & 2 \end{matrix} \end{bmatrix}$ | | | |
| 118 | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 0 & 1 \\ 0 & 1 & 2 \\ 1 & 2 & 0 \end{matrix} \end{bmatrix}$ | | | |
| 119 | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 0 & 1 \\ 0 & 1 & 2 \\ 1 & 2 & 1 \end{matrix} \end{bmatrix}$ | $X^{12} + 2X^9Y^3 + 8X^8Y^4 + 14X^7Y^5 + 14X^6Y^6 + 14X^5Y^7 + 7X^4Y^8 + 2X^3Y^9 + 2X^2Y^{10}$ | III | |
| 120 | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 0 & 1 \\ 0 & 1 & 2 \\ 1 & 2 & 2 \end{matrix} \end{bmatrix}$ | | | |
| 121 | $\begin{bmatrix} I_3 & \begin{matrix} 2 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 2 \end{matrix} \end{bmatrix}$ | $X^{12} + 2X^9Y^3 + 7X^8Y^4 + 16X^7Y^5 + 15X^6Y^6 + 10X^5Y^7 + 8X^4Y^8 + 4X^3Y^9 + X^2Y^{10}$ | III | |
| 123 | $\begin{bmatrix} I_3 & \begin{matrix} 2 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 3 \end{matrix} \end{bmatrix}$ | | | |
| 124 | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 2 & 1 \\ 1 & 1 & 2 \\ 2 & 1 & 1 \end{matrix} \end{bmatrix}$ | $X^{12} + 2X^9Y^3 + 6X^8Y^4 + 18X^7Y^5 + 16X^6Y^6 + 6X^5Y^7 + 9X^4Y^8 + 6X^3Y^9$ | III | |
| 125 | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 2 & 1 \\ 1 & 1 & 3 \\ 2 & 0 & 1 \end{matrix} \end{bmatrix}$ | | | |
| 126* | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 2 & 0 \\ 1 & 1 & 1 \\ 1 & 0 & 2 \end{matrix} \end{bmatrix}$ | | | |
| 127* | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 2 & 2 \\ 1 & 1 & 1 \\ 1 & 2 & 0 \end{matrix} \end{bmatrix}$ | $X^{12} + 15X^8Y^4 + 32X^6Y^6 + 15X^4Y^8 + Y^{12}$ | III | ○ |
| 128* | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 3 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 3 \end{matrix} \end{bmatrix}$ | | | |
| 129* | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 2 & 2 \\ 2 & 1 & 3 \\ 2 & 1 & 3 \end{matrix} \end{bmatrix}$ | $X^{12} + 10X^8Y^4 + 16X^7Y^5 + 12X^6Y^6 + 16X^5Y^7 + 5X^4Y^8 + 4X^2Y^{10}$ | I-(i) | |
| 130* | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 2 & 0 \\ 2 & 1 & 1 \\ 0 & 1 & 2 \end{matrix} \end{bmatrix}$ | | I-(i) | |
| 131* | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 1 & 1 \\ 0 & 1 & 2 \\ 2 & 1 & 3 \end{matrix} \end{bmatrix}$ | | | |
| 132* | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 2 & 1 \\ 1 & 1 & 2 \\ 2 & 1 & 0 \end{matrix} \end{bmatrix}$ | $X^{12} + 9X^8Y^4 + 18X^7Y^5 + 13X^6Y^6 + 12X^5Y^7 + 6X^4Y^8 + 2X^3Y^9 + 3X^2Y^{10}$ | III | |
| 133* | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 2 & 1 \\ 1 & 1 & 3 \\ 3 & 1 & 1 \end{matrix} \end{bmatrix}$ | | | |
| 134* | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 2 & 1 \\ 1 & 1 & 2 \\ 1 & 2 & 3 \end{matrix} \end{bmatrix}$ | | | |
| 135* | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 2 & 1 \\ 1 & 1 & 2 \\ 2 & 1 & 3 \end{matrix} \end{bmatrix}$ | $X^{12} + 6X^8Y^4 + 24X^7Y^5 + 16X^6Y^6 + 9X^4Y^8 + 8X^3Y^9$ | III | |
| 136* | $\begin{bmatrix} I_3 & \begin{matrix} 1 & 2 & 1 \\ 1 & 1 & 3 \\ 3 & 1 & 2 \end{matrix} \end{bmatrix}$ | | | |

TABLE 6. Non-free formally self-dual codes over \mathbb{Z}_4 of length 6

| No. | Generator matrix | Lee weight enumerator | construction |
|-----|--|---|--------------|
| 1 | $\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 2 & 0 & 0 \end{bmatrix}$ | $X^{12} + 4X^{11}Y + 8X^{10}Y^2 + 12X^9Y^3 + 14X^8Y^4 + 12X^7Y^5 + 8X^6Y^6 + 4X^5Y^7 + X^4Y^8$ | II |
| 2 | $\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 1 \\ 0 & 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 2 & 0 & 0 \end{bmatrix}$ | $X^{12} + 2X^{11}Y + 5X^{10}Y^2 + 8X^9Y^3 + 10X^8Y^4 + 12X^7Y^5 + 10X^6Y^6 + 8X^5Y^7 + 5X^4Y^8 + 2X^3Y^9 + X^2Y^{10}$ | II |
| 3 | $\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 2 \\ 0 & 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 2 & 0 & 0 \end{bmatrix}$ | $X^{12} + 2X^{11}Y + 4X^{10}Y^2 + 8X^9Y^3 + 10X^8Y^4 + 12X^7Y^5 + 12X^6Y^6 + 8X^5Y^7 + 5X^4Y^8 + 2X^3Y^9$ | II |
| 4 | $\begin{bmatrix} 1 & 0 & 0 & 0 & 2 & 2 \\ 0 & 1 & 0 & 0 & 2 & 2 \\ 0 & 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 2 & 0 & 0 \end{bmatrix}$ | $X^{12} + 8X^{10}Y^2 + 14X^8Y^4 + 4X^7Y^5 + 8X^6Y^6 + 12X^5Y^7 + X^4Y^8 + 12X^3Y^9 + 4XY^{11}$ | I |
| 5 | $\begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 & 1 \\ 0 & 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 2 & 0 & 0 \end{bmatrix}$ | $X^{12} + 6X^{10}Y^2 + 15X^8Y^4 + 20X^6Y^6 + 15X^4Y^8 + 6X^2Y^{10} + Y^{12}$ | II |
| 6 | $\begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 & 0 & 2 \\ 0 & 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 2 & 0 & 0 \end{bmatrix}$ | $X^{12} + 5X^{10}Y^2 + 2X^9Y^3 + 10X^8Y^4 + 8X^7Y^5 + 10X^6Y^6 + 12X^5Y^7 + 5X^4Y^8 + 8X^3Y^9 + X^2Y^{10} + 2XY^{11}$ | II |
| 7 | $\begin{bmatrix} 1 & 0 & 0 & 0 & 2 & 0 \\ 0 & 1 & 0 & 0 & 0 & 2 \\ 0 & 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 2 & 0 & 0 \end{bmatrix}$ | $X^{12} + 4X^{10}Y^2 + 4X^9Y^3 + 6X^8Y^4 + 12X^7Y^5 + 8X^6Y^6 + 12X^5Y^7 + 9X^4Y^8 + 4X^3Y^9 + 4X^2Y^{10}$ | I |
| 8 | $\begin{bmatrix} 1 & 0 & 0 & 0 & 2 & 2 \\ 0 & 1 & 0 & 0 & 0 & 2 \\ 0 & 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 2 & 0 & 0 \end{bmatrix}$ | $X^{12} + 4X^{10}Y^2 + 2X^9Y^3 + 10X^8Y^4 + 8X^7Y^5 + 12X^6Y^6 + 12X^5Y^7 + 5X^4Y^8 + 8X^3Y^9 + 2XY^{11}$ | I |
| 9 | $\begin{bmatrix} 1 & 0 & 0 & 0 & 1 & 2 \\ 0 & 1 & 0 & 0 & 0 & 2 \\ 0 & 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 2 & 0 & 0 \end{bmatrix}$ | $X^{12} + 3X^{10}Y^2 + 4X^9Y^3 + 6X^8Y^4 + 12X^7Y^5 + 10X^6Y^6 + 12X^5Y^7 + 9X^4Y^8 + 4X^3Y^9 + 3X^2Y^{10}$ | I |
| 10 | $\begin{bmatrix} 1 & 0 & 0 & 0 & 3 & 2 \\ 0 & 1 & 0 & 0 & 2 & 0 \\ 0 & 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 2 & 0 & 0 \end{bmatrix}$ | | |

TABLE 7. Free formally self-dual codes over \mathbb{Z}_4 of length 8

| No. | Generator Matrix | Lee weight enumerator | Construction | Even | Non-SD |
|-----|---|---|--------------|------|--------|
| 1 | $I_4 \mid \begin{matrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{matrix}$ | $X^{16} + 8X^{15}Y + 28X^{14}Y^2 + 56X^{13}Y^3 + 70X^{12}Y^4 + 56X^{11}Y^5 + 28X^{10}Y^6 + 8X^9Y^7 + X^8Y^8$ | II | | ○ |
| 2 | $I_4 \mid \begin{matrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{matrix}$ | $X^{16} + 6X^{15}Y + 17X^{14}Y^2 + 32X^{13}Y^3 + 46X^{12}Y^4 + 52X^{11}Y^5 + 46X^{10}Y^6 + 32X^9Y^7 + 17X^8Y^8 + 6X^7Y^9 + X^6Y^{10}$ | II | | ○ |
| 3 | $I_4 \mid \begin{matrix} 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{matrix}$ | $X^{16} + 6X^{15}Y + 16X^{14}Y^2 + 28X^{13}Y^3 + 42X^{12}Y^4 + 56X^{11}Y^5 + 56X^{10}Y^6 + 36X^9Y^7 + 13X^8Y^8 + 2X^7Y^9$ | II | | ○ |
| 4 | $I_4 \mid \begin{matrix} 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 2 \\ 0 & 0 & 2 & 2 \end{matrix}$ | $X^{16} + 4X^{15}Y + 12X^{14}Y^2 + 28X^{13}Y^3 + 38X^{12}Y^4 + 32X^{11}Y^5 + 28X^{10}Y^6 + 32X^9Y^7 + 33X^8Y^8 + 28X^7Y^9 + 16X^6Y^{10} + 4X^5Y^{11}$ | II | | ○ |
| 5 | $I_4 \mid \begin{matrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{matrix}$ | $X^{16} + 4X^{15}Y + 10X^{14}Y^2 + 20X^{13}Y^3 + 31X^{12}Y^4 + 40X^{11}Y^5 + 44X^{10}Y^6 + 40X^9Y^7 + 31X^8Y^8 + 20X^7Y^9 + 10X^6Y^{10} + 4X^5Y^{11} + X^4Y^{12}$ | II | | ○ |
| 6 | $I_4 \mid \begin{matrix} 2 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{matrix}$ | $X^{16} + 4X^{15}Y + 9X^{14}Y^2 + 18X^{13}Y^3 + 30X^{12}Y^4 + 40X^{11}Y^5 + 46X^{10}Y^6 + 44X^9Y^7 + 33X^8Y^8 + 20X^7Y^9 + 9X^6Y^{10} + 2X^5Y^{11}$ | II | | ○ |
| 7 | $I_4 \mid \begin{matrix} 2 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{matrix}$ | $X^{16} + 4X^{15}Y + 8X^{14}Y^2 + 16X^{13}Y^3 + 30X^{12}Y^4 + 40X^{11}Y^5 + 44X^{10}Y^6 + 48X^9Y^7 + 41X^8Y^8 + 20X^7Y^9 + 4X^6Y^{10}$ | II | | ○ |
| 8 | $I_4 \mid \begin{matrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 \end{matrix}$ | | | | |
| 9 | $I_4 \mid \begin{matrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 \end{matrix}$ | | | | |
| 10 | $I_4 \mid \begin{matrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 0 \\ 0 & 0 & 2 & 2 \end{matrix}$ | $X^{16} + 4X^{15}Y + 8X^{14}Y^2 + 14X^{13}Y^3 + 26X^{12}Y^4 + 44X^{11}Y^5 + 56X^{10}Y^6 + 48X^9Y^7 + 29X^8Y^8 + 16X^7Y^9 + 8X^6Y^{10} + 2X^5Y^{11}$ | II | | ○ |
| 11 | $I_4 \mid \begin{matrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 1 \end{matrix}$ | $X^{16} + 4X^{15}Y + 8X^{14}Y^2 + 12X^{13}Y^3 + 23X^{12}Y^4 + 48X^{11}Y^5 + 64X^{10}Y^6 + 48X^9Y^7 + 23X^8Y^8 + 12X^7Y^9 + 8X^6Y^{10} + 4X^5Y^{11} + X^4Y^{12}$ | II | | ○ |
| 12 | $I_4 \mid \begin{matrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 2 & 0 \end{matrix}$ | $X^{16} + 4X^{15}Y + 7X^{14}Y^2 + 12X^{13}Y^3 + 26X^{12}Y^4 + 44X^{11}Y^5 + 54X^{10}Y^6 + 52X^9Y^7 + 37X^8Y^8 + 16X^7Y^9 + 3X^6Y^{10}$ | II | | ○ |
| 13 | $I_4 \mid \begin{matrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 2 & 2 \end{matrix}$ | | | | |
| 14 | $I_4 \mid \begin{matrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 3 \\ 0 & 0 & 1 & 1 \end{matrix}$ | | | | |
| 15 | $I_4 \mid \begin{matrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 1 & 1 \end{matrix}$ | $X^{16} + 4X^{15}Y + 6X^{14}Y^2 + 8X^{13}Y^3 + 22X^{12}Y^4 + 48X^{11}Y^5 + 64X^{10}Y^6 + 56X^9Y^7 + 33X^8Y^8 + 12X^7Y^9 + 2X^6Y^{10}$ | II | | ○ |

Table 7. Free formally self-dual codes over \mathbb{Z}_4 of length 8 (cont'd.)

| No. | Generator Matrix | Lee weight enumerator | Construction | Even | Non-SD |
|-----|---|---|--------------|------|--------|
| 16 | $I_4 \left \begin{array}{cccc} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 1 \\ 0 & 0 & 1 & 2 \end{array} \right.$ | $X^{16} + 4X^{15}Y + 6X^{14}Y^2 + 4X^{13}Y^3 + 15X^{12}Y^4 + 56X^{11}Y^5 + 84X^{10}Y^6 + 56X^9Y^7 + 15X^8Y^8 + 4X^7Y^9 + 6X^6Y^{10} + 4X^5Y^{11} + X^4Y^{12}$ | II | | ○ |
| 17 | $I_4 \left \begin{array}{cccc} 0 & 0 & 0 & 0 \\ 0 & 2 & 2 & 2 \\ 0 & 2 & 2 & 2 \\ 0 & 2 & 2 & 2 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 16X^{14}Y^2 + 30X^{13}Y^3 + 30X^{12}Y^4 + 30X^{11}Y^5 + 16X^{10}Y^6 + 8X^9Y^7 + 13X^8Y^8 + 26X^7Y^9 + 40X^6Y^{10} + 26X^5Y^{11} + 12X^4Y^{12} + 6X^3Y^{13}$ | II | | ○ |
| 18 | $I_4 \left \begin{array}{cccc} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 2 \\ 0 & 0 & 2 & 2 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 9X^{14}Y^2 + 16X^{13}Y^3 + 22X^{12}Y^4 + 32X^{11}Y^5 + 30X^{10}Y^6 + 32X^9Y^7 + 33X^8Y^8 + 26X^7Y^9 + 25X^6Y^{10} + 16X^5Y^{11} + 8X^4Y^{12} + 4X^3Y^{13}$ | II | | ○ |
| 19 | $I_4 \left \begin{array}{cccc} 0 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 2 & 2 \\ 0 & 2 & 0 & 0 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 8X^{14}Y^2 + 18X^{13}Y^3 + 22X^{12}Y^4 + 28X^{11}Y^5 + 28X^{10}Y^6 + 28X^9Y^7 + 41X^8Y^8 + 34X^7Y^9 + 20X^6Y^{10} + 18X^5Y^{11} + 8X^4Y^{12}$ | II | | ○ |
| 20 | $I_4 \left \begin{array}{cccc} 0 & 0 & 0 & 0 \\ 0 & 2 & 2 & 2 \\ 0 & 2 & 0 & 0 \\ 0 & 2 & 0 & 0 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 8X^{14}Y^2 + 18X^{13}Y^3 + 22X^{12}Y^4 + 26X^{11}Y^5 + 32X^{10}Y^6 + 32X^9Y^7 + 29X^8Y^8 + 34X^7Y^9 + 32X^6Y^{10} + 14X^5Y^{11} + 4X^4Y^{12} + 2X^3Y^{13}$ | II | | ○ |
| 21 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 2 \\ 0 & 0 & 2 & 2 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 8X^{14}Y^2 + 16X^{13}Y^3 + 18X^{12}Y^4 + 32X^{11}Y^5 + 40X^{10}Y^6 + 28X^9Y^7 + 29X^8Y^8 + 30X^7Y^9 + 24X^6Y^{10} + 20X^5Y^{11} + 8X^4Y^{12}$ | II | | ○ |
| 22 | $I_4 \left \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 7X^{14}Y^2 + 12X^{13}Y^3 + 21X^{12}Y^4 + 30X^{11}Y^5 + 35X^{10}Y^6 + 40X^9Y^7 + 35X^8Y^8 + 30X^7Y^9 + 21X^6Y^{10} + 12X^5Y^{11} + 7X^4Y^{12} + 2X^3Y^{13} + X^2Y^{14}$ | II | | ○ |
| 23 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 6X^{14}Y^2 + 12X^{13}Y^3 + 19X^{12}Y^4 + 30X^{11}Y^5 + 36X^{10}Y^6 + 40X^9Y^7 + 39X^8Y^8 + 30X^7Y^9 + 22X^6Y^{10} + 12X^5Y^{11} + 5X^4Y^{12} + 2X^3Y^{13}$ | II | | ○ |
| 24 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 2 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 5X^{14}Y^2 + 12X^{13}Y^3 + 18X^{12}Y^4 + 28X^{11}Y^5 + 38X^{10}Y^6 + 40X^9Y^7 + 41X^8Y^8 + 34X^7Y^9 + 21X^6Y^{10} + 12X^5Y^{11} + 4X^4Y^{12}$ | II | | ○ |
| 25 | $I_4 \left \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 \end{array} \right.$ | | | | |
| 26 | $I_4 \left \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 0 \\ 0 & 0 & 2 & 2 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 5X^{14}Y^2 + 10X^{13}Y^3 + 18X^{12}Y^4 + 30X^{11}Y^5 + 38X^{10}Y^6 + 44X^9Y^7 + 41X^8Y^8 + 30X^7Y^9 + 21X^6Y^{10} + 10X^5Y^{11} + 4X^4Y^{12} + 2X^3Y^{13}$ | II | | ○ |
| 27 | $I_4 \left \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 1 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 5X^{14}Y^2 + 8X^{13}Y^3 + 19X^{12}Y^4 + 30X^{11}Y^5 + 39X^{10}Y^6 + 48X^9Y^7 + 39X^8Y^8 + 30X^7Y^9 + 19X^6Y^{10} + 8X^5Y^{11} + 5X^4Y^{12} + 2X^3Y^{13} + X^2Y^{14}$ | II | | ○ |
| 28 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 \end{array} \right.$ | | | | |
| 29 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 0 \\ 0 & 0 & 0 & 2 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 4X^{14}Y^2 + 12X^{13}Y^3 + 18X^{12}Y^4 + 24X^{11}Y^5 + 40X^{10}Y^6 + 44X^9Y^7 + 37X^8Y^8 + 38X^7Y^9 + 28X^6Y^{10} + 8X^5Y^{11}$ | II | | ○ |
| 30 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 \end{array} \right.$ | | | | |

Table 7. Free formally self-dual codes over \mathbb{Z}_4 of length 8 (cont'd.)

| No. | Generator Matrix | Lee weight enumerator | Construction | Even | Non-SD |
|-----|---|---|--------------|------|--------|
| 31 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 0 \\ 0 & 0 & 2 & 2 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 4X^{14}Y^2 + 10X^{13}Y^3 + 18X^{12}Y^4 + 28X^{11}Y^5 + 36X^{10}Y^6 + 44X^9Y^7 + 49X^8Y^8 + 34X^7Y^9 + 16X^6Y^{10} + 10X^5Y^{11} + 4X^4Y^{12}$ | II | | ○ |
| 32 | $I_4 \left \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 2 & 0 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 4X^{14}Y^2 + 10X^{13}Y^3 + 17X^{12}Y^4 + 28X^{11}Y^5 + 40X^{10}Y^6 + 44X^9Y^7 + 43X^8Y^8 + 34X^7Y^9 + 20X^6Y^{10} + 10X^5Y^{11} + 3X^4Y^{12}$ | II | | ○ |
| 33 | $I_4 \left \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 2 & 2 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 4X^{14}Y^2 + 8X^{13}Y^3 + 19X^{12}Y^4 + 30X^{11}Y^5 + 32X^{10}Y^6 + 48X^9Y^7 + 55X^8Y^8 + 30X^7Y^9 + 12X^6Y^{10} + 8X^5Y^{11} + 5X^4Y^{12} + 2X^3Y^{13}$ | II) | | ○ |
| 34 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 1 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 3X^{14}Y^2 + 10X^{13}Y^3 + 18X^{12}Y^4 + 24X^{11}Y^5 + 38X^{10}Y^6 + 48X^9Y^7 + 45X^8Y^8 + 38X^7Y^9 + 23X^6Y^{10} + 6X^5Y^{11}$ | II | | ○ |
| 35 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 2 & 0 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 3X^{14}Y^2 + 8X^{13}Y^3 + 16X^{12}Y^4 + 28X^{11}Y^5 + 42X^{10}Y^6 + 48X^9Y^7 + 45X^8Y^8 + 34X^7Y^9 + 19X^6Y^{10} + 8X^5Y^{11} + 2X^4Y^{12}$ | II | | ○ |
| 36 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 2 & 0 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 3X^{14}Y^2 + 8X^{13}Y^3 + 17X^{12}Y^4 + 30X^{11}Y^5 + 43X^{10}Y^6 + 56X^9Y^7 + 43X^8Y^8 + 30X^7Y^9 + 17X^6Y^{10} + 4X^5Y^{11} + 3X^4Y^{12} + 2X^3Y^{13} + X^2Y^{14}$ | II | | ○ |
| 37 | $I_4 \left \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 1 & 1 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 3X^{14}Y^2 + 8X^{13}Y^3 + 16X^{12}Y^4 + 28X^{11}Y^5 + 42X^{10}Y^6 + 48X^9Y^7 + 45X^8Y^8 + 34X^7Y^9 + 19X^6Y^{10} + 8X^5Y^{11} + 2X^4Y^{12}$ | II | | ○ |
| 38 | $I_4 \left \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 1 & 1 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 3X^{14}Y^2 + 8X^{13}Y^3 + 17X^{12}Y^4 + 30X^{11}Y^5 + 43X^{10}Y^6 + 56X^9Y^7 + 43X^8Y^8 + 30X^7Y^9 + 17X^6Y^{10} + 4X^5Y^{11} + 3X^4Y^{12} + 2X^3Y^{13} + X^2Y^{14}$ | II | | ○ |
| 40 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 1 & 1 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 2X^{14}Y^2 + 8X^{13}Y^3 + 18X^{12}Y^4 + 24X^{11}Y^5 + 36X^{10}Y^6 + 52X^9Y^7 + 53X^8Y^8 + 38X^7Y^9 + 18X^6Y^{10} + 4X^5Y^{11}$ | II | | ○ |
| 41 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 3 \\ 0 & 0 & 1 & 1 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 2X^{14}Y^2 + 4X^{13}Y^3 + 19X^{12}Y^4 + 30X^{11}Y^5 + 28X^{10}Y^6 + 56X^9Y^7 + 71X^8Y^8 + 30X^7Y^9 + 2X^6Y^{10} + 4X^5Y^{11} + 5X^4Y^{12} + 2X^3Y^{13}$ | II | | ○ |
| 42 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 2 & 1 \\ 0 & 0 & 1 & 2 \end{array} \right.$ | $X^{16} + 2X^{15}Y + 2X^{14}Y^2 + 4X^{13}Y^3 + 19X^{12}Y^4 + 30X^{11}Y^5 + 28X^{10}Y^6 + 56X^9Y^7 + 71X^8Y^8 + 30X^7Y^9 + 2X^6Y^{10} + 4X^5Y^{11} + 5X^4Y^{12} + 2X^3Y^{13}$ | II | | ○ |
| 43 | $I_4 \left \begin{array}{cccc} 2 & 2 & 2 & 2 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 2 & 2 \end{array} \right.$ | $X^{16} + 28X^{14}Y^2 + 70X^{12}Y^4 + 28X^{10}Y^6 + X^8Y^8 + 8X^7Y^9 + 56X^5Y^{11} + 56X^3Y^{13} + 8XY^{15}$ | I-(iv) | | ○ |
| 44 | $I_4 \left \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 2 & 2 & 2 \\ 0 & 2 & 2 & 2 \\ 0 & 2 & 2 & 2 \end{array} \right.$ | $X^{16} + 17X^{14}Y^2 + 46X^{12}Y^4 + 46X^{10}Y^6 + 6X^9Y^7 + 17X^8Y^8 + 32X^7Y^9 + X^6Y^{10} + 52X^5Y^{11} + 32X^3Y^{13} + 6XY^{15}$ | I-(i) | | ○ |
| 45 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 2 & 2 & 2 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 0 & 0 \end{array} \right.$ | $X^{16} + 16X^{14}Y^2 + 6X^{13}Y^3 + 30X^{12}Y^4 + 26X^{11}Y^5 + 16X^{10}Y^6 + 28X^9Y^7 + X^8Y^8 + 36X^7Y^9 + 12X^6Y^{10} + 30X^5Y^{11} + 40X^4Y^{12} + 2X^3Y^{13} + 12X^2Y^{14}$ | I-(ii) | | ○ |
| 46 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 2 & 2 & 2 & 2 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 0 & 0 \end{array} \right.$ | $X^{16} + 16X^{14}Y^2 + 6X^{13}Y^3 + 30X^{12}Y^4 + 26X^{11}Y^5 + 16X^{10}Y^6 + 28X^9Y^7 + X^8Y^8 + 36X^7Y^9 + 12X^6Y^{10} + 30X^5Y^{11} + 40X^4Y^{12} + 2X^3Y^{13} + 12X^2Y^{14}$ | I-(v) | | |

Table 7. Free formally self-dual codes over \mathbb{Z}_4 of length 8 (cont'd.)

| No. | Generator Matrix | Lee weight enumerator | Construction | Even | Non-SD |
|-----|---|--|--------------|------|--------|
| 47 | $I_4 \left \begin{array}{cccc} 2 & 2 & 2 & 2 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 0 & 0 \end{array} \right.$ | $X^{16} + 16X^{14}Y^2 + 6X^{13}Y^3 + 30X^{12}Y^4 + 26X^{11}Y^5 + 16X^{10}Y^6 + 26X^9Y^7 + 13X^8Y^8 + 8X^7Y^9 + 40X^6Y^{10} + 30X^5Y^{11} + 12X^4Y^{12} + 30X^3Y^{13} + 2XY^{15}$ | I-(iv) | | ○ |
| 48 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 2 & 2 & 2 \\ 0 & 2 & 2 & 2 \\ 0 & 2 & 2 & 2 \end{array} \right.$ | $X^{16} + 16X^{14}Y^2 + 2X^{13}Y^3 + 30X^{12}Y^4 + 30X^{11}Y^5 + 16X^{10}Y^6 + 36X^9Y^7 + X^8Y^8 + 28X^7Y^9 + 12X^6Y^{10} + 26X^5Y^{11} + 40X^4Y^{12} + 6X^3Y^{13} + 12X^2Y^{14}$ | I-(ii) | | ○ |
| 49 | $I_4 \left \begin{array}{cccc} 2 & 2 & 2 & 2 \\ 0 & 2 & 2 & 2 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 2 & 2 \end{array} \right.$ | $X^{16} + 16X^{14}Y^2 + 42X^{12}Y^4 + 56X^{10}Y^6 + 2X^9Y^7 + 13X^8Y^8 + 36X^7Y^9 + 56X^5Y^{11} + 28X^3Y^{13} + 6XY^{15}$ | I-(ii) | | ○ |
| 50 | $I_4 \left \begin{array}{cccc} 1 & 2 & 2 & 2 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 2 & 2 \end{array} \right.$ | $X^{16} + 15X^{14}Y^2 + 12X^{13}Y^3 + 16X^{12}Y^4 + 40X^{11}Y^5 + 16X^{10}Y^6 + 12X^9Y^7 + 17X^8Y^8 + 12X^7Y^9 + 31X^6Y^{10} + 40X^5Y^{11} + 30X^4Y^{12} + 12X^3Y^{13} + 2X^2Y^{14}$ | I-(i) | | ○ |
| 51 | $I_4 \left \begin{array}{cccc} 1 & 2 & 2 & 2 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 0 & 0 \end{array} \right.$ | | | | |
| 52 | $I_4 \left \begin{array}{cccc} 2 & 2 & 2 & 2 \\ 2 & 2 & 0 & 0 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 0 & 0 \end{array} \right.$ | $X^{16} + 12X^{14}Y^2 + 38X^{12}Y^4 + 4X^{11}Y^5 + 28X^{10}Y^6 + 28X^9Y^7 + 33X^8Y^8 + 32X^7Y^9 + 16X^6Y^{10} + 32X^5Y^{11} + 28X^3Y^{13} + 4XY^{15}$ | I-(iv),(v) | | ○ |
| 53 | $I_4 \left \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 2 & 2 \\ 0 & 0 & 2 & 2 \end{array} \right.$ | $X^{16} + 10X^{14}Y^2 + 31X^{12}Y^4 + 4X^{11}Y^5 + 44X^{10}Y^6 + 20X^9Y^7 + 31X^8Y^8 + 40X^7Y^9 + 10X^6Y^{10} + 40X^5Y^{11} + X^4Y^{12} + 20X^3Y^{13} + 4XY^{15}$ | I-(iv) | | ○ |
| 54 | $I_4 \left \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 2 & 2 \\ 0 & 2 & 0 & 0 \end{array} \right.$ | $X^{16} + 9X^{14}Y^2 + 2X^{13}Y^3 + 22X^{12}Y^4 + 20X^{11}Y^5 + 22X^{10}Y^6 + 44X^9Y^7 + 17X^8Y^8 + 40X^7Y^9 + 25X^6Y^{10} + 18X^5Y^{11} + 24X^4Y^{12} + 4X^3Y^{13} + 8X^2Y^{14}$ | I-(v) | | ○ |
| 55 | $I_4 \left \begin{array}{cccc} 1 & 0 & 0 & 0 \\ 0 & 2 & 2 & 2 \\ 0 & 2 & 0 & 0 \\ 0 & 2 & 0 & 0 \end{array} \right.$ | $X^{16} + 9X^{14}Y^2 + 4X^{13}Y^3 + 22X^{12}Y^4 + 16X^{11}Y^5 + 30X^{10}Y^6 + 26X^9Y^7 + 33X^8Y^8 + 32X^7Y^9 + 25X^6Y^{10} + 32X^5Y^{11} + 8X^4Y^{12} + 16X^3Y^{13} + 2XY^{15}$ | I-(i) | | ○ |
| 56 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 2 & 2 \\ 0 & 0 & 2 & 2 \end{array} \right.$ | $X^{16} + 9X^{14}Y^2 + 4X^{13}Y^3 + 22X^{12}Y^4 + 18X^{11}Y^5 + 22X^{10}Y^6 + 40X^9Y^7 + 17X^8Y^8 + 44X^7Y^9 + 25X^6Y^{10} + 20X^5Y^{11} + 24X^4Y^{12} + 2X^3Y^{13} + 8X^2Y^{14}$ | I-(i) | | ○ |
| 57 | $I_4 \left \begin{array}{cccc} 2 & 2 & 0 & 0 \\ 0 & 2 & 2 & 2 \\ 2 & 2 & 0 & 0 \\ 2 & 0 & 2 & 2 \end{array} \right.$ | $X^{16} + 8X^{14}Y^2 + 16X^{13}Y^3 + 14X^{12}Y^4 + 20X^{11}Y^5 + 12X^{10}Y^6 + 16X^9Y^7 + 41X^8Y^8 + 40X^7Y^9 + 36X^6Y^{10} + 32X^5Y^{11} + 16X^4Y^{12} + 4X^3Y^{13}$ | I-(ii) | | ○ |
| 58 | $I_4 \left \begin{array}{cccc} 2 & 0 & 2 & 2 \\ 0 & 2 & 2 & 2 \\ 2 & 0 & 2 & 2 \\ 2 & 2 & 0 & 0 \end{array} \right.$ | $X^{16} + 8X^{14}Y^2 + 16X^{13}Y^3 + 14X^{12}Y^4 + 18X^{11}Y^5 + 16X^{10}Y^6 + 20X^9Y^7 + 29X^8Y^8 + 40X^7Y^9 + 48X^6Y^{10} + 28X^5Y^{11} + 12X^4Y^{12} + 6X^3Y^{13}$ | I-(iii) | | ○ |
| 59 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 \\ 0 & 0 & 2 & 2 \\ 0 & 0 & 2 & 0 \end{array} \right.$ | $X^{16} + 8X^{14}Y^2 + 6X^{13}Y^3 + 14X^{12}Y^4 + 28X^{11}Y^5 + 16X^{10}Y^6 + 40X^9Y^7 + 29X^8Y^8 + 20X^7Y^9 + 48X^6Y^{10} + 18X^5Y^{11} + 12X^4Y^{12} + 16X^3Y^{13}$ | I-(v) | | ○ |
| 60 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 2 & 2 & 2 \\ 0 & 2 & 0 & 0 \\ 0 & 2 & 0 & 0 \end{array} \right.$ | | | | |

Table 7. Free formally self-dual codes over \mathbb{Z}_4 of length 8 (cont'd)

| No. | Generator Matrix | Lee weight enumerator | Construction | Even | Non-SD |
|-----|---|---|--------------|------|--------|
| 61 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 2 & 2 & 2 & 2 \\ 2 & 0 & 0 & 2 \\ 2 & 0 & 0 & 0 \end{array} \right.$ | $X^{16} + 8X^{14}Y^2 + 4X^{13}Y^3 + 22X^{12}Y^4 + 14X^{11}Y^5 + 28X^{10}Y^6 + 26X^9Y^7 + 41X^8Y^8 + 36X^7Y^9 + 20X^6Y^{10} + 32X^5Y^{11} + 8X^4Y^{12} + 14X^3Y^{13} + 2XY^{15}$ | I-(v) | | ○ |
| 62 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 0 \\ 0 & 2 & 2 & 2 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 0 & 0 \end{array} \right.$ | $X^{16} + 8X^{14}Y^2 + 4X^{13}Y^3 + 22X^{12}Y^4 + 14X^{11}Y^5 + 24X^{10}Y^6 + 44X^9Y^7 + 13X^8Y^8 + 48X^7Y^9 + 32X^6Y^{10} + 16X^5Y^{11} + 20X^4Y^{12} + 2X^3Y^{13} + 8X^2Y^{14}$ | I-(iii) | | ○ |
| 63 | $I_4 \left \begin{array}{cccc} 2 & 0 & 2 & 2 \\ 2 & 2 & 2 & 2 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 2 & 2 \end{array} \right.$ | $X^{16} + 8X^{14}Y^2 + 2X^{13}Y^3 + 22X^{12}Y^4 + 14X^{11}Y^5 + 32X^{10}Y^6 + 34X^9Y^7 + 29X^8Y^8 + 32X^7Y^9 + 32X^6Y^{10} + 26X^5Y^{11} + 4X^4Y^{12} + 18X^3Y^{13} + 2XY^{15}$ | I-(iv),(v) | | ○ |
| 64 | $I_4 \left \begin{array}{cccc} 2 & 0 & 2 & 2 \\ 0 & 2 & 2 & 2 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 2 & 2 \end{array} \right.$ | $X^{16} + 8X^{14}Y^2 + 2X^{13}Y^3 + 14X^{12}Y^4 + 30X^{11}Y^5 + 24X^{10}Y^6 + 36X^9Y^7 + 33X^8Y^8 + 28X^7Y^9 + 20X^6Y^{10} + 26X^5Y^{11} + 24X^4Y^{12} + 6X^3Y^{13} + 4X^2Y^{14}$ | I-(iii) | | ○ |
| 65 | $I_4 \left \begin{array}{cccc} 2 & 2 & 2 & 2 \\ 0 & 2 & 2 & 2 \\ 2 & 2 & 2 & 0 \\ 2 & 2 & 2 & 2 \end{array} \right.$ | $X^{16} + 8X^{14}Y^2 + 30X^{12}Y^4 + 44X^{10}Y^6 + 20X^9Y^7 + 41X^8Y^8 + 48X^7Y^9 + 4X^6Y^{10} + 40X^5Y^{11} + 16X^3Y^{13} + 4XY^{15}$ | I-(ii) | | ○ |
| 66 | $I_4 \left \begin{array}{cccc} 2 & 2 & 1 & 1 \\ 1 & 2 & 2 & 2 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 1 & 1 \end{array} \right.$ | | I-(v) | | |
| 67 | $I_4 \left \begin{array}{cccc} 2 & 2 & 0 & 0 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 0 & 2 \end{array} \right.$ | $X^{16} + 8X^{14}Y^2 + 26X^{12}Y^4 + 2X^{11}Y^5 + 56X^{10}Y^6 + 16X^9Y^7 + 29X^8Y^8 + 48X^7Y^9 + 8X^6Y^{10} + 44X^5Y^{11} + 14X^3Y^{13} + 4XY^{15}$ | I-(v) | | ○ |
| 68 | $I_4 \left \begin{array}{cccc} 2 & 0 & 2 & 2 \\ 2 & 2 & 2 & 2 \\ 2 & 0 & 2 & 2 \\ 2 & 2 & 0 & 0 \end{array} \right.$ | $X^{16} + 8X^{14}Y^2 + 22X^{12}Y^4 + 18X^{11}Y^5 + 28X^{10}Y^6 + 34X^9Y^7 + 41X^8Y^8 + 28X^7Y^9 + 20X^6Y^{10} + 28X^5Y^{11} + 8X^4Y^{12} + 18X^3Y^{13} + 2XY^{15}$ | I-(v) | | ○ |
| 69 | $I_4 \left \begin{array}{cccc} 2 & 2 & 2 & 2 \\ 2 & 2 & 0 & 0 \\ 2 & 2 & 0 & 0 \\ 2 & 0 & 2 & 2 \end{array} \right.$ | $X^{16} + 8X^{14}Y^2 + 18X^{12}Y^4 + 20X^{11}Y^5 + 40X^{10}Y^6 + 30X^9Y^7 + 29X^8Y^8 + 28X^7Y^9 + 24X^6Y^{10} + 32X^5Y^{11} + 8X^4Y^{12} + 16X^3Y^{13} + 2XY^{15}$ | I-(ii),(iv) | | ○ |
| 70 | $I_4 \left \begin{array}{cccc} 1 & 2 & 2 & 2 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 0 & 0 \\ 2 & 2 & 2 & 2 \end{array} \right.$ | $X^{16} + 7X^{14}Y^2 + 8X^{13}Y^3 + 16X^{12}Y^4 + 20X^{11}Y^5 + 16X^{10}Y^6 + 36X^9Y^7 + 33X^8Y^8 + 36X^7Y^9 + 39X^6Y^{10} + 20X^5Y^{11} + 14X^4Y^{12} + 8X^3Y^{13} + 2X^2Y^{14}$ | I-(i) | | ○ |
| 71 | $I_4 \left \begin{array}{cccc} 3 & 2 & 2 & 2 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 0 & 2 \\ 2 & 0 & 0 & 0 \end{array} \right.$ | | | | |
| 72 | $I_4 \left \begin{array}{cccc} 1 & 2 & 2 & 2 \\ 2 & 2 & 0 & 0 \\ 2 & 2 & 2 & 0 \\ 2 & 2 & 0 & 0 \end{array} \right.$ | $X^{16} + 7X^{14}Y^2 + 4X^{13}Y^3 + 8X^{12}Y^4 + 32X^{11}Y^5 + 32X^{10}Y^6 + 28X^9Y^7 + 33X^8Y^8 + 28X^7Y^9 + 23X^6Y^{10} + 32X^5Y^{11} + 22X^4Y^{12} + 4X^3Y^{13} + 2X^2Y^{14}$ | I-(i) | | ○ |
| 73 | $I_4 \left \begin{array}{cccc} 1 & 2 & 2 & 2 \\ 2 & 0 & 2 & 2 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 2 & 2 \end{array} \right.$ | | | | |
| 74 | $I_4 \left \begin{array}{cccc} 1 & 2 & 2 & 2 \\ 2 & 0 & 2 & 2 \\ 2 & 0 & 2 & 2 \\ 2 & 2 & 0 & 0 \end{array} \right.$ | $X^{16} + 7X^{14}Y^2 + 24X^{12}Y^4 + 12X^{11}Y^5 + 24X^{10}Y^6 + 52X^9Y^7 + 17X^8Y^8 + 52X^7Y^9 + 23X^6Y^{10} + 12X^5Y^{11} + 22X^4Y^{12} + 10X^2Y^{14}$ | I-(i) | | ○ |
| 75 | $I_4 \left \begin{array}{cccc} 1 & 2 & 2 & 2 \\ 2 & 2 & 0 & 0 \\ 2 & 2 & 0 & 0 \\ 2 & 0 & 2 & 2 \end{array} \right.$ | | | | |
| 76 | $I_4 \left \begin{array}{cccc} 2 & 2 & 3 & 3 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 3 & 1 \end{array} \right.$ | $X^{16} + 6X^{14}Y^2 + 22X^{12}Y^4 + 64X^{10}Y^6 + 12X^9Y^7 + 33X^8Y^8 + 56X^7Y^9 + 2X^6Y^{10} + 48X^5Y^{11} + 8X^3Y^{13} + 4XY^{15}$ | I-(v) | | ○ |

Table 7. Free formally self-dual codes over \mathbb{Z}_4 of length 8 (cont'd)

| No. | Generator Matrix | Lee weight enumerator | Construction | Even | Non-SD |
|-----|---|---|--------------|------|--------|
| 77 | $I_4 \left \begin{array}{cccc} 2 & 0 & 2 & 2 \\ 2 & 2 & 2 & 2 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 2 & 0 \end{array} \right.$ | $X^{16} + 4X^{14}Y^2 + 2X^{13}Y^3 + 18X^{12}Y^4 + 8X^{11}Y^5 + 36X^{10}Y^6 + 30X^9Y^7 + 49X^8Y^8 + 48X^7Y^9 + 16X^6Y^{10} + 30X^5Y^{11} + 4X^4Y^{12} + 8X^3Y^{13} + 2XY^{15}$ | I-(iv) | | ○ |
| 78 | $I_4 \left \begin{array}{cccc} 2 & 0 & 2 & 2 \\ 0 & 2 & 2 & 2 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 2 & 0 \end{array} \right.$ | $X^{16} + 4X^{14}Y^2 + 2X^{13}Y^3 + 14X^{12}Y^4 + 16X^{11}Y^5 + 28X^{10}Y^6 + 48X^9Y^7 + 29X^8Y^8 + 44X^7Y^9 + 36X^6Y^{10} + 14X^5Y^{11} + 12X^4Y^{12} + 4X^3Y^{13} + 4X^2Y^{14}$ | I-(iii) | | ○ |
| 79 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 2 \\ 2 & 2 & 2 & 2 \\ 2 & 0 & 2 & 0 \\ 2 & 2 & 0 & 0 \end{array} \right.$ | $X^{16} + 4X^{14}Y^2 + 22X^{12}Y^4 + 6X^{11}Y^5 + 28X^{10}Y^6 + 42X^9Y^7 + 49X^8Y^8 + 44X^7Y^9 + 24X^6Y^{10} + 20X^5Y^{11} + 14X^3Y^{13} + 2XY^{15}$ | I-(v) | | ○ |
| 80 | $I_4 \left \begin{array}{cccc} 2 & 0 & 3 & 3 \\ 2 & 2 & 2 & 2 \\ 2 & 0 & 3 & 3 \\ 2 & 2 & 0 & 0 \end{array} \right.$ | $X^{16} + 4X^{14}Y^2 + 18X^{12}Y^4 + 10X^{11}Y^5 + 36X^{10}Y^6 + 34X^9Y^7 + 49X^8Y^8 + 44X^7Y^9 + 16X^6Y^{10} + 28X^5Y^{11} + 4X^4Y^{12} + 10X^3Y^{13} + 2XY^{15}$ | | | |
| 81 | $I_4 \left \begin{array}{cccc} 2 & 2 & 0 & 0 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 0 & 2 \\ 2 & 2 & 0 & 2 \end{array} \right.$ | $X^{16} + 4X^{14}Y^2 + 18X^{12}Y^4 + 10X^{11}Y^5 + 36X^{10}Y^6 + 34X^9Y^7 + 49X^8Y^8 + 44X^7Y^9 + 16X^6Y^{10} + 28X^5Y^{11} + 4X^4Y^{12} + 10X^3Y^{13} + 2XY^{15}$ | I-(ii) | | ○ |
| 82 | $I_4 \left \begin{array}{cccc} 2 & 2 & 2 & 2 \\ 2 & 2 & 2 & 0 \\ 2 & 2 & 0 & 2 \\ 2 & 0 & 2 & 2 \end{array} \right.$ | $X^{16} + 4X^{14}Y^2 + 18X^{12}Y^4 + 8X^{11}Y^5 + 40X^{10}Y^6 + 38X^9Y^7 + 37X^8Y^8 + 44X^7Y^9 + 28X^6Y^{10} + 24X^5Y^{11} + 12X^3Y^{13} + 2XY^{15}$ | I-(iv) | | ○ |
| 83 | $I_4 \left \begin{array}{cccc} 2 & 2 & 2 & 2 \\ 2 & 2 & 1 & 1 \\ 2 & 2 & 1 & 1 \\ 2 & 0 & 2 & 2 \end{array} \right.$ | $X^{16} + 4X^{14}Y^2 + 18X^{12}Y^4 + 8X^{11}Y^5 + 40X^{10}Y^6 + 38X^9Y^7 + 37X^8Y^8 + 44X^7Y^9 + 28X^6Y^{10} + 24X^5Y^{11} + 12X^3Y^{13} + 2XY^{15}$ | | | |
| 84 | $I_4 \left \begin{array}{cccc} 2 & 2 & 2 & 0 \\ 0 & 2 & 2 & 2 \\ 2 & 2 & 0 & 2 \\ 2 & 0 & 2 & 2 \end{array} \right.$ | $X^{16} + 4X^{14}Y^2 + 6X^{12}Y^4 + 32X^{11}Y^5 + 28X^{10}Y^6 + 40X^9Y^7 + 49X^8Y^8 + 24X^7Y^9 + 24X^6Y^{10} + 24X^5Y^{11} + 16X^4Y^{12} + 8X^3Y^{13}$ | I-(ii) | | ○ |
| 85 | $I_4 \left \begin{array}{cccc} 2 & 2 & 1 & 1 \\ 0 & 2 & 2 & 2 \\ 2 & 2 & 1 & 1 \\ 2 & 0 & 2 & 2 \end{array} \right.$ | $X^{16} + 4X^{14}Y^2 + 6X^{12}Y^4 + 32X^{11}Y^5 + 28X^{10}Y^6 + 40X^9Y^7 + 49X^8Y^8 + 24X^7Y^9 + 24X^6Y^{10} + 24X^5Y^{11} + 16X^4Y^{12} + 8X^3Y^{13}$ | | | |
| 86 | $I_4 \left \begin{array}{cccc} 2 & 0 & 0 & 2 \\ 0 & 2 & 2 & 2 \\ 2 & 0 & 2 & 0 \\ 2 & 2 & 0 & 0 \end{array} \right.$ | $X^{16} + 4X^{14}Y^2 + 6X^{12}Y^4 + 30X^{11}Y^5 + 32X^{10}Y^6 + 44X^9Y^7 + 37X^8Y^8 + 24X^7Y^9 + 36X^6Y^{10} + 20X^5Y^{11} + 12X^4Y^{12} + 10X^3Y^{13}$ | I-(iii) | | ○ |
| 87 | $I_4 \left \begin{array}{cccc} 2 & 0 & 3 & 3 \\ 0 & 2 & 2 & 2 \\ 2 & 0 & 3 & 3 \\ 2 & 2 & 0 & 0 \end{array} \right.$ | $X^{16} + 4X^{14}Y^2 + 6X^{12}Y^4 + 30X^{11}Y^5 + 32X^{10}Y^6 + 44X^9Y^7 + 37X^8Y^8 + 24X^7Y^9 + 36X^6Y^{10} + 20X^5Y^{11} + 12X^4Y^{12} + 10X^3Y^{13}$ | | | |
| 88 | $I_4 \left \begin{array}{cccc} 1 & 2 & 2 & 2 \\ 2 & 2 & 0 & 0 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 0 & 2 \end{array} \right.$ | $X^{16} + 3X^{14}Y^2 + 4X^{13}Y^3 + 12X^{12}Y^4 + 16X^{11}Y^5 + 24X^{10}Y^6 + 44X^9Y^7 + 41X^8Y^8 + 44X^7Y^9 + 35X^6Y^{10} + 16X^5Y^{11} + 10X^4Y^{12} + 4X^3Y^{13} + 2X^2Y^{14}$ | I-(i) | | |
| 89 | $I_4 \left \begin{array}{cccc} 3 & 2 & 2 & 2 \\ 2 & 0 & 2 & 2 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 2 & 0 \end{array} \right.$ | | | | |
| 90 | $I_4 \left \begin{array}{cccc} 1 & 2 & 2 & 2 \\ 2 & 0 & 0 & 2 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 2 & 0 \end{array} \right.$ | | | | ○ |
| 91 | $I_4 \left \begin{array}{cccc} 1 & 2 & 2 & 2 \\ 2 & 2 & 2 & 0 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 0 & 2 \end{array} \right.$ | | | | |
| 92 | $I_4 \left \begin{array}{cccc} 1 & 2 & 2 & 2 \\ 2 & 0 & 1 & 1 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 1 & 1 \end{array} \right.$ | | | | |
| 93 | $I_4 \left \begin{array}{cccc} 3 & 2 & 2 & 2 \\ 2 & 2 & 3 & 3 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 3 & 3 \end{array} \right.$ | | | | |

Table 7. Free formally self-dual codes over \mathbb{Z}_4 of length 8 (cont'd)

| No. | Generator Matrix | Lee weight enumerator | Construction | Even | Non-SD |
|-----|---|--|--------------|------|--------|
| 94 | $I_4 \mid \begin{array}{cccc} 1 & 2 & 2 & 2 \\ 2 & 2 & 2 & 0 \\ 2 & 2 & 0 & 2 \\ 2 & 0 & 2 & 2 \end{array}$ | | | | |
| 95 | $I_4 \mid \begin{array}{cccc} 1 & 2 & 2 & 2 \\ 2 & 2 & 1 & 1 \\ 2 & 2 & 1 & 1 \\ 2 & 0 & 2 & 1 \end{array}$ | $X^{16} + 3X^{14}Y^2 + 4X^{12}Y^4 + 28X^{11}Y^5 + 40X^{10}Y^6 + 36X^9Y^7 + 41X^8Y^8 + 36X^7Y^9 + 19X^6Y^{10} + 28X^5Y^{11} + 18X^4Y^{12} + 2X^2Y^{14}$ | I-(i) | | ○ |
| 96 | $I_4 \mid \begin{array}{cccc} 3 & 2 & 2 & 2 \\ 2 & 0 & 3 & 3 \\ 2 & 0 & 3 & 3 \\ 2 & 2 & 0 & 0 \end{array}$ | | | | |
| 97 | $I_4 \mid \begin{array}{cccc} 3 & 2 & 2 & 2 \\ 2 & 0 & 0 & 2 \\ 2 & 0 & 2 & 0 \\ 2 & 2 & 0 & 0 \end{array}$ | | | | |
| 98 | $I_4 \mid \begin{array}{cccc} 2 & 0 & 1 & 1 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 1 & 3 \end{array}$ | $X^{16} + 2X^{14}Y^2 + 2X^{13}Y^3 + 14X^{12}Y^4 + 10X^{11}Y^5 + 28X^{10}Y^6 + 52X^9Y^7 + 33X^8Y^8 + 52X^7Y^9 + 38X^6Y^{10} + 10X^5Y^{11} + 8X^4Y^{12} + 2X^3Y^{13} + 4X^2Y^{14}$ | I-(ii) | | ○ |
| 99 | $I_4 \mid \begin{array}{cccc} 2 & 2 & 2 & 2 \\ 2 & 0 & 1 & 1 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 1 & 3 \end{array}$ | $X^{16} + 2X^{14}Y^2 + 2X^{13}Y^3 + 14X^{12}Y^4 + 6X^{11}Y^5 + 44X^{10}Y^6 + 26X^9Y^7 + 53X^8Y^8 + 56X^7Y^9 + 10X^6Y^{10} + 34X^5Y^{11} + 4X^4Y^{12} + 2X^3Y^{13} + 2XY^{15}$ | I-(iii) | | ○ |
| 100 | $I_4 \mid \begin{array}{cccc} 2 & 2 & 3 & 3 \\ 0 & 2 & 2 & 2 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 3 & 1 \end{array}$ | $X^{16} + 2X^{14}Y^2 + 18X^{12}Y^4 + 4X^{11}Y^5 + 36X^{10}Y^6 + 38X^9Y^7 + 53X^8Y^8 + 52X^7Y^9 + 18X^6Y^{10} + 24X^5Y^{11} + 8X^3Y^{13} + 2XY^{15}$ | I-(iv) | | ○ |
| 101 | $I_4 \mid \begin{array}{cccc} 1 & 2 & 2 & 2 \\ 2 & 0 & 1 & 1 \\ 2 & 0 & 0 & 0 \\ 2 & 0 & 1 & 3 \end{array}$ | $X^{16} + X^{14}Y^2 + 4X^{13}Y^3 + 14X^{12}Y^4 + 8X^{11}Y^5 + 20X^{10}Y^6 + 52X^9Y^7 + 45X^8Y^8 + 52X^7Y^9 + 41X^6Y^{10} + 8X^5Y^{11} + 4X^4Y^{12} + 4X^3Y^{13} + 2X^2Y^{14}$ | I-(i) | | ○ |
| 102 | $I_4 \mid \begin{array}{cccc} 3 & 2 & 2 & 2 \\ 2 & 2 & 3 & 3 \\ 2 & 2 & 2 & 2 \\ 2 & 2 & 3 & 1 \end{array}$ | | | | |

| No. | Generator matrix | Lee weight enumerator | SD |
|-----|--|---|----|
| 103 | [1 0 0 0 1 0 2 2] [0 1 0 0 2 0 0 0] [0 0 1 0 2 0 0 0] [0 0 0 1 0 1 0 0] | $X^{16} + 8*X^{14}*Y^2 + 8*X^{13}*Y^3 + 15*X^{12}*Y^4 + 24*X^{11}*Y^5 + 18*X^{10}*Y^6 + 32*X^9*Y^7 + 31*X^8*Y^8 + 32*X^7*Y^9 + 36*X^6*Y^{10} + 24*X^5*Y^{11} + 17*X^4*Y^{12} + 8*X^3*Y^{13} + 2*X^2*Y^{14}$ | |
| 104 | [1 0 0 0 3 0 2 2] [0 1 0 0 2 0 2 2] [0 0 1 0 2 0 2 2] [0 0 0 1 0 1 0 0] | | |
| 105 | [1 0 0 0 2 0 0 0] [0 1 0 0 0 0 2 2] [0 0 1 0 2 0 0 0] [0 0 0 1 0 1 0 0] | $X^{16} + 9*X^{14}*Y^2 + 4*X^{13}*Y^3 + 22*X^{12}*Y^4 + 18*X^{11}*Y^5 + 22*X^{10}*Y^6 + 40*X^9*Y^7 + 17*X^8*Y^8 + 44*X^7*Y^9 + 25*X^6*Y^{10} + 20*X^5*Y^{11} + 24*X^4*Y^{12} + 2*X^3*Y^{13} + 8*X^2*Y^{14}$ | |
| 106 | [1 0 0 0 2 0 2 2] [0 1 0 0 0 0 2 2] [0 0 1 0 2 0 2 2] [0 0 0 1 0 1 0 0] | $X^{16} + 9*X^{14}*Y^2 + 30*X^{12}*Y^4 + 2*X^{11}*Y^5 + 46*X^{10}*Y^6 + 20*X^9*Y^7 + 33*X^8*Y^8 + 44*X^7*Y^9 + 9*X^6*Y^{10} + 40*X^5*Y^{11} + 18*X^3*Y^{13} + 4*X*Y^{15}$ | |
| 107 | [1 0 0 0 2 0 2 0] [0 1 0 0 2 0 2 2] [0 0 1 0 0 1 0 0] [0 0 0 1 2 0 2 2] | | |
| 108 | [1 0 0 0 2 0 2 2] [0 1 0 0 2 0 0 0] [0 0 1 0 2 0 0 0] [0 0 0 1 0 1 0 0] | $X^{16} + 9*X^{14}*Y^2 + 4*X^{13}*Y^3 + 22*X^{12}*Y^4 + 16*X^{11}*Y^5 + 30*X^{10}*Y^6 + 26*X^9*Y^7 + 33*X^8*Y^8 + 32*X^7*Y^9 + 25*X^6*Y^{10} + 32*X^5*Y^{11} + 8*X^4*Y^{12} + 16*X^3*Y^{13} + 2*X*Y^{15}$ | |
| 109 | [1 0 0 0 2 0 2 2] [0 1 0 0 2 0 2 2] [0 0 1 0 2 0 2 2] [0 0 0 1 0 1 0 0] | $X^{16} + 17*X^{14}*Y^2 + 46*X^{12}*Y^4 + 46*X^{10}*Y^6 + 6*X^9*Y^7 + 17*X^8*Y^8 + 32*X^7*Y^9 + X^6*Y^{10} + 52*X^5*Y^{11} + 32*X^3*Y^{13} + 6*X*Y^{15}$ | |
| 110 | [1 0 0 0 1 0 0 2] [0 1 0 0 2 0 0 0] [0 0 1 0 0 1 0 0] [0 0 0 1 0 0 1 0] | $X^{16} + 5*X^{14}*Y^2 + 4*X^{13}*Y^3 + 13*X^{12}*Y^4 + 20*X^{11}*Y^5 + 25*X^{10}*Y^6 + 40*X^9*Y^7 + 35*X^8*Y^8 + 40*X^7*Y^9 + 31*X^6*Y^{10} + 20*X^5*Y^{11} + 15*X^4*Y^{12} + 4*X^3*Y^{13} + 3*X^2*Y^{14}$ | |
| 111 | [1 0 0 0 3 0 0 2] [0 1 0 0 2 0 0 2] [0 0 1 0 0 1 0 0] [0 0 0 1 0 0 1 0] | | |
| 112 | [1 0 0 0 2 0 0 0] [0 1 0 0 0 0 0 2] [0 0 1 0 0 1 0 0] [0 0 0 1 0 0 1 0] | $X^{16} + 6*X^{14}*Y^2 + 4*X^{13}*Y^3 + 15*X^{12}*Y^4 + 20*X^{11}*Y^5 + 24*X^{10}*Y^6 + 40*X^9*Y^7 + 31*X^8*Y^8 + 40*X^7*Y^9 + 30*X^6*Y^{10} + 20*X^5*Y^{11} + 17*X^4*Y^{12} + 4*X^3*Y^{13} + 4*X^2*Y^{14}$ | |

| | | | |
|-----|--|---|--|
| 113 | [1 0 0 0 1 3 1 1] [0 1 0 0 1 1 1 0] [0 0 1 0 1 1 3 3] [0 0 0 1 0 1 3 3] | $X^{16} + 4*X^{13}*Y^3 + 9*X^{12}*Y^4 + 16*X^{11}*Y^5 + 16*X^{10}*Y^6 + 40*X^9*Y^7 + 75*X^8*Y^8 + 48*X^7*Y^9 + 16*X^6*Y^{10} + 20*X^5*Y^{11} + 11*X^4*Y^{12}$ | |
| 114 | [1 0 0 0 1 3 1 1] [0 1 0 0 1 1 1 2] [0 0 1 0 1 1 3 3] [0 0 0 1 2 1 3 3] | $X^{16} + 4*X^{13}*Y^3 + 5*X^{12}*Y^4 + 16*X^{11}*Y^5 + 32*X^{10}*Y^6 + 40*X^9*Y^7 + 51*X^8*Y^8 + 48*X^7*Y^9 + 32*X^6*Y^{10} + 20*X^5*Y^{11} + 7*X^4*Y^{12}$ | |
| 115 | [1 0 0 0 1 3 1 1] [0 1 0 0 1 1 1 0] [0 0 1 0 1 1 3 1] [0 0 0 1 0 1 1 0] | | |
| 116 | [1 0 0 0 1 2 0 0] [0 1 0 0 1 1 1 0] [0 0 1 0 1 0 2 1] [0 0 0 1 0 0 1 1] | $X^{16} + 2*X^{13}*Y^3 + 11*X^{12}*Y^4 + 12*X^{11}*Y^5 + 21*X^{10}*Y^6 + 52*X^9*Y^7 + 55*X^8*Y^8 + 48*X^7*Y^9 + 34*X^6*Y^{10} + 10*X^5*Y^{11} + 5*X^4*Y^{12} + 4*X^3*Y^{13} + X^2*Y^{14}$ | |
| 117 | [1 0 0 0 1 2 0 1] [0 1 0 0 1 1 1 0] [0 0 1 0 1 0 2 0] [0 0 0 1 0 1 0 1] | | |
| 118 | [1 0 0 0 1 2 0 0] [0 1 0 0 1 1 1 0] [0 0 1 0 1 0 2 1] [0 0 0 1 0 0 1 3] | $X^{16} + 2*X^{13}*Y^3 + 9*X^{12}*Y^4 + 12*X^{11}*Y^5 + 29*X^{10}*Y^6 + 52*X^9*Y^7 + 43*X^8*Y^8 + 48*X^7*Y^9 + 42*X^6*Y^{10} + 10*X^5*Y^{11} + 3*X^4*Y^{12} + 4*X^3*Y^{13} + X^2*Y^{14}$ | |
| 119 | [1 0 0 0 1 2 0 0] [0 1 0 0 1 1 1 3] [0 0 1 0 1 0 2 2] [0 0 0 1 3 0 2 1] | $X^{16} + 2*X^{13}*Y^3 + 9*X^{12}*Y^4 + 14*X^{11}*Y^5 + 25*X^{10}*Y^6 + 48*X^9*Y^7 + 55*X^8*Y^8 + 48*X^7*Y^9 + 30*X^6*Y^{10} + 14*X^5*Y^{11} + 7*X^4*Y^{12} + 2*X^3*Y^{13} + X^2*Y^{14}$ | |
| 120 | [1 0 0 0 1 2 0 2] [0 1 0 0 1 1 1 1] [0 0 1 0 1 0 2 0] [0 0 0 1 1 2 0 1] | | |

| | | | |
|-----|--|--|--|
| 121 | [1 0 0 0 1 2 0 0] [0 1 0 0 1 1 1 1] [0 0 1 0 1 0 2 0] [0 0 0 1 1 0 0 3] | | |
| 122 | [1 0 0 0 1 2 0 0] [0 1 0 0 1 1 1 1] [0 0 1 0 1 0 2 2] [0 0 0 1 1 0 2 3] | $X^{16} + 2*X^{13}*Y^3 + 7*X^{12}*Y^4 + 14*X^{11}*Y^5 + 33*X^{10}*Y^6 + 48*X^9*Y^7 + 43*X^8*Y^8 + 48*X^7*Y^9 + 38*X^6*Y^10 + 14*X^5*Y^11 + 5*X^4*Y^12 + 2*X^3*Y^13 + X^2*Y^14$ | |
| 123 | [1 0 0 0 1 2 0 1] [0 1 0 0 1 1 1 1] [0 0 1 0 1 0 2 1] [0 0 0 1 1 1 1 2] | | |
| 124 | [1 0 0 0 1 2 0 0] [0 1 0 0 1 1 1 0] [0 0 1 0 1 0 2 1] [0 0 0 1 0 0 1 2] | | |
| 125 | [1 0 0 0 1 2 0 0] [0 1 0 0 1 1 1 2] [0 0 1 0 1 0 2 1] [0 0 0 1 2 0 1 2] | $X^{16} + 10*X^{12}*Y^4 + 14*X^{11}*Y^5 + 26*X^{10}*Y^6 + 52*X^9*Y^7 + 53*X^8*Y^8 + 48*X^7*Y^9 + 28*X^6*Y^10 + 12*X^5*Y^11 + 8*X^4*Y^12 + 2*X^3*Y^13 + 2*X^2*Y^14$ | |
| 126 | [1 0 0 0 1 2 0 2] [0 1 0 0 1 1 1 2] [0 0 1 0 1 0 2 1] [0 0 0 1 2 2 1 2] | | |
| 127 | [1 0 0 0 1 3 1 3] [0 1 0 0 1 1 1 2] [0 0 1 0 1 1 3 2] [0 0 0 1 2 3 2 2] | | |
| 128 | [1 0 0 0 1 2 0 0] [0 1 0 0 1 1 1 0] [0 0 1 0 1 0 2 2] [0 0 0 1 0 0 2 1] | $X^{16} + 16*X^{12}*Y^4 + 48*X^{10}*Y^6 + 126*X^8*Y^8 + 48*X^6*Y^10$ | |
| 129 | [1 0 0 0 1 2 0 2] [0 1 0 0 1 1 1 2] [0 0 1 0 1 0 2 2] [0 0 0 1 2 2 2 1] | $+ 16*X^4*Y^12 + Y^16$ | |

| | | | |
|-----|--|---|--|
| 130 | [1 0 0 0 1 2 0 0] [0 1 0 0 1 1 1 1] [0 0 1 0 1 0 2 0] [0 0 0 1 1 0 0 2] | $X^{16} + 12*X^{12}*Y^4 + 8*X^{11}*Y^5 + 32*X^{10}*Y^6 + 56*X^9*Y^7 + 37*X^8*Y^8 + 56*X^7*Y^9 + 36*X^6*Y^10 + 8*X^5*Y^11 + 6*X^4*Y^12 + 4*X^2*Y^14$ | |
| 131 | [1 0 0 0 1 2 0 1] [0 1 0 0 1 1 1 1] [0 0 1 0 1 0 2 1] [0 0 0 1 1 1 1 3] | | |
| 132 | [1 0 0 0 1 2 0 0] [0 1 0 0 1 1 1 1] [0 0 1 0 1 0 2 1] [0 0 0 1 1 0 1 2] | $X^{16} + 9*X^{12}*Y^4 + 20*X^{11}*Y^5 + 16*X^{10}*Y^6 + 48*X^9*Y^7 + 75*X^8*Y^8 + 40*X^7*Y^9 + 16*X^6*Y^10 + 16*X^5*Y^11 + 11*X^4*Y^12 + 4*X^3*Y^13$ | |
| 133 | [1 0 0 0 1 2 0 1] [0 1 0 0 1 1 1 0] [0 0 1 0 1 0 2 3] [0 0 0 1 0 1 3 3] | | |
| 134 | [1 0 0 0 1 3 1 0] [0 1 0 0 1 1 1 1] [0 0 1 0 1 1 3 2] [0 0 0 1 1 0 2 3] | $X^{16} + 9*X^{12}*Y^4 + 12*X^{11}*Y^5 + 35*X^{10}*Y^6 + 52*X^9*Y^7 + 39*X^8*Y^8 + 52*X^7*Y^9 + 34*X^6*Y^10 + 12*X^5*Y^11 + 7*X^4*Y^12 + 3*X^2*Y^14$ | |
| 135 | [1 0 0 0 1 3 1 0] [0 1 0 0 1 1 1 1] [0 0 1 0 1 1 3 1] [0 0 0 1 1 0 1 2] | $X^{16} + 7*X^{12}*Y^4 + 18*X^{11}*Y^5 + 28*X^{10}*Y^6 + 52*X^9*Y^7 + 51*X^8*Y^8 + 40*X^7*Y^9 + 36*X^6*Y^10 + 12*X^5*Y^11 + 5*X^4*Y^12 + 6*X^3*Y^13$ | |
| 136 | [1 0 0 0 1 3 1 0] [0 1 0 0 1 1 1 2] [0 0 1 0 1 1 3 1] [0 0 0 1 2 0 1 0] | $X^{16} + 8*X^{12}*Y^4 + 14*X^{11}*Y^5 + 34*X^{10}*Y^6 + 52*X^9*Y^7 + 41*X^8*Y^8 + 48*X^7*Y^9 + 36*X^6*Y^10 + 12*X^5*Y^11 + 6*X^4*Y^12 + 2*X^3*Y^13 + 2*X^2*Y^14$ | |
| 137 | [1 0 0 0 1 3 1 1] [0 1 0 0 1 1 1 2] [0 0 1 0 1 1 3 2] [0 0 0 1 2 1 2 0] | | |
| 138 | [1 0 0 0 1 3 1 0] [0 1 0 0 1 1 1 1] [0 0 1 0 1 1 3 2] [0 0 0 1 1 0 2 0] | $X^{16} + 8*X^{12}*Y^4 + 16*X^{11}*Y^5 + 30*X^{10}*Y^6 + 48*X^9*Y^7 + 53*X^8*Y^8 + 48*X^7*Y^9 + 24*X^6*Y^10 + 16*X^5*Y^11 + 10*X^4*Y^12 + 2*X^2*Y^14$ | |
| 139 | [1 0 0 0 1 3 1 0] [0 1 0 0 1 1 1 1] [0 0 1 0 1 1 3 2] [0 0 0 1 1 0 2 1] | $X^{16} + 11*X^{12}*Y^4 + 12*X^{11}*Y^5 + 27*X^{10}*Y^6 + 52*X^9*Y^7 + 51*X^8*Y^8 + 52*X^7*Y^9 + 26*X^6*Y^10 + 12*X^5*Y^11 + 9*X^4*Y^12 + 3*X^2*Y^14$ | |

| | | | |
|-----|--|---|--|
| 140 | [1 0 0 0 1 3 1 0] [0 1 0 0 1 1 1 1] [0 0 1 0 1 1 3 2] [0 0 0 1 1 0 2 2] | $X^{16} + 6*X^{12}*Y^4 + 16*X^{11}*Y^5 + 38*X^{10}*Y^6 + 48*X^9*Y^7 + 41*X^8*Y^8 + 48*X^7*Y^9 + 32*X^6*Y^{10} + 16*X^5*Y^{11} + 8*X^4*Y^{12} + 2*X^2*Y^{14}$ | |
| 141 | [1 0 0 0 1 3 1 0] [0 1 0 0 1 1 1 1] [0 0 1 0 1 1 3 3] [0 0 0 1 1 0 3 1] | | |
| 142 | [1 0 0 0 1 3 1 0] [0 1 0 0 1 1 1 1] [0 0 1 0 1 1 3 3] [0 0 0 1 1 0 3 2] | $X^{16} + 5*X^{12}*Y^4 + 20*X^{11}*Y^5 + 32*X^{10}*Y^6 + 48*X^9*Y^7 + 51*X^8*Y^8 + 40*X^7*Y^9 + 32*X^6*Y^{10} + 16*X^5*Y^{11} + 7*X^4*Y^{12} + 4*X^3*Y^{13}$ | |
| 143 | [1 0 0 0 1 3 1 1] [0 1 0 0 1 1 1 1] [0 0 1 0 1 1 3 2] [0 0 0 1 1 1 2 0] | | |
| 144 | [1 0 0 0 1 3 1 1] [0 1 0 0 1 1 1 1] [0 0 1 0 1 1 3 2] [0 0 0 1 1 1 2 3] | | |
| 145 | [1 0 0 0 1 3 1 0] [0 1 0 0 1 1 1 2] [0 0 1 0 1 1 3 1] [0 0 0 1 2 0 1 1] | $X^{16} + 5*X^{12}*Y^4 + 18*X^{11}*Y^5 + 37*X^{10}*Y^6 + 48*X^9*Y^7 + 43*X^8*Y^8 + 44*X^7*Y^9 + 34*X^6*Y^{10} + 16*X^5*Y^{11} + 7*X^4*Y^{12} + 2*X^3*Y^{13} + X^2*Y^{14}$ | |
| 146 | [1 0 0 0 1 3 1 1] [0 1 0 0 1 1 1 2] [0 0 1 0 1 1 3 2] [0 0 0 1 2 1 2 1] | | |
| 147 | [1 0 0 0 1 3 1 0] [0 1 0 0 1 1 1 2] [0 0 1 0 1 1 3 1] [0 0 0 1 2 0 1 3] | $X^{16} + 7*X^{12}*Y^4 + 18*X^{11}*Y^5 + 29*X^{10}*Y^6 + 48*X^9*Y^7 + 55*X^8*Y^8 + 44*X^7*Y^9 + 26*X^6*Y^{10} + 16*X^5*Y^{11} + 9*X^4*Y^{12} + 2*X^3*Y^{13} + X^2*Y^{14}$ | |
| 148 | [1 0 0 0 1 3 1 1] [0 1 0 0 1 1 1 2] [0 0 1 0 1 1 3 2] [0 0 0 1 2 1 2 3] | | |

| | | |
|-----|--|--|
| 149 | [1 0 0 0 1 3 1 1] [0 1 0 0 1 1 1 3] [0 0 1 0 1 1 3 1] [0 0 0 1 3 1 1 0] | X^16 + 5*X^12*Y^4 + 20*X^11*Y^5 + 33*X^10*Y^6 + 44*X^9*Y^7 + 55*X^8*Y^8 + 44*X^7*Y^9 + 22*X^6*Y^10 + 20*X^5*Y^11 + 11*X^4*Y^12 + X^2*Y^14 |
| 150 | [1 0 0 0 1 3 1 2] [0 1 0 0 1 1 1 1] [0 0 1 0 1 1 3 2] [0 0 0 1 1 2 2 1] | |
| 151 | [1 0 0 0 1 3 1 1] [0 1 0 0 1 1 1 2] [0 0 1 0 1 1 3 1] [0 0 0 1 2 1 1 1] | X^16 + 3*X^12*Y^4 + 16*X^11*Y^5 + 50*X^10*Y^6 + 48*X^9*Y^7 + 23*X^8*Y^8 + 48*X^7*Y^9 + 44*X^6*Y^10 + 16*X^5*Y^11 + 5*X^4*Y^12 + 2*X^2*Y^14 |
| 152 | [1 0 0 0 1 3 1 1] [0 1 0 0 1 1 1 2] [0 0 1 0 1 1 3 1] [0 0 0 1 2 1 1 0] | |
| 153 | [1 0 0 0 1 3 1 1] [0 1 0 0 1 1 1 3] [0 0 1 0 1 1 3 2] [0 0 0 1 3 1 2 2] | X^16 + 3*X^12*Y^4 + 22*X^11*Y^5 + 36*X^10*Y^6 + 44*X^9*Y^7 + 51*X^8*Y^8 + 40*X^7*Y^9 + 28*X^6*Y^10 + 20*X^5*Y^11 + 9*X^4*Y^12 + 2*X^3*Y^13 |
| 154 | [1 0 0 0 1 3 1 2] [0 1 0 0 1 1 1 1] [0 0 1 0 1 1 3 3] [0 0 0 1 1 2 3 2] | |
| 155 | [1 0 0 0 1 3 1 1] [0 1 0 0 1 1 1 1] [0 0 1 0 1 1 3 3] [0 0 0 1 1 1 3 1] | X^16 + 14*X^12*Y^4 + 8*X^11*Y^5 + 24*X^10*Y^6 + 56*X^9*Y^7 + 49*X^8*Y^8 + 56*X^7*Y^9 + 28*X^6*Y^10 + 8*X^5*Y^11 + |
| 156 | [1 0 0 0 1 3 1 2] [0 1 0 0 1 1 1 1] [0 0 1 0 1 1 3 2] [0 0 0 1 1 2 2 0] | 8*X^4*Y^12 + 4*X^2*Y^14 |
| 157 | [1 0 0 0 1 3 1 1] [0 1 0 0 1 1 1 3] [0 0 1 0 1 1 3 2] [0 0 0 1 3 1 2 1] | X^16 + X^12*Y^4 + 20*X^11*Y^5 + 48*X^10*Y^6 + 48*X^9*Y^7 + 27*X^8*Y^8 + 40*X^7*Y^9 + 48*X^6*Y^10 + 16*X^5*Y^11 + 3*X^4*Y^12 + 4*X^3*Y^13 |

| | | | |
|-----|--|---|---|
| 158 | [1 0 0 0 2 1 1 1] [0 1 0 0 1 2 3 0] [0 0 1 0 1 1 2 3] [0 0 0 1 0 1 3 2] | | |
| 159 | [1 0 0 0 2 1 1 1] [0 1 0 0 1 2 3 2] [0 0 1 0 1 1 2 0] [0 0 0 1 2 1 0 3] | $X^{16} + 24*X^{11*Y^5} + 44*X^{10*Y^6} + 40*X^{9*Y^7} + 45*X^{8*Y^8} + 40*X^{7*Y^9} + 28*X^{6*Y^{10}} + 24*X^{5*Y^{11}} + 10*X^{4*Y^{12}}$ | |
| 160 | [1 0 0 0 2 1 1 2] [0 1 0 0 1 2 3 3] [0 0 1 0 1 1 2 0] [0 0 0 1 3 2 0 3] | | |
| 161 | [1 0 0 0 1 2 1 1] [0 1 0 0 1 1 3 2] [0 0 1 0 3 1 2 1] [0 0 0 1 2 1 1 0] | $X^{16} + 20*X^{11*Y^5} + 53*X^{10*Y^6} + 44*X^{9*Y^7} + 25*X^{8*Y^8} + 44*X^{7*Y^9} + 42*X^{6*Y^{10}} + 20*X^{5*Y^{11}} + 6*X^{4*Y^{12}} + X^{2*Y^{14}}$ | |
| 162 | [1 0 0 0 1 2 1 1] [0 1 0 0 1 1 3 2] [0 0 1 0 3 1 2 1] [0 0 0 1 2 1 1 2] | | |
| 163 | [1 0 0 0 1 2 1 1] [0 1 0 0 1 1 3 2] [0 0 1 0 3 1 2 1] [0 0 0 1 2 1 1 3] | $X^{16} + 112*X^{10*Y^6} + 30*X^{8*Y^8} + 112*X^{6*Y^{10}} + Y^{16}$ | 0 |

Table 8. Non-free formally self-dual codes over Z_4 of length 8

| No. | Generator matrix | Lee weight enumerator | Const. |
|-----|-------------------|--|--------|
| 1 | [1 0 0 0 0 1 2 2] | | |
| | [0 1 0 0 0 2 0 0] | | |
| | [0 0 1 0 0 2 0 0] | X^16 + 8*X^14*Y^2 + 8*X^13*Y^3 + 15*X^12*Y^4 + | I-i |
| | [0 0 0 2 0 0 0 0] | 24*X^11*Y^5 + 18*X^10*Y^6 + 32*X^9*Y^7 + 31*X^8*Y^8 + | |
| | [0 0 0 0 2 0 0 0] | 32*X^7*Y^9 + 36*X^6*Y^10 + 24*X^5*Y^11 + 17*X^4*Y^12 + | |
| 2 | [1 0 0 0 0 3 2 2] | 8*X^3*Y^13 + 2*X^2*Y^14 | |
| | [0 1 0 0 0 2 2 2] | | |
| | [0 0 1 0 0 2 2 2] | | I-i |
| | [0 0 0 2 0 0 0 0] | | |
| | [0 0 0 0 2 0 0 0] | | |
| 3 | [1 0 0 0 0 2 0 0] | X^16 + 9*X^14*Y^2 + 4*X^13*Y^3 + 22*X^12*Y^4 + | |
| | [0 1 0 0 0 0 2 2] | 18*X^11*Y^5 + 22*X^10*Y^6 + 40*X^9*Y^7 + 17*X^8*Y^8 + | I- |
| | [0 0 1 0 0 2 0 0] | 44*X^7*Y^9 + 25*X^6*Y^10 + 20*X^5*Y^11 + 24*X^4*Y^12 + | ii,iii |
| | [0 0 0 2 0 0 0 0] | 2*X^3*Y^13 + 8*X^2*Y^14 | |
| | [0 0 0 0 2 0 0 0] | | |
| 4 | [1 0 0 0 0 2 2 2] | | |
| | [0 1 0 0 0 0 2 2] | X^16 + 9*X^14*Y^2 + 30*X^12*Y^4 + 2*X^11*Y^5 + | |
| | [0 0 1 0 0 2 2 2] | 46*X^10*Y^6 + 20*X^9*Y^7 + 33*X^8*Y^8 + 44*X^7*Y^9 + | I- |
| | [0 0 0 2 0 0 0 0] | 9*X^6*Y^10 + 40*X^5*Y^11 + 18*X^3*Y^13 + 4*X*Y^15 | ii,iii |
| | [0 0 0 0 2 0 0 0] | | |
| 5 | [1 0 0 0 0 2 2 2] | X^16 + 9*X^14*Y^2 + 4*X^13*Y^3 + 22*X^12*Y^4 + | |
| | [0 1 0 0 0 2 0 0] | 16*X^11*Y^5 + 30*X^10*Y^6 + 26*X^9*Y^7 + 33*X^8*Y^8 + | |
| | [0 0 1 0 0 2 0 0] | 32*X^7*Y^9 + 25*X^6*Y^10 + 32*X^5*Y^11 + 8*X^4*Y^12 + | I-iv,v |
| | [0 0 0 2 0 0 0 0] | 16*X^3*Y^13 + 2*X*Y^15 | |
| | [0 0 0 0 2 0 0 0] | | |
| 6 | [1 0 0 0 0 2 2 2] | | |
| | [0 1 0 0 0 2 2 2] | X^16 + 17*X^14*Y^2 + 46*X^12*Y^4 + 46*X^10*Y^6 + | |
| | [0 0 1 0 0 2 2 2] | 6*X^9*Y^7 + 17*X^8*Y^8 + 32*X^7*Y^9 + X^6*Y^10 + | I-iv,v |
| | [0 0 0 2 0 0 0 0] | 52*X^5*Y^11 + 32*X^3*Y^13 + 6*X*Y^15 | |
| | [0 0 0 0 2 0 0 0] | | |

| | | | |
|----|---|---|--------------|
| | | | |
| 7 | [1 0 0 0 0 1 2 0] [0 1 0 0 0 2 0 0] [0 0 1 0 0 0 0 1] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | X^16 + 5*X^14*Y^2 + 4*X^13*Y^3 + 13*X^12*Y^4 + 20*X^11*Y^5 + 25*X^10*Y^6 + 40*X^9*Y^7 + 35*X^8*Y^8 + 40*X^7*Y^9 + 31*X^6*Y^10 + 20*X^5*Y^11 + 15*X^4*Y^12 + 4*X^3*Y^13 + 3*X^2*Y^14 | I-i |
| 8 | [1 0 0 0 0 3 2 0] [0 1 0 0 0 2 2 0] [0 0 1 0 0 0 0 1] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | | I-i,II |
| 9 | [1 0 0 0 0 2 0 0] [0 1 0 0 0 0 2 0] [0 0 1 0 0 0 0 1] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | X^16 + 6*X^14*Y^2 + 4*X^13*Y^3 + 15*X^12*Y^4 + 20*X^11*Y^5 + 24*X^10*Y^6 + 40*X^9*Y^7 + 31*X^8*Y^8 + 40*X^7*Y^9 + 30*X^6*Y^10 + 20*X^5*Y^11 + 17*X^4*Y^12 + 4*X^3*Y^13 + 4*X^2*Y^14 | I-ii,II |
| 10 | [1 0 0 0 0 2 2 0] [0 1 0 0 0 0 2 0] [0 0 1 0 0 0 0 1] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | X^16 + 6*X^14*Y^2 + 2*X^13*Y^3 + 19*X^12*Y^4 + 12*X^11*Y^5 + 36*X^10*Y^6 + 30*X^9*Y^7 + 39*X^8*Y^8 + 40*X^7*Y^9 + 22*X^6*Y^10 + 30*X^5*Y^11 + 5*X^4*Y^12 + 12*X^3*Y^13 + 2*X*Y^15 | I-iii, II |
| 11 | [1 0 0 0 0 2 2 0] [0 1 0 0 0 2 2 0] [0 0 1 0 0 0 0 1] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | X^16 + 10*X^14*Y^2 + 31*X^12*Y^4 + 4*X^11*Y^5 + 44*X^10*Y^6 + 20*X^9*Y^7 + 31*X^8*Y^8 + 40*X^7*Y^9 + 10*X^6*Y^10 + 40*X^5*Y^11 + X^4*Y^12 + 20*X^3*Y^13 + 4*X*Y^15 | I-v |
| 12 | [1 0 0 0 0 2 0 0] [0 1 0 0 0 0 2 2] [0 0 1 0 0 0 0 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | X^16 + 5*X^14*Y^2 + 4*X^13*Y^3 + 14*X^12*Y^4 + 18*X^11*Y^5 + 26*X^10*Y^6 + 40*X^9*Y^7 + 33*X^8*Y^8 + 44*X^7*Y^9 + 29*X^6*Y^10 + 20*X^5*Y^11 + 16*X^4*Y^12 + 2*X^3*Y^13 + 4*X^2*Y^14 | I-ii,II |
| 13 | [1 0 0 0 0 2 2 2] [0 1 0 0 0 0 2 2] [0 0 1 0 0 0 0 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | X^16 + 5*X^14*Y^2 + 2*X^13*Y^3 + 18*X^12*Y^4 + 10*X^11*Y^5 + 38*X^10*Y^6 + 30*X^9*Y^7 + 41*X^8*Y^8 + 44*X^7*Y^9 + 21*X^6*Y^10 + 30*X^5*Y^11 + 4*X^4*Y^12 + 10*X^3*Y^13 + 2*X*Y^15 | I-iv,v |
| 14 | [1 0 0 0 0 0 0 0] [0 1 0 0 0 0 1 0] [0 0 1 0 0 0 0 1] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | X^16 + 2*X^15*Y + 7*X^14*Y^2 + 12*X^13*Y^3 + 21*X^12*Y^4 + 30*X^11*Y^5 + 35*X^10*Y^6 + 40*X^9*Y^7 + 35*X^8*Y^8 + 30*X^7*Y^9 + 21*X^6*Y^10 + 12*X^5*Y^11 + 7*X^4*Y^12 + 2*X^3*Y^13 + X^2*Y^14 | II |

| | | | |
|----|---|--|----|
| | | | |
| 15 | [1 0 0 0 0 2 0 0] [0 1 0 0 0 0 1 0] [0 0 1 0 0 0 0 1] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | $X^{16} + 7*X^{14*Y^2} + 2*X^{13*Y^3} + 21*X^{12*Y^4} + 12*X^{11*Y^5} + 35*X^{10*Y^6} + 30*X^9*Y^7 + 35*X^8*Y^8 + 40*X^7*Y^9 + 21*X^6*Y^10 + 30*X^5*Y^11 + 7*X^4*Y^12 + 12*X^3*Y^13 + X^2*Y^14 + 2*X*Y^15$ | II |
| 16 | [1 0 0 0 0 1 0 0] [0 1 0 0 0 0 1 0] [0 0 1 0 0 0 0 1] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | $X^{16} + 8*X^{14*Y^2} + 28*X^{12*Y^4} + 56*X^{10*Y^6} + 70*X^8*Y^8 + 56*X^6*Y^10 + 28*X^4*Y^12 + 8*X^2*Y^14 + Y^16$ | II |
| 17 | [1 0 0 0 0 0 0 0] [0 1 0 0 0 0 1 0] [0 0 1 0 0 0 0 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | $X^{16} + 2*X^{15*Y} + 6*X^{14*Y^2} + 12*X^{13*Y^3} + 19*X^{12*Y^4} + 30*X^{11*Y^5} + 36*X^{10*Y^6} + 40*X^9*Y^7 + 39*X^8*Y^8 + 30*X^7*Y^9 + 22*X^6*Y^10 + 12*X^5*Y^11 + 5*X^4*Y^12 + 2*X^3*Y^13$ | II |
| 18 | [1 0 0 0 0 0 0 0] [0 1 0 0 0 0 2 0] [0 0 1 0 0 0 0 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | $X^{16} + 2*X^{15*Y} + 5*X^{14*Y^2} + 12*X^{13*Y^3} + 18*X^{12*Y^4} + 28*X^{11*Y^5} + 38*X^{10*Y^6} + 40*X^9*Y^7 + 41*X^8*Y^8 + 34*X^7*Y^9 + 21*X^6*Y^10 + 12*X^5*Y^11 + 4*X^4*Y^12$ | II |
| 19 | [1 0 0 0 0 2 0 0] [0 1 0 0 0 0 2 0] [0 0 1 0 0 0 0 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | $X^{16} + 5*X^{14*Y^2} + 6*X^{13*Y^3} + 10*X^{12*Y^4} + 24*X^{11*Y^5} + 22*X^{10*Y^6} + 36*X^9*Y^7 + 41*X^8*Y^8 + 32*X^7*Y^9 + 37*X^6*Y^10 + 22*X^5*Y^11 + 12*X^4*Y^12 + 8*X^3*Y^13$ | II |
| 20 | [1 0 0 0 0 0 0 0] [0 1 0 0 0 0 2 2] [0 0 1 0 0 0 0 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | $X^{16} + 2*X^{15*Y} + 5*X^{14*Y^2} + 10*X^{13*Y^3} + 18*X^{12*Y^4} + 30*X^{11*Y^5} + 38*X^{10*Y^6} + 44*X^9*Y^7 + 41*X^8*Y^8 + 30*X^7*Y^9 + 21*X^6*Y^10 + 10*X^5*Y^11 + 4*X^4*Y^12 + 2*X^3*Y^13$ | II |
| 21 | [1 0 0 0 0 0 0 0] [0 1 0 0 0 0 1 2] [0 0 1 0 0 0 2 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | $X^{16} + 2*X^{15*Y} + 4*X^{14*Y^2} + 10*X^{13*Y^3} + 17*X^{12*Y^4} + 28*X^{11*Y^5} + 40*X^{10*Y^6} + 44*X^9*Y^7 + 43*X^8*Y^8 + 34*X^7*Y^9 + 20*X^6*Y^10 + 10*X^5*Y^11 + 3*X^4*Y^12$ | II |

| | | | |
|----|---|--|-------|
| | [1 0 0 0 0 1 0 2] [0 1 0 0 0 2 2 2] [0 0 1 0 0 0 1 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | X^16 + 3*X^14*Y^2 + 13*X^12*Y^4 + 16*X^11*Y^5 + 31*X^10*Y^6 + 48*X^9*Y^7 + 35*X^8*Y^8 + 48*X^7*Y^9 + 25*X^6*Y^10 + 16*X^5*Y^11 + 15*X^4*Y^12 + 5*X^2*Y^14 | I-i |
| 22 | [1 0 0 0 0 3 0 2] [0 1 0 0 0 2 2 0] [0 0 1 0 0 0 1 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | | |
| 23 | [1 0 0 0 0 2 2 2] [0 1 0 0 0 0 0 2] [0 0 1 0 0 0 1 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | | I-i |
| 24 | [1 0 0 0 0 2 2 2] [0 1 0 0 0 0 0 2] [0 0 1 0 0 0 1 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | X^16 + 4*X^14*Y^2 + 6*X^13*Y^3 + 9*X^12*Y^4 + 22*X^11*Y^5 + 24*X^10*Y^6 + 36*X^9*Y^7 + 43*X^8*Y^8 + 36*X^7*Y^9 + 36*X^6*Y^10 + 22*X^5*Y^11 + 11*X^4*Y^12 + 6*X^3*Y^13 | I-ii |
| 25 | [1 0 0 0 0 2 2 0] [0 1 0 0 0 0 0 2] [0 0 1 0 0 0 1 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | | I-iii |
| 26 | [1 0 0 0 0 2 0 2] [0 1 0 0 0 2 2 2] [0 0 1 0 0 0 1 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | X^16 + 4*X^14*Y^2 + 17*X^12*Y^4 + 10*X^11*Y^5 + 40*X^10*Y^6 + 34*X^9*Y^7 + 43*X^8*Y^8 + 44*X^7*Y^9 + 20*X^6*Y^10 + 28*X^5*Y^11 + 3*X^4*Y^12 + 10*X^3*Y^13 + 2*X*Y^15 | I-iv |
| 27 | [1 0 0 0 0 2 2 0] [0 1 0 0 0 2 0 2] [0 0 1 0 0 0 1 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | | I-v |
| 28 | [1 0 0 0 0 1 2 2] [0 1 0 0 0 2 0 2] [0 0 1 0 0 2 2 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | X^16 + 4*X^14*Y^2 + 4*X^13*Y^3 + 11*X^12*Y^4 + 20*X^11*Y^5 + 26*X^10*Y^6 + 40*X^9*Y^7 + 39*X^8*Y^8 + 40*X^7*Y^9 + 32*X^6*Y^10 + 20*X^5*Y^11 + 13*X^4*Y^12 + 4*X^3*Y^13 + 2*X^2*Y^14 | I-i |
| 29 | [1 0 0 0 0 3 2 2] [0 1 0 0 0 2 2 0] [0 0 1 0 0 2 0 0] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | | I-i |

| | | | |
|----|---|---|-------|
| 30 | [1 0 0 0 0 2 0 2] [0 1 0 0 0 0 2 2] [0 0 1 0 0 2 2 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | $X^{16} + 5*X^{14}*Y^2 + 18*X^{12}*Y^4 + 12*X^{11}*Y^5 + 38*X^{10}*Y^6 + 34*X^9*Y^7 + 41*X^8*Y^8 + 40*X^7*Y^9 + 21*X^6*Y^{10} + 28*X^5*Y^{11} + 4*X^4*Y^{12} + 12*X^3*Y^{13} + 2*X*Y^{15}$ | I-ii |
| 31 | [1 0 0 0 0 2 2 0] [0 1 0 0 0 0 2 2] [0 0 1 0 0 2 0 0] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | $X^{16} + 5*X^{14}*Y^2 + 2*X^{13}*Y^3 + 14*X^{12}*Y^4 + 20*X^{11}*Y^5 + 26*X^{10}*Y^6 + 44*X^9*Y^7 + 33*X^8*Y^8 + 40*X^7*Y^9 + 29*X^6*Y^{10} + 18*X^5*Y^{11} + 16*X^4*Y^{12} + 4*X^3*Y^{13} + 4*X^2*Y^{14}$ | I-iii |
| 32 | [1 0 0 0 0 2 2 2] [0 1 0 0 0 2 0 2] [0 0 1 0 0 2 2 2] [0 0 0 2 0 0 0 0] [0 0 0 0 2 0 0 0] | $X^{16} + 9*X^{14}*Y^2 + 30*X^{12}*Y^4 + 2*X^{11}*Y^5 + 46*X^{10}*Y^6 + 20*X^9*Y^7 + 33*X^8*Y^8 + 44*X^7*Y^9 + 9*X^6*Y^{10} + 40*X^5*Y^{11} + 18*X^3*Y^{13} + 4*X*Y^{15}$ | I-iv |

Table 9. Free formally self-dual codes over Z_4 of length 10

| No. | Generator matrix | Lee weight enumerator | Const. |
|-----|---|--|--------|
| 1 | $[1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 1 \ 2 \ 1 \ 1]$ $[0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1 \ 3 \ 2]$ $[0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 3 \ 1 \ 2 \ 1]$ $[0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 2 \ 1 \ 1 \ 3]$ | $X^{20} + 2*X^{19*Y} + X^{18*Y^2} + 112*X^{14*Y^6} + 224*X^{13*Y^7} + 142*X^{12*Y^8} + 60*X^{11*Y^9} + 142*X^{10*Y^{10}} + 224*X^{9*Y^{11}} + 112*X^{8*Y^{12}} + X^{4*Y^{16}} + 2*X^{3*Y^{17}} + X^{2*Y^{18}}$ | II |
| 2 | $[1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 1 \ 2 \ 0 \ 1]$ $[0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 1 \ 1 \ 1 \ 1]$ $[0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 1 \ 0 \ 2 \ 1]$ $[0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 1 \ 1 \ 1 \ 3]$ | $X^{20} + 2*X^{19*Y} + X^{18*Y^2} + 12*X^{16*Y^4} + 32*X^{15*Y^5} + 60*X^{14*Y^6} + 128*X^{13*Y^7} + 181*X^{12*Y^8} + 186*X^{11*Y^9} + 185*X^{10*Y^{10}} + 136*X^{9*Y^{11}} + 58*X^{8*Y^{12}} + 20*X^{7*Y^{13}} + 10*X^{6*Y^{14}} + 8*X^{5*Y^{15}} + 4*X^{4*Y^{16}}$ | II |
| 3 | $[1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 2 \ 1 \ 1 \ 1]$ $[0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 1 \ 2 \ 3 \ 0]$ $[0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 1 \ 1 \ 2 \ 3]$ $[0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 1 \ 3 \ 2]$ | $X^{20} + 2*X^{19*Y} + X^{18*Y^2} + 24*X^{15*Y^5} + 92*X^{14*Y^6} + 152*X^{13*Y^7} + 169*X^{12*Y^8} + 170*X^{11*Y^9} + 153*X^{10*Y^{10}} + 120*X^{9*Y^{11}} + 86*X^{8*Y^{12}} + 44*X^{7*Y^{13}} + 10*X^{6*Y^{14}}$ | II |
| 4 | $[1 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0]$ $[0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 2 \ 2]$ $[0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 2 \ 2]$ | $X^{20} + 2*X^{19*Y} + 10*X^{18*Y^2} + 20*X^{17*Y^3} + 35*X^{16*Y^4} + 66*X^{15*Y^5} + 84*X^{14*Y^6} + 108*X^{13*Y^7} + 127*X^{12*Y^8} + 118*X^{11*Y^9} + 122*X^{10*Y^{10}} + 108*X^{9*Y^{11}} + 85*X^{8*Y^{12}} + 70*X^{7*Y^{13}} + 40*X^{6*Y^{14}} + 20*X^{5*Y^{15}} + 8*X^{4*Y^{16}}$ | II |
| 5 | $[1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0]$ $[0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 2 \ 2]$ $[0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 2 \ 2]$ | $X^{20} + 4*X^{19*Y} + 13*X^{18*Y^2} + 34*X^{17*Y^3} + 58*X^{16*Y^4} + 84*X^{15*Y^5} + 122*X^{14*Y^6} + 140*X^{13*Y^7} + 125*X^{12*Y^8} + 116*X^{11*Y^9} + 113*X^{10*Y^{10}} + 98*X^{9*Y^{11}} + 72*X^{8*Y^{12}} + 36*X^{7*Y^{13}} + 8*X^{6*Y^{14}}$ | II |
| 6 | $[1 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0]$ $[0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 2 \ 2]$ $[0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 2 \ 2]$ | $X^{20} + 2*X^{19*Y} + 9*X^{18*Y^2} + 20*X^{17*Y^3} + 30*X^{16*Y^4} + 64*X^{15*Y^5} + 90*X^{14*Y^6} + 96*X^{13*Y^7} + 133*X^{12*Y^8} + 138*X^{11*Y^9} + 109*X^{10*Y^{10}} + 108*X^{9*Y^{11}} + 92*X^{8*Y^{12}} + 68*X^{7*Y^{13}} + 48*X^{6*Y^{14}} + 16*X^{5*Y^{15}}$ | II |
| 7 | $[1 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 1 \ 2]$ $[0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 2 \ 0]$ | $X^{20} + 4*X^{19*Y} + 9*X^{18*Y^2} + 20*X^{17*Y^3} + 41*X^{16*Y^4} + 72*X^{15*Y^5} + 113*X^{14*Y^6} + 152*X^{13*Y^7} + 171*X^{12*Y^8} + 164*X^{11*Y^9} + 131*X^{10*Y^{10}} + 84*X^{9*Y^{11}} + 43*X^{8*Y^{12}} + 16*X^{7*Y^{13}} + 3*X^{6*Y^{14}}$ | II |

| | | | |
|----|---|---|----|
| | | | |
| 8 | [1 0 0 0 0 0 0 0 0 0] [0 1 0 0 0 0 0 0 0 0] [0 0 1 0 0 0 0 0 0 0] [0 0 0 1 0 0 0 0 1 2] [0 0 0 0 1 0 0 0 2 0] | $X^{20} + 6*X^{19*Y} + 16*X^{18*Y^2} + 30*X^{17*Y^3} + 57*X^{16*Y^4} + 108*X^{15*Y^5} + 168*X^{14*Y^6} + 204*X^{13*Y^7} + 195*X^{12*Y^8} + 142*X^{11*Y^9} + 72*X^{10*Y^{10}} + 22*X^{9*Y^{11}} + 3*X^{8*Y^{12}}$ | II |
| 9 | [1 0 0 0 0 2 0 0 0 0] [0 1 0 0 0 0 0 0 0 0] [0 0 1 0 0 0 0 0 0 0] [0 0 0 1 0 0 0 0 1 2] [0 0 0 0 1 0 0 0 2 0] | $X^{20} + 4*X^{19*Y} + 8*X^{18*Y^2} + 18*X^{17*Y^3} + 41*X^{16*Y^4} + 70*X^{15*Y^5} + 104*X^{14*Y^6} + 148*X^{13*Y^7} + 179*X^{12*Y^8} + 176*X^{11*Y^9} + 144*X^{10*Y^{10}} + 90*X^{9*Y^{11}} + 35*X^{8*Y^{12}} + 6*X^{7*Y^{13}}$ | II |
| 10 | [1 0 0 0 0 1 0 0 0 0] [0 1 0 0 0 0 0 0 0 0] [0 0 1 0 0 0 0 0 0 0] [0 0 0 1 0 0 0 0 1 3] [0 0 0 0 1 0 0 0 1 1] | $X^{20} + 4*X^{19*Y} + 8*X^{18*Y^2} + 16*X^{17*Y^3} + 35*X^{16*Y^4} + 68*X^{15*Y^5} + 114*X^{14*Y^6} + 160*X^{13*Y^7} + 183*X^{12*Y^8} + 172*X^{11*Y^9} + 132*X^{10*Y^{10}} + 80*X^{9*Y^{11}} + 37*X^{8*Y^{12}} + 12*X^{7*Y^{13}} + 2*X^{6*Y^{14}}$ | II |
| 11 | [1 0 0 0 0 0 0 0 0 0] [0 1 0 0 0 0 0 0 0 0] [0 0 1 0 0 0 0 0 0 0] [0 0 0 1 0 0 0 0 1 3] [0 0 0 0 1 0 0 0 1 1] | $X^{20} + 6*X^{19*Y} + 15*X^{18*Y^2} + 24*X^{17*Y^3} + 44*X^{16*Y^4} + 100*X^{15*Y^5} + 182*X^{14*Y^6} + 232*X^{13*Y^7} + 209*X^{12*Y^8} + 134*X^{11*Y^9} + 59*X^{10*Y^{10}} + 16*X^{9*Y^{11}} + 2*X^{8*Y^{12}}$ | II |
| 12 | [1 0 0 0 0 2 0 0 0 0] [0 1 0 0 0 0 0 0 0 0] [0 0 1 0 0 0 0 0 0 0] [0 0 0 1 0 0 0 0 1 3] [0 0 0 0 1 0 0 0 1 1] | $X^{20} + 4*X^{19*Y} + 7*X^{18*Y^2} + 14*X^{17*Y^3} + 36*X^{16*Y^4} + 68*X^{15*Y^5} + 102*X^{14*Y^6} + 148*X^{13*Y^7} + 193*X^{12*Y^8} + 196*X^{11*Y^9} + 147*X^{10*Y^{10}} + 78*X^{9*Y^{11}} + 26*X^{8*Y^{12}} + 4*X^{7*Y^{13}}$ | II |
| 13 | [1 0 0 0 0 1 0 0 0 0] [0 1 0 0 0 0 2 0 0 0] [0 0 1 0 0 0 0 1 0 0] [0 0 0 1 0 0 0 0 0 0] [0 0 0 0 1 0 0 0 0 0] | $X^{20} + 4*X^{19*Y} + 11*X^{18*Y^2} + 26*X^{17*Y^3} + 49*X^{16*Y^4} + 80*X^{15*Y^5} + 115*X^{14*Y^6} + 142*X^{13*Y^7} + 155*X^{12*Y^8} + 148*X^{11*Y^9} + 121*X^{10*Y^{10}} + 86*X^{9*Y^{11}} + 51*X^{8*Y^{12}} + 24*X^{7*Y^{13}} + 9*X^{6*Y^{14}} + 2*X^{5*Y^{15}}$ | II |
| 14 | [1 0 0 0 0 0 0 0 0 0] [0 1 0 0 0 0 2 0 0 0] [0 0 1 0 0 0 0 1 0 0] [0 0 0 1 0 0 0 0 0 0] [0 0 0 0 1 0 0 0 0 0] | $X^{20} + 6*X^{19*Y} + 18*X^{18*Y^2} + 40*X^{17*Y^3} + 75*X^{16*Y^4} + 118*X^{15*Y^5} + 156*X^{14*Y^6} + 176*X^{13*Y^7} + 167*X^{12*Y^8} + 130*X^{11*Y^9} + 82*X^{10*Y^{10}} + 40*X^{9*Y^{11}} + 13*X^{8*Y^{12}} + 2*X^{7*Y^{13}}$ | II |
| 15 | [1 0 0 0 0 2 0 0 0 0] [0 1 0 0 0 0 2 0 0 0] [0 0 1 0 0 0 0 1 0 0] [0 0 0 1 0 0 0 0 0 0] [0 0 0 0 1 0 0 0 0 0] | $X^{20} + 4*X^{19*Y} + 10*X^{18*Y^2} + 24*X^{17*Y^3} + 47*X^{16*Y^4} + 76*X^{15*Y^5} + 112*X^{14*Y^6} + 144*X^{13*Y^7} + 159*X^{12*Y^8} + 156*X^{11*Y^9} + 130*X^{10*Y^{10}} + 88*X^{9*Y^{11}} + 49*X^{8*Y^{12}} + 20*X^{7*Y^{13}} + 4*X^{6*Y^{14}}$ | II |

| | | | |
|----|-----------------------|--|--------|
| | [1 0 0 0 0 1 0 0 0 0] | $X^{20} + 2*X^{19*Y} + 18*X^{18*Y^2} + 34*X^{17*Y^3} +$ | |
| 16 | [0 1 0 0 0 0 0 0 0 0] | $63*X^{16*Y^4} + 92*X^{15*Y^5} + 92*X^{14*Y^6} + 98*X^{13*Y^7} +$ | |
| | [0 0 1 0 0 0 0 2 2 2] | $75*X^{12*Y^8} + 72*X^{11*Y^9} + 82*X^{10*Y^10} + 86*X^{9*Y^11}$ | II |
| | [0 0 0 1 0 0 0 2 2 2] | $+ 105*X^{8*Y^12} + 84*X^{7*Y^13} + 64*X^{6*Y^14} + 38*X^{5*Y^15}$ | |
| | [0 0 0 0 1 0 0 2 2 2] | $+ 12*X^{4*Y^16} + 6*X^{3*Y^17}$ | |
| | [1 0 0 0 0 0 0 0 0 0] | $X^{20} + 4*X^{19*Y} + 21*X^{18*Y^2} + 64*X^{17*Y^3} +$ | |
| 17 | [0 1 0 0 0 0 0 0 0 0] | $106*X^{16*Y^4} + 120*X^{15*Y^5} + 106*X^{14*Y^6} +$ | |
| | [0 0 1 0 0 0 0 2 2 2] | $70*X^{13*Y^7} + 45*X^{12*Y^8} + 60*X^{11*Y^9} + 105*X^{10*Y^10}$ | II |
| | [0 0 0 1 0 0 0 2 2 2] | $+ 132*X^{9*Y^11} + 104*X^{8*Y^12} + 56*X^{7*Y^13} +$ | |
| | [0 0 0 0 1 0 0 2 2 2] | $24*X^{6*Y^14} + 6*X^{5*Y^15}$ | |
| | [1 0 0 0 0 2 0 0 0 0] | $X^{20} + 2*X^{19*Y} + 17*X^{18*Y^2} + 34*X^{17*Y^3} +$ | |
| 18 | [0 1 0 0 0 0 0 0 0 0] | $50*X^{16*Y^4} + 92*X^{15*Y^5} + 106*X^{14*Y^6} + 98*X^{13*Y^7}$ | |
| | [0 0 1 0 0 0 0 2 2 2] | $+ 89*X^{12*Y^8} + 66*X^{11*Y^9} + 69*X^{10*Y^10} + 78*X^{9*Y^11}$ | II |
| | [0 0 0 1 0 0 0 2 2 2] | $+ 104*X^{8*Y^12} + 112*X^{7*Y^13} + 64*X^{6*Y^14} +$ | |
| | [0 0 0 0 1 0 0 2 2 2] | $30*X^{5*Y^15} + 12*X^{4*Y^16}$ | |
| | [1 0 0 0 0 1 0 0 0 0] | $X^{20} + 2*X^{18*Y^2} + X^{16*Y^4} + 112*X^{14*Y^6} +$ | |
| 19 | [0 1 0 0 0 0 1 2 1 1] | $254*X^{12*Y^8} + 284*X^{10*Y^10} + 254*X^{8*Y^12} +$ | I |
| | [0 0 1 0 0 0 1 1 3 2] | $112*X^{6*Y^14} + X^{4*Y^16} + 2*X^{2*Y^18} + Y^{20}$ | |
| | [0 0 0 1 0 0 3 1 2 1] | | |
| | [0 0 0 0 1 0 2 1 1 3] | | |
| | [1 0 0 0 0 2 0 0 0 0] | $X^{20} + X^{18*Y^2} + 2*X^{17*Y^3} + 112*X^{14*Y^6} +$ | |
| 20 | [0 1 0 0 0 0 1 2 1 1] | $142*X^{12*Y^8} + 224*X^{11*Y^9} + 142*X^{10*Y^10} +$ | |
| | [0 0 1 0 0 0 1 1 3 2] | $60*X^{9*Y^11} + 112*X^{8*Y^12} + 224*X^{7*Y^13} + X^{4*Y^16} +$ | II |
| | [0 0 0 1 0 0 3 1 2 1] | $X^{2*Y^18} + 2*X*Y^{19}$ | |
| | [0 0 0 0 1 0 2 1 1 3] | | |
| | [1 0 0 0 0 2 1 1 3 1] | $X^{20} + X^{18*Y^2} + 8*X^{17*Y^3} + 14*X^{16*Y^4} +$ | |
| 21 | [0 1 0 0 0 0 2 2 2 2] | $16*X^{15*Y^5} + 38*X^{14*Y^6} + 64*X^{13*Y^7} + 89*X^{12*Y^8} +$ | I- |
| | [0 0 1 0 0 2 1 3 1 1] | $162*X^{11*Y^9} + 189*X^{10*Y^10} + 160*X^{9*Y^11} +$ | ii,iii |
| | [0 0 0 1 0 2 1 1 1 1] | $148*X^{8*Y^12} + 92*X^{7*Y^13} + 28*X^{6*Y^14} + 8*X^{5*Y^15} +$ | |
| | [0 0 0 0 1 2 1 1 3 3] | $4*X^{4*Y^16} + 2*X^{3*Y^17}$ | |
| | [1 0 0 0 0 2 3 3 1 3] | $X^{20} + X^{18*Y^2} + 14*X^{16*Y^4} + 8*X^{15*Y^5} +$ | |
| 22 | [0 1 0 0 0 2 2 2 2 2] | $54*X^{14*Y^6} + 24*X^{13*Y^7} + 185*X^{12*Y^8} + 120*X^{11*Y^9}$ | I- |
| | [0 0 1 0 0 2 3 1 3 3] | $+ 189*X^{10*Y^10} + 210*X^{9*Y^11} + 52*X^{8*Y^12} +$ | vi,v |
| | [0 0 0 1 0 2 3 3 3 3] | $112*X^{7*Y^13} + 12*X^{6*Y^14} + 36*X^{5*Y^15} + 4*X^{4*Y^16} +$ | |
| | [0 0 0 0 1 2 3 3 1 1] | $2*X*Y^{19}$ | |
| | [1 0 0 0 0 2 1 1 1 3] | $X^{20} + X^{18*Y^2} + 8*X^{17*Y^3} + 12*X^{16*Y^4} +$ | |
| 23 | [0 1 0 0 0 0 2 2 2 2] | $12*X^{15*Y^5} + 44*X^{14*Y^6} + 80*X^{13*Y^7} + 85*X^{12*Y^8} +$ | I- |
| | [0 0 1 0 0 2 1 2 0 1] | $138*X^{11*Y^9} + 185*X^{10*Y^10} + 176*X^{9*Y^11} +$ | ii,iii |
| | [0 0 0 1 0 2 1 1 1 1] | $154*X^{8*Y^12} + 88*X^{7*Y^13} + 26*X^{6*Y^14} + 8*X^{5*Y^15} +$ | |
| | [0 0 0 0 1 2 1 0 2 1] | $4*X^{4*Y^16} + 2*X^{3*Y^17}$ | |

| | | | |
|----|-----------------------|---|------|
| | [1 0 0 0 0 2 2 2 2 2] | $X^{20} + X^{18*Y^2} + 12*X^{16*Y^4} + 8*X^{15*Y^5} +$ | |
| 24 | [0 1 0 0 0 2 1 1 1 3] | $60*X^{14*Y^6} + 20*X^{13*Y^7} + 181*X^{12*Y^8} + 136*X^{11*Y^9}$ | I- |
| | [0 0 1 0 0 2 1 2 0 1] | $+ 185*X^{10*Y^{10}} + 186*X^{9*Y^{11}} + 58*X^{8*Y^{12}} +$ | vi,v |
| | [0 0 0 1 0 2 1 1 1 1] | $128*X^{7*Y^{13}} + 10*X^{6*Y^{14}} + 32*X^{5*Y^{15}} + 4*X^{4*Y^{16}} +$ | |
| | [0 0 0 0 1 2 1 0 2 1] | $2*X^{*Y^{19}}$ | |
| | [1 0 0 0 0 1 0 0 0 0] | $X^{20} + 2*X^{18*Y^2} + 13*X^{16*Y^4} + 8*X^{15*Y^5} +$ | |
| 25 | [0 1 0 0 0 0 1 2 0 1] | $56*X^{14*Y^6} + 72*X^{13*Y^7} + 113*X^{12*Y^8} + 176*X^{11*Y^9}$ | |
| | [0 0 1 0 0 0 1 1 1 1] | $+ 142*X^{10*Y^{10}} + 176*X^{9*Y^{11}} + 115*X^{8*Y^{12}} +$ | II |
| | [0 0 0 1 0 0 1 0 2 1] | $72*X^{7*Y^{13}} + 52*X^{6*Y^{14}} + 8*X^{5*Y^{15}} + 14*X^{4*Y^{16}} +$ | |
| | [0 0 0 0 1 0 1 1 1 3] | $4*X^{2*Y^{18}}$ | |
| | [1 0 0 0 0 2 0 0 0 0] | $X^{20} + X^{18*Y^2} + 2*X^{17*Y^3} + 12*X^{16*Y^4} + 8*X^{15*Y^5}$ | |
| 26 | [0 1 0 0 0 0 1 2 0 1] | $+ 44*X^{14*Y^6} + 88*X^{13*Y^7} + 85*X^{12*Y^8} +$ | |
| | [0 0 1 0 0 0 1 1 1 1] | $176*X^{11*Y^9} + 185*X^{10*Y^{10}} + 138*X^{9*Y^{11}} +$ | II |
| | [0 0 0 1 0 0 1 0 2 1] | $154*X^{8*Y^{12}} + 80*X^{7*Y^{13}} + 26*X^{6*Y^{14}} + 12*X^{5*Y^{15}}$ | |
| | [0 0 0 0 1 0 1 1 1 3] | $+ 4*X^{4*Y^{16}} + 8*X^{3*Y^{17}}$ | |
| | [1 0 0 0 0 1 0 0 0 0] | $X^{20} + 2*X^{18*Y^2} + X^{16*Y^4} + 112*X^{14*Y^6} +$ | |
| 27 | [0 1 0 0 0 0 1 2 1 1] | $254*X^{12*Y^8} + 284*X^{10*Y^{10}} + 254*X^{8*Y^{12}} +$ | |
| | [0 0 1 0 0 0 1 1 3 2] | $112*X^{6*Y^{14}} + X^{4*Y^{16}} + 2*X^{2*Y^{18}} + Y^{20}$ | II |
| | [0 0 0 1 0 0 3 1 2 1] | | |
| | [0 0 0 0 1 0 2 1 1 3] | | |
| | [1 0 0 0 0 2 0 0 0 0] | $X^{20} + X^{18*Y^2} + 2*X^{17*Y^3} + 112*X^{14*Y^6} +$ | |
| 28 | [0 1 0 0 0 0 1 2 1 1] | $142*X^{12*Y^8} + 224*X^{11*Y^9} + 142*X^{10*Y^{10}} +$ | |
| | [0 0 1 0 0 0 1 1 3 2] | $60*X^{9*Y^{11}} + 112*X^{8*Y^{12}} + 224*X^{7*Y^{13}} + X^{4*Y^{16}} +$ | II |
| | [0 0 0 1 0 0 3 1 2 1] | $X^{2*Y^{18}} + 2*X^{*Y^{19}}$ | |
| | [0 0 0 0 1 0 2 1 1 3] | | |
| | [1 0 0 0 0 1 0 0 0 0] | $X^{20} + 2*X^{18*Y^2} + X^{16*Y^4} + 24*X^{15*Y^5} +$ | |
| 29 | [0 1 0 0 0 0 2 1 1 1] | $44*X^{14*Y^6} + 88*X^{13*Y^7} + 133*X^{12*Y^8} + 144*X^{11*Y^9}$ | |
| | [0 0 1 0 0 0 1 2 3 0] | $+ 162*X^{10*Y^{10}} + 144*X^{9*Y^{11}} + 111*X^{8*Y^{12}} +$ | II |
| | [0 0 0 1 0 0 1 1 2 3] | $88*X^{7*Y^{13}} + 48*X^{6*Y^{14}} + 24*X^{5*Y^{15}} + 10*X^{4*Y^{16}}$ | |
| | [0 0 0 0 1 0 0 1 3 2] | | |
| | [1 0 0 0 0 2 0 0 0 0] | $X^{20} + X^{18*Y^2} + 2*X^{17*Y^3} + 24*X^{15*Y^5} +$ | |
| 30 | [0 1 0 0 0 0 2 1 1 1] | $44*X^{14*Y^6} + 64*X^{13*Y^7} + 137*X^{12*Y^8} + 168*X^{11*Y^9}$ | |
| | [0 0 1 0 0 0 1 2 3 0] | $+ 153*X^{10*Y^{10}} + 154*X^{9*Y^{11}} + 118*X^{8*Y^{12}} +$ | II |
| | [0 0 0 1 0 0 1 1 2 3] | $80*X^{7*Y^{13}} + 58*X^{6*Y^{14}} + 20*X^{5*Y^{15}}$ | |
| | [0 0 0 0 1 0 0 1 3 2] | | |
| | [1 0 0 0 0 2 2 1 1 2] | $X^{20} + X^{18*Y^2} + 2*X^{17*Y^3} + 12*X^{15*Y^5} +$ | |
| 31 | [0 1 0 0 0 0 0 0 0 2] | $53*X^{14*Y^6} + 104*X^{13*Y^7} + 118*X^{12*Y^8} + 114*X^{11*Y^9}$ | |
| | [0 0 1 0 0 0 1 2 1 1] | $+ 155*X^{10*Y^{10}} + 194*X^{9*Y^{11}} + 136*X^{8*Y^{12}} +$ | II |
| | [0 0 0 1 0 0 1 1 3 2] | $64*X^{7*Y^{13}} + 47*X^{6*Y^{14}} + 20*X^{5*Y^{15}} + X^{4*Y^{16}} +$ | |
| | [0 0 0 0 1 0 3 1 2 1] | $2*X^{3*Y^{17}}$ | |

| | | | |
|----|-----------------------|--|-------|
| | [1 0 0 0 0 2 0 0 0 2] | $X^{20} + X^{18}Y^2 + 2X^{15}Y^5 + 93X^{14}Y^6 +$ | |
| | [0 1 0 0 0 2 2 1 1 2] | $32X^{13}Y^7 + 166X^{12}Y^8 + 148X^{11}Y^9 +$ | |
| 32 | [0 0 1 0 0 0 1 2 1 1] | $155X^{10}Y^{10} + 138X^9Y^{11} + 88X^8Y^{12} +$ | II |
| | [0 0 0 1 0 0 1 1 3 2] | $170X^7Y^{13} + 7X^6Y^{14} + 20X^5Y^{15} + X^4Y^{16} +$ | |
| | [0 0 0 0 1 0 3 1 2 1] | $2XY^{19}$ | |
| | [1 0 0 0 0 1 2 2 2 2] | | |
| | [0 1 0 0 0 2 0 0 1 1] | | |
| 33 | [0 0 1 0 0 2 0 0 0 0] | $X^{20} + 6X^{18}Y^2 + 8X^{17}Y^3 + 23X^{16}Y^4 +$ | I-i |
| | [0 0 0 1 0 2 0 0 0 0] | $16X^{15}Y^5 + 70X^{14}Y^6 + 96X^{13}Y^7 + 59X^{12}Y^8 +$ | |
| | [0 0 0 0 1 2 0 0 1 3] | $136X^{11}Y^9 + 132X^{10}Y^{10} + 136X^9Y^{11} +$ | |
| | [1 0 0 0 0 3 2 2 2 2] | $161X^8Y^{12} + 96X^7Y^{13} + 46X^6Y^{14} + 16X^5Y^{15} +$ | |
| 34 | [0 1 0 0 0 2 2 2 3 3] | $12X^4Y^{16} + 8X^3Y^{17} + 2X^2Y^{18}$ | I-i |
| | [0 0 1 0 0 2 2 2 2 2] | | |
| | [0 0 0 1 0 2 2 2 2 2] | | |
| | [0 0 0 0 1 2 2 2 3 1] | | |
| | [1 0 0 0 0 2 0 0 1 1] | $X^{20} + 7X^{18}Y^2 + 4X^{17}Y^3 + 28X^{16}Y^4 +$ | |
| | [0 1 0 0 0 0 2 2 2 2] | $12X^{15}Y^5 + 86X^{14}Y^6 + 60X^{13}Y^7 + 97X^{12}Y^8 +$ | |
| 35 | [0 0 1 0 0 2 0 0 0 0] | $170X^{11}Y^9 + 59X^{10}Y^{10} + 196X^9Y^{11} +$ | I-ii |
| | [0 0 0 1 0 2 0 0 0 0] | $114X^8Y^{12} + 56X^7Y^{13} + 96X^6Y^{14} + 12X^5Y^{15} +$ | |
| | [0 0 0 0 1 2 0 0 1 3] | $16X^4Y^{16} + 2X^3Y^{17} + 8X^2Y^{18}$ | |
| | [1 0 0 0 0 2 2 2 3 3] | | |
| | [0 1 0 0 0 0 2 2 2 2] | $X^{20} + 7X^{18}Y^2 + 36X^{16}Y^4 + 102X^{14}Y^6 +$ | |
| 36 | [0 0 1 0 0 2 2 2 2 2] | $4X^{13}Y^7 + 193X^{12}Y^8 + 78X^{11}Y^9 + 147X^{10}Y^{10} +$ | I-iii |
| | [0 0 0 1 0 2 2 2 2 2] | $196X^9Y^{11} + 26X^8Y^{12} + 148X^7Y^{13} +$ | |
| | [0 0 0 0 1 2 2 2 3 1] | $68X^5Y^{15} + 14X^3Y^{17} + 4XY^{19}$ | |
| | [1 0 0 0 0 2 2 2 2 2] | | |
| | [0 1 0 0 0 2 0 0 1 1] | $X^{20} + 7X^{18}Y^2 + 4X^{17}Y^3 + 28X^{16}Y^4 +$ | |
| 37 | [0 0 1 0 0 2 0 0 0 0] | $12X^{15}Y^5 + 86X^{14}Y^6 + 56X^{13}Y^7 + 121X^{12}Y^8 +$ | I-iv |
| | [0 0 0 1 0 2 0 0 0 0] | $+ 108X^{11}Y^9 + 147X^{10}Y^{10} + 134X^9Y^{11} +$ | |
| | [0 0 0 0 1 2 0 0 1 3] | $98X^8Y^{12} + 140X^7Y^{13} + 16X^6Y^{14} + 44X^5Y^{15} + 8X^4Y^{16} + 12X^3Y^{17} + 2XY^{19}$ | |
| | [1 0 0 0 0 2 2 2 3 3] | | |
| | [0 1 0 0 0 2 2 2 2 2] | $X^{20} + 15X^{18}Y^2 + 44X^{16}Y^4 + 182X^{14}Y^6 +$ | |
| 38 | [0 0 1 0 0 2 2 2 2 2] | $209X^{12}Y^8 + 16X^{11}Y^9 + 59X^{10}Y^{10} +$ | I-v |
| | [0 0 0 1 0 2 2 2 2 2] | $134X^9Y^{11} + 2X^8Y^{12} + 232X^7Y^{13} + 100X^5Y^{15} + 24X^3Y^{17} + 6XY^{19}$ | |
| | [0 0 0 0 1 2 2 2 3 1] | | |
| | [1 0 0 0 0 1 0 0 2 2] | $X^{20} + 8X^{18}Y^2 + 20X^{16}Y^4 + 32X^{15}Y^5 +$ | |
| | [0 1 0 0 0 2 2 0 0 0] | $60X^{14}Y^6 + 96X^{13}Y^7 + 118X^{12}Y^8 + 128X^{11}Y^9 +$ | |
| 39 | [0 0 1 0 0 0 1 0 2 2] | $+ 116X^{10}Y^{10} + 128X^9Y^{11} + 84X^8Y^{12} +$ | I-i |
| | [0 0 0 1 0 2 2 0 0 0] | $96X^7Y^{13} + 68X^6Y^{14} + 32X^5Y^{15} + 33X^4Y^{16} + 4XY^{18}$ | |
| | [0 0 0 0 1 0 0 1 0 0] | | |

| | | | |
|----|-----------------------|---|--------|
| | [1 0 0 0 0 2 2 0 0 0] | $X^{20} + 9*X^{18*Y^2} + 4*X^{17*Y^3} + 23*X^{16*Y^4} +$ | |
| 40 | [0 1 0 0 0 0 0 0 2 2] | $42*X^{15*Y^5} + 49*X^{14*Y^6} + 104*X^{13*Y^7} + 97*X^{12*Y^8}$ | I- |
| | [0 0 1 0 0 0 1 0 2 2] | $+ 118*X^{11*Y^9} + 131*X^{10*Y^{10}} + 100*X^{9*Y^{11}} +$ | ii,iii |
| | [0 0 0 1 0 2 2 0 0 0] | $117*X^{8*Y^{12}} + 86*X^{7*Y^{13}} + 67*X^{6*Y^{14}} + 48*X^{5*Y^{15}}$ | |
| | [0 0 0 0 1 0 0 1 0 0] | $+ 18*X^{4*Y^{16}} + 10*X^{3*Y^{17}}$ | |
| | [1 0 0 0 0 2 0 0 2 2] | $X^{20} + 9*X^{18*Y^2} + 39*X^{16*Y^4} + 12*X^{15*Y^5} +$ | |
| 41 | [0 1 0 0 0 2 2 0 0 0] | $81*X^{14*Y^6} + 66*X^{13*Y^7} + 113*X^{12*Y^8} + 128*X^{11*Y^9}$ | I- |
| | [0 0 1 0 0 0 1 0 2 2] | $+ 131*X^{10*Y^{10}} + 126*X^{9*Y^{11}} + 101*X^{8*Y^{12}} +$ | iv,v |
| | [0 0 0 1 0 2 2 0 0 0] | $92*X^{7*Y^{13}} + 35*X^{6*Y^{14}} + 62*X^{5*Y^{15}} + 2*X^{4*Y^{16}} +$ | |
| | [0 0 0 0 1 0 0 1 0 0] | $24*X^{3*Y^{17}} + 2*X*Y^{19}$ | |
| | [0 0 0 0 1 2 0 2 2] | $X^{20} + 9*X^{18*Y^2} + 39*X^{16*Y^4} + 12*X^{15*Y^5} +$ | |
| 42 | [0 1 0 0 0 2 2 0 0 0] | $79*X^{14*Y^6} + 76*X^{13*Y^7} + 89*X^{12*Y^8} + 168*X^{11*Y^9}$ | |
| | [0 0 1 0 0 2 2 0 0 0] | $+ 81*X^{10*Y^{10}} + 168*X^{9*Y^{11}} + 85*X^{8*Y^{12}} +$ | I-i |
| | [0 0 0 1 0 2 0 0 2 2] | $76*X^{7*Y^{13}} + 77*X^{6*Y^{14}} + 12*X^{5*Y^{15}} + 42*X^{4*Y^{16}} +$ | |
| | [0 0 0 0 1 0 0 1 0 0] | $10*X^{2*Y^{18}}$ | |
| | [1 0 0 0 0 2 2 0 0 0] | $X^{20} + 10*X^{18*Y^2} + 16*X^{17*Y^3} + 31*X^{16*Y^4} +$ | |
| 43 | [0 1 0 0 0 0 2 0 2 2] | $52*X^{15*Y^5} + 48*X^{14*Y^6} + 72*X^{13*Y^7} + 79*X^{12*Y^8} +$ | |
| | [0 0 1 0 0 2 2 0 0 0] | $92*X^{11*Y^9} + 130*X^{10*Y^{10}} + 128*X^{9*Y^{11}} +$ | I-ii |
| | [0 0 0 1 0 2 0 0 2 2] | $129*X^{8*Y^{12}} + 108*X^{7*Y^{13}} + 68*X^{6*Y^{14}} + 40*X^{5*Y^{15}}$ | |
| | [0 0 0 0 1 0 0 1 0 0] | $+ 16*X^{4*Y^{16}} + 4*X^{3*Y^{17}}$ | |
| | [1 0 0 0 0 2 0 0 2 2] | $X^{20} + 10*X^{18*Y^2} + 16*X^{17*Y^3} + 31*X^{16*Y^4} +$ | |
| 44 | [0 1 0 0 0 0 2 0 2 2] | $50*X^{15*Y^5} + 52*X^{14*Y^6} + 72*X^{13*Y^7} + 75*X^{12*Y^8} +$ | |
| | [0 0 1 0 0 2 0 0 2 2] | $98*X^{11*Y^9} + 122*X^{10*Y^{10}} + 128*X^{9*Y^{11}} + 37*X^{8*Y^{12}}$ | I-iii |
| | [0 0 0 1 0 2 2 0 0 0] | $+ 102*X^{7*Y^{13}} + 72*X^{6*Y^{14}} + 40*X^{5*Y^{15}} +$ | |
| | [0 0 0 0 1 0 0 1 0 0] | $12*X^{4*Y^{16}} + 6*X^{3*Y^{17}}$ | |
| | [1 0 0 0 0 2 2 0 2 2] | $X^{20} + 10*X^{18*Y^2} + 35*X^{16*Y^4} + 20*X^{15*Y^5} +$ | |
| 45 | [0 1 0 0 0 2 2 0 0 0] | $84*X^{14*Y^6} + 70*X^{13*Y^7} + 127*X^{12*Y^8} + 108*X^{11*Y^9}$ | |
| | [0 0 1 0 0 2 2 0 0 0] | $+ 122*X^{10*Y^{10}} + 118*X^{9*Y^{11}} + 85*X^{8*Y^{12}} +$ | I-iv |
| | [0 0 0 1 0 2 0 0 2 2] | $108*X^{7*Y^{13}} + 40*X^{6*Y^{14}} + 66*X^{5*Y^{15}} + 8*X^{4*Y^{16}} +$ | |
| | [0 0 0 0 1 0 0 1 0 0] | $20*X^{3*Y^{17}} + 2*X*Y^{19}$ | |
| | [1 0 0 0 0 2 0 0 2 2] | $X^{20} + 10*X^{18*Y^2} + 39*X^{16*Y^4} + 18*X^{15*Y^5} +$ | |
| 46 | [0 1 0 0 0 2 2 0 2 2] | $80*X^{14*Y^6} + 70*X^{13*Y^7} + 119*X^{12*Y^8} + 114*X^{11*Y^9}$ | |
| | [0 0 1 0 0 2 0 0 2 2] | $+ 130*X^{10*Y^{10}} + 118*X^{9*Y^{11}} + 89*X^{8*Y^{12}}$ | I-v |
| | [0 0 0 1 0 2 2 0 0 0] | $102*X^{7*Y^{13}} + 36*X^{6*Y^{14}} + 66*X^{5*Y^{15}} + 8*X^{4*Y^{16}} +$ | |
| | [0 0 0 0 1 0 0 1 0 0] | $22*X^{3*Y^{17}} + 2*X*Y^{19}$ | |
| | [1 0 0 0 0 1 2 0 2 2] | $X^{20} + 9*X^{18*Y^2} + 8*X^{17*Y^3} + 31*X^{16*Y^4} +$ | |
| 47 | [0 1 0 0 0 2 2 0 2 2] | $36*X^{15*Y^5} + 55*X^{14*Y^6} + 84*X^{13*Y^7} + 81*X^{12*Y^8} +$ | |
| | [0 0 1 0 0 2 2 0 2 2] | $128*X^{11*Y^9} + 121*X^{10*Y^{10}} + 128*X^{9*Y^{11}} +$ | I-i |
| | [0 0 0 1 0 2 0 0 2 2] | $125*X^{8*Y^{12}} + 84*X^{7*Y^{13}} + 69*X^{6*Y^{14}} + 36*X^{5*Y^{15}}$ | |
| | [0 0 0 0 1 0 0 1 0 0] | $+ 18*X^{4*Y^{16}} + 8*X^{3*Y^{17}} + 2*X^{2*Y^{18}}$ | |

| | | | |
|----|-----------------------|--|-------|
| | [1 0 0 0 0 2 2 0 2 2] | $X^{20} + 10*X^{18}*Y^2 + 47*X^{16}*Y^4 + 112*X^{14}*Y^6 +$ | |
| 48 | [0 1 0 0 0 0 2 0 2 2] | $20*X^{13}*Y^7 + 159*X^{12}*Y^8 + 88*X^{11}*Y^9 +$ | |
| | [0 0 1 0 0 2 2 0 2 2] | $130*X^{10}*Y^{10} + 156*X^9*Y^{11} + 49*X^8*Y^{12} +$ | I-ii |
| | [0 0 0 1 0 2 0 0 2 2] | $144*X^7*Y^{13} + 4*X^6*Y^{14} + 76*X^5*Y^{15} + 24*X^3*Y^{17} +$ | |
| | [0 0 0 0 1 0 0 1 0 0] | $4*X*Y^{19}$ | |
| 49 | [1 0 0 0 0 2 0 0 0 0] | $X^{20} + 10*X^{18}*Y^2 + 4*X^{17}*Y^3 + 39*X^{16}*Y^4 +$ | |
| | [0 1 0 0 0 0 2 0 2 2] | $22*X^{15}*Y^5 + 76*X^{14}*Y^6 + 76*X^{13}*Y^7 + 83*X^{12}*Y^8 +$ | |
| 49 | [0 0 1 0 0 2 0 0 0 0] | $150*X^{11}*Y^9 + 82*X^{10}*Y^{10} + 156*X^9*Y^{11} +$ | I-iii |
| | [0 0 0 1 0 2 2 0 0 0] | $97*X^8*Y^{12} + 82*X^7*Y^{13} + 80*X^6*Y^{14} + 20*X^5*Y^{15} +$ | |
| | [0 0 0 0 1 0 0 1 0 0] | $36*X^4*Y^{16} + 2*X^3*Y^{17} + 8*X^2*Y^{18}$ | |
| 50 | [1 0 0 0 0 2 2 0 2 2] | $X^{20} + 18*X^{18}*Y^2 + 75*X^{16}*Y^4 + 156*X^{14}*Y^6 +$ | |
| | [0 1 0 0 0 2 2 0 2 2] | $2*X^{13}*Y^7 + 167*X^{12}*Y^8 + 40*X^{11}*Y^9 + 82*X^{10}*Y^{10} +$ | |
| 50 | [0 0 1 0 0 2 2 0 2 2] | $130*X^9*Y^{11} + 13*X^8*Y^{12} + 176*X^7*Y^{13} +$ | I-iv |
| | [0 0 0 1 0 2 0 0 2 2] | $118*X^5*Y^{15} + 40*X^3*Y^{17} + 6*X*Y^{19}$ | |
| 51 | [1 0 0 0 0 2 0 0 0 0] | $X^{20} + 10*X^{18}*Y^2 + 4*X^{17}*Y^3 + 39*X^{16}*Y^4 +$ | |
| | [0 1 0 0 0 2 2 0 2 2] | $22*X^{15}*Y^5 + 80*X^{14}*Y^6 + 58*X^{13}*Y^7 + 119*X^{12}*Y^8 +$ | |
| 51 | [0 0 1 0 0 2 0 0 0 0] | $102*X^{11}*Y^9 + 130*X^{10}*Y^{10} + 130*X^9*Y^{11} +$ | I-v |
| | [0 0 0 1 0 2 2 0 0 0] | $89*X^8*Y^{12} + 114*X^7*Y^{13} + 36*X^6*Y^{14} + 62*X^5*Y^{15} +$ | |
| | [0 0 0 0 1 0 0 1 0 0] | $8*X^4*Y^{16} + 18*X^3*Y^{17} + 2*X*Y^{19}$ | |
| 52 | [1 0 0 0 0 1 2 2 2 2] | | |
| | [0 1 0 0 0 2 0 2 2 2] | | |
| 52 | [0 0 1 0 0 2 0 0 0 0] | $X^{20} + 16*X^{18}*Y^2 + 4*X^{17}*Y^3 + 31*X^{16}*Y^4 +$ | I-i |
| | [0 0 0 1 0 2 0 2 2 2] | $72*X^{15}*Y^5 + 56*X^{14}*Y^6 + 112*X^{13}*Y^7 + 123*X^{12}*Y^8 +$ | |
| | [0 0 0 0 1 2 0 2 2 2] | $68*X^{11}*Y^9 + 82*X^{10}*Y^{10} + 68*X^9*Y^{11} +$ | |
| 53 | [1 0 0 0 0 3 2 2 2 2] | $57*X^8*Y^{12} + 112*X^7*Y^{13} + 100*X^6*Y^{14} + 72*X^5*Y^{15} +$ | |
| | [0 1 0 0 0 2 2 0 0 0] | $44*X^4*Y^{16} + 4*X^3*Y^{17} + 2*X^2*Y^{18}$ | I-i |
| 53 | [0 0 1 0 0 2 2 2 2 2] | | |
| | [0 0 0 1 0 2 2 0 0 0] | | |
| | [0 0 0 0 1 2 2 0 0 0] | | |
| 54 | [1 0 0 0 0 2 0 2 2 2] | $X^{20} + 17*X^{18}*Y^2 + 2*X^{17}*Y^3 + 46*X^{16}*Y^4 +$ | |
| | [0 1 0 0 0 0 2 2 2 2] | $56*X^{15}*Y^5 + 58*X^{14}*Y^6 + 140*X^{13}*Y^7 + 81*X^{12}*Y^8 +$ | |
| 54 | [0 0 1 0 0 2 0 0 0 0] | $64*X^{11}*Y^9 + 105*X^{10}*Y^{10} + 66*X^9*Y^{11} +$ | I-ii |
| | [0 0 0 1 0 2 0 2 2 2] | $68*X^8*Y^{12} + 112*X^7*Y^{13} + 72*X^6*Y^{14} + 64*X^5*Y^{15} +$ | |
| | [0 0 0 0 1 2 0 2 2 2] | $60*X^4*Y^{16} + 8*X^3*Y^{17} + 4*X^2*Y^{18},$ | |
| 55 | [1 0 0 0 0 2 2 0 0 0] | $X^{20} + 17*X^{18}*Y^2 + 50*X^{16}*Y^4 + 30*X^{15}*Y^5 +$ | |
| | [0 1 0 0 0 0 2 2 2 2] | $106*X^{14}*Y^6 + 112*X^{13}*Y^7 + 89*X^{12}*Y^8 + 78*X^{11}*Y^9 +$ | |
| 55 | [0 0 1 0 0 2 2 2 2 2] | $69*X^{10}*Y^{10} + 66*X^9*Y^{11} + 104*X^8*Y^{12} +$ | I-iii |
| | [0 0 0 1 0 2 2 0 0 0] | $98*X^7*Y^{13} + 64*X^6*Y^{14} + 92*X^5*Y^{15} + 12*X^4*Y^{16} +$ | |
| | [0 0 0 0 1 2 2 0 0 0] | $34*X^3*Y^{17} + 2*X*Y^{19}$ | |

| | | | |
|----|-------------------------|--|-------|
| | [1 0 0 0 0 2 2 2 2 2] | $X^{20} + 17*X^{18}*Y^2 + 2*X^{17}*Y^3 + 58*X^{16}*Y^4 +$ | |
| | [0 1 0 0 0 2 0 2 2 2] | $32*X^{15}*Y^5 + 98*X^{14}*Y^6 + 84*X^{13}*Y^7 + 81*X^{12}*Y^8 +$ | |
| 56 | [0 0 1 0 0 2 0 0 0 0] | $118*X^{11}*Y^9 + 69*X^{10}*Y^{10} + 60*X^9*Y^{11} +$ | I-iv |
| | [0 0 0 1 0 2 0 2 2 2] | $112*X^8*Y^{12} + 84*X^7*Y^{13} + 72*X^6*Y^{14} + 92*X^5*Y^{15}$ | |
| | [0 0 0 0 1 2 0 2 2 2] | $+ 4*X^4*Y^{16} + 38*X^3*Y^{17} + 2*X*Y^{19},$ | |
| | [1 0 0 0 0 2 2 0 0 0] | $X^{20} + 21*X^{18}*Y^2 + 106*X^{16}*Y^4 + 6*X^{15}*Y^5 +$ | |
| 57 | [0 1 0 0 0 2 2 2 2 2] | $106*X^{14}*Y^6 + 56*X^{13}*Y^7 + 45*X^{12}*Y^8 + 132*X^{11}*Y^9$ | |
| | [0 0 1 0 0 2 2 2 2 2] | $+ 105*X^{10}*Y^{10} + 60*X^9*Y^{11} + 104*X^8*Y^{12} +$ | I-v |
| | [0 0 0 1 0 2 2 0 0 0] | $70*X^7*Y^{13} + 24*X^6*Y^{14} + 120*X^5*Y^{15} + 64*X^3*Y^{17}$ | |
| | [0 0 0 0 1 2 2 0 0 0] | $+ 4*X*Y^{19}$ | |
| | [1 0 0 0 0 1 2 2 2 2] | | |
| | [0 1 0 0 0 2 0 0 1 1] | | |
| 58 | [0 0 1 0 0 2 2 0 0 0] | $X^{20} + 4*X^{18}*Y^2 + 4*X^{17}*Y^3 + 19*X^{16}*Y^4 +$ | I-i |
| | [0 0 0 1 0 2 0 0 0 0] | $24*X^{15}*Y^5 + 44*X^{14}*Y^6 + 64*X^{13}*Y^7 + 111*X^{12}*Y^8$ | |
| | [0 0 0 0 1 2 0 0 1 1] | $+ 164*X^{11}*Y^9 + 142*X^{10}*Y^{10} + 164*X^9*Y^{11} +$ | |
| | [1 0 0 0 0 3 2 2 2 2] | $117*X^8*Y^{12} + 64*X^7*Y^{13} + 64*X^6*Y^{14} + 24*X^5*Y^{15}$ | |
| 59 | [0 1 0 0 0 2 2 2 3 3] | $+ 8*X^4*Y^{16} + 4*X^3*Y^{17} + 2*X^2*Y^{18}$ | I-i |
| | [0 0 1 0 0 2 0 2 2 2] | | |
| | [0 0 0 1 0 2 2 2 2 2] | | |
| | [0 0 0 0 1 2 2 2 3 3] | | |
| | [1 0 0 0 0 2 0 0 1 1] | $X^{20} + 5*X^{18}*Y^2 + 2*X^{17}*Y^3 + 22*X^{16}*Y^4 +$ | |
| 60 | [0 1 0 0 0 0 2 2 2 2] | $14*X^{15}*Y^5 + 58*X^{14}*Y^6 + 92*X^{13}*Y^7 + 93*X^{12}*Y^8 +$ | |
| | [0 0 1 0 0 2 2 0 0 0] | $142*X^{11}*Y^9 + 141*X^{10}*Y^{10} + 162*X^9*Y^{11} +$ | I-ii |
| | [0 0 0 1 0 2 0 0 0 0] | $116*X^8*Y^{12} + 82*X^7*Y^{13} + 48*X^6*Y^{14} + 16*X^5*Y^{15}$ | |
| | [0 0 0 0 1 2 0 0 1 1] | $+ 24*X^4*Y^{16} + 2*X^3*Y^{17} + 4*X^2*Y^{18}$ | |
| | [1 0 0 0 0 0 2 2 2 3 3] | $X^{20} + 5*X^{18}*Y^2 + 26*X^{16}*Y^4 + 82*X^{14}*Y^6 +$ | |
| | [0 1 0 0 0 0 2 2 2 2] | $64*X^{13}*Y^7 + 125*X^{12}*Y^8 + 120*X^{11}*Y^9 +$ | |
| 61 | [0 0 1 0 0 2 0 2 2 2] | $153*X^{10}*Y^{10} + 162*X^9*Y^{11} + 104*X^8*Y^{12} +$ | I-iii |
| | [0 0 0 1 0 2 2 2 2 2] | $104*X^7*Y^{13} + 16*X^6*Y^{14} + 44*X^5*Y^{15} + 16*X^3*Y^{17}$ | |
| | [0 0 0 0 1 2 2 2 3 3] | $+ 2*X*Y^{19}$ | |
| | [1 0 0 0 0 0 2 2 2 2 2] | $X^{20} + 5*X^{18}*Y^2 + 2*X^{17}*Y^3 + 22*X^{16}*Y^4 +$ | |
| | [0 1 0 0 0 0 2 0 0 1 1] | $14*X^{15}*Y^5 + 74*X^{14}*Y^6 + 36*X^{13}*Y^7 + 153*X^{12}*Y^8$ | |
| 62 | [0 0 1 0 0 2 2 0 0 0] | $+ 124*X^{11}*Y^9 + 153*X^{10}*Y^{10} + 156*X^9*Y^{11} +$ | I-iv |
| | [0 0 0 1 0 2 0 0 0 0] | $76*X^8*Y^{12} + 126*X^7*Y^{13} + 24*X^6*Y^{14} + 44*X^5*Y^{15}$ | |
| | [0 0 0 0 1 2 0 0 1 1] | $+ 4*X^4*Y^{16} + 8*X^3*Y^{17} + 2*X*Y^{19}$ | |
| | [1 0 0 0 0 0 2 2 2 3 3] | $X^{20} + 9*X^{18}*Y^2 + 46*X^{16}*Y^4 + 106*X^{14}*Y^6 +$ | |
| | [0 1 0 0 0 0 2 2 2 2] | $8*X^{13}*Y^7 + 165*X^{12}*Y^8 + 102*X^{11}*Y^9 + 141*X^{10}*Y^{10}$ | |
| 63 | [0 0 1 0 0 0 2 0 2 2 2] | $+ 156*X^9*Y^{11} + 44*X^8*Y^{12} + 148*X^7*Y^{13}$ | I-v |
| | [0 0 0 1 0 2 2 2 2 2] | $+ 72*X^5*Y^{15} + 22*X^3*Y^{17} + 4*X*Y^{19}$ | |
| | [0 0 0 0 1 2 2 2 3 3] | | |

| | | | |
|----|---|--|-------|
| | [1 0 0 0 0 1 0 2 2 2] [0 1 0 0 0 2 0 2 2 2] [0 0 1 0 0 0 1 0 0 0] [0 0 0 1 0 2 0 2 2 2] [0 0 0 0 1 2 0 2 2 2] | $X^{20} + 17*X^{18*Y^2} + 12*X^{17*Y^3} + 47*X^{16*Y^4} + 64*X^{15*Y^5} + 63*X^{14*Y^6} + 104*X^{13*Y^7} + 65*X^{12*Y^8} + 76*X^{11*Y^9} + 81*X^{10*Y^10} + 76*X^{9*Y^11} + 109*X^{8*Y^12} + 104*X^{7*Y^13} + 93*X^{6*Y^14} + 64*X^{5*Y^15} + 34*X^{4*Y^16} + 12*X^{3*Y^17} + 2*X^{2*Y^18}$ | I-i |
| 64 | [1 0 0 0 0 2 0 2 2 2] [0 1 0 0 0 0 0 2 2 2] [0 0 1 0 0 0 1 0 0 0] [0 0 0 1 0 2 0 2 2 2] [0 0 0 0 1 2 0 2 2 2] | $X^{20} + 18*X^{18*Y^2} + 75*X^{16*Y^4} + 156*X^{14*Y^6} + 2*X^{13*Y^7} + 167*X^{12*Y^8} + 40*X^{11*Y^9} + 82*X^{10*Y^10} + 130*X^{9*Y^11} + 13*X^{8*Y^12} + 176*X^{7*Y^13} + 118*X^{5*Y^15} + 40*X^{3*Y^17} + 6*X*Y^19$ | I-ii |
| 65 | [1 0 0 0 0 2 0 0 0 0] [0 1 0 0 0 0 0 2 2 2] [0 0 1 0 0 0 1 0 0 0] [0 0 0 1 0 2 0 0 0 0] [0 0 0 0 1 2 0 0 0 0] | $X^{20} + 18*X^{18*Y^2} + 6*X^{17*Y^3} + 63*X^{16*Y^4} + 38*X^{15*Y^5} + 92*X^{14*Y^6} + 86*X^{13*Y^7} + 63*X^{12*Y^8} + 118*X^{11*Y^9} + 30*X^{10*Y^10} + 130*X^{9*Y^11} + 65*X^{8*Y^12} + 98*X^{7*Y^13} + 104*X^{6*Y^14} + 34*X^{5*Y^15} + 64*X^{4*Y^16} + 2*X^{3*Y^17} + 12*X^{2*Y^18}$ | I-iii |
| 66 | [1 0 0 0 0 2 0 2 2 2] [0 1 0 0 0 2 0 2 2 2] [0 0 1 0 0 0 1 0 0 0] [0 0 0 1 0 2 0 0 0 0] [0 0 0 0 1 2 0 0 0 0] | $X^{20} + 30*X^{18*Y^2} + 127*X^{16*Y^4} + 196*X^{14*Y^6} + 127*X^{12*Y^8} + 8*X^{11*Y^9} + 30*X^{10*Y^10} + 72*X^{9*Y^11} + X^{8*Y^12} + 176*X^{7*Y^13} + 176*X^{5*Y^15} + 72*X^{3*Y^17} + 8*X*Y^19$ | I-iv |
| 67 | [1 0 0 0 0 2 0 0 0 0] [0 1 0 0 0 2 0 2 2 2] [0 0 1 0 0 0 1 0 0 0] [0 0 0 1 0 2 0 2 2 2] [0 0 0 0 1 2 0 2 2 2] | $X^{20} + 18*X^{18*Y^2} + 6*X^{17*Y^3} + 63*X^{16*Y^4} + 38*X^{15*Y^5} + 92*X^{14*Y^6} + 84*X^{13*Y^7} + 75*X^{12*Y^8} + 86*X^{11*Y^9} + 82*X^{10*Y^10} + 72*X^{9*Y^11} + 105*X^{8*Y^12} + 98*X^{7*Y^13} + 64*X^{6*Y^14} + 92*X^{5*Y^15} + 12*X^{4*Y^16} + 34*X^{3*Y^17} + 2*X*Y^19$ | I-v |
| 68 | [1 0 0 0 0 1 2 2 2 2] [0 1 0 0 0 2 2 2 2 2] [0 0 1 0 0 2 2 2 2 2] [0 0 0 1 0 2 2 2 2 2] [0 0 0 0 1 2 2 2 2 2] | $X^{20} + 28*X^{18*Y^2} + 16*X^{17*Y^3} + 71*X^{16*Y^4} + 112*X^{15*Y^5} + 56*X^{14*Y^6} + 112*X^{13*Y^7} + 71*X^{12*Y^8} + 16*X^{11*Y^9} + 30*X^{10*Y^10} + 16*X^{9*Y^11} + 57*X^{8*Y^12} + 112*X^{7*Y^13} + 140*X^{6*Y^14} + 112*X^{5*Y^15} + 56*X^{4*Y^16} + 16*X^{3*Y^17} + 2*X^{2*Y^18},$ | I-i |
| 69 | [1 0 0 0 0 3 2 2 2 2] [0 1 0 0 0 2 0 0 0 0] [0 0 1 0 0 2 0 0 0 0] [0 0 0 1 0 2 0 0 0 0] [0 0 0 0 1 2 0 0 0 0] | $X^{20} + 29*X^{18*Y^2} + 114*X^{16*Y^4} + 210*X^{14*Y^6} + 141*X^{12*Y^8} + 2*X^{11*Y^9} + 17*X^{10*Y^10} + 64*X^{9*Y^11} + 204*X^{7*Y^13} + 168*X^{5*Y^15} + 66*X^{3*Y^17} + 8*X*Y^19,$ | I-ii |
| 70 | | | |
| 71 | | | |

| | | | |
|----|-----------------------|--|-------|
| | [1 0 0 0 0 2 0 0 0 0] | $X^{20} + 29*X^{18}*Y^2 + 8*X^{17}*Y^3 + 98*X^{16}*Y^4 +$ | |
| 72 | [0 1 0 0 0 0 2 2 2 2] | $64*X^{15}*Y^5 + 98*X^{14}*Y^6 + 112*X^{13}*Y^7 + 29*X^{12}*Y^8$ | I-iii |
| | [0 0 1 0 0 2 0 0 0 0] | $+ 66*X^{11}*Y^9 + X^{10}*Y^{10} + 64*X^9*Y^{11} + 16*X^8*Y^{12}$ | |
| | [0 0 0 1 0 2 0 0 0 0] | $+ 140*X^7*Y^{13} + 112*X^6*Y^{14} + 56*X^5*Y^{15} +$ | |
| | [0 0 0 0 1 2 0 0 0 0] | $112*X^4*Y^{16} + 2*X^3*Y^{17} + 16*X^2*Y^{18}$ | |
| 73 | [1 0 0 0 0 2 2 2 2 2] | | |
| | [0 1 0 0 0 2 2 2 2 2] | $X^{20} + 45*X^{18}*Y^2 + 210*X^{16}*Y^4 + 210*X^{14}*Y^6 +$ | |
| | [0 0 1 0 0 2 2 2 2 2] | $45*X^{12}*Y^8 + X^{10}*Y^{10} + 10*X^9*Y^{11} + 120*X^7*Y^{13} +$ | I-iv |
| | [0 0 0 1 0 2 2 2 2 2] | $252*X^5*Y^{15} + 120*X^3*Y^{17} + 10*X*Y^{19}$ | |
| 74 | [1 0 0 0 0 2 0 0 0 0] | $X^{20} + 29*X^{18}*Y^2 + 8*X^{17}*Y^3 + 98*X^{16}*Y^4 +$ | |
| | [0 1 0 0 0 2 2 2 2 2] | $64*X^{15}*Y^5 + 98*X^{14}*Y^6 + 112*X^{13}*Y^7 + 29*X^{12}*Y^8$ | |
| | [0 0 1 0 0 2 0 0 0 0] | $+ 64*X^{11}*Y^9 + 17*X^{10}*Y^{10} + 10*X^9*Y^{11}$ | I-v |
| | [0 0 0 1 0 2 0 0 0 0] | $+ 112*X^8*Y^{12} + 56*X^7*Y^{13} + 112*X^6*Y^{14} +$ | |
| | [0 0 0 0 1 2 0 0 0 0] | $140*X^5*Y^{15} + 16*X^4*Y^{16} + 56*X^3*Y^{17} + 2*X*Y^{19}$ | |
| 75 | [1 0 0 0 0 1 2 1 1 0] | $X^{20} + 2*X^{17}*Y^3 + 8*X^{15}*Y^5 + 63*X^{14}*Y^6 +$ | |
| | [0 1 0 0 0 1 1 3 2 0] | $68*X^{13}*Y^7 + 102*X^{12}*Y^8 + 202*X^{11}*Y^9 +$ | |
| | [0 0 1 0 0 3 1 2 1 0] | $155*X^{10}*Y^{10} + 122*X^9*Y^{11} + 152*X^8*Y^{12} +$ | III |
| | [0 0 0 1 0 2 1 1 2 1] | $108*X^7*Y^{13} + 37*X^6*Y^{14} + X^4*Y^{16} + 2*X^3*Y^{17} +$ | |
| | [0 0 0 0 1 0 0 0 1 1] | X^2*Y^{18} | |
| 76 | [1 0 0 0 0 1 2 1 1 0] | $X^{20} + 2*X^{17}*Y^3 + 63*X^{14}*Y^6 + 108*X^{13}*Y^7 +$ | |
| | [0 1 0 0 0 1 1 3 2 0] | $102*X^{12}*Y^8 + 122*X^{11}*Y^9 + 155*X^{10}*Y^{10} +$ | |
| | [0 0 1 0 0 3 1 2 1 0] | $202*X^9*Y^{11} + 152*X^8*Y^{12} + 68*X^7*Y^{13} +$ | III |
| | [0 0 0 1 0 2 1 1 2 1] | $37*X^6*Y^{14} + 8*X^5*Y^{15} + X^4*Y^{16} + 2*X^3*Y^{17} +$ | |
| | [0 0 0 0 1 0 0 0 1 3] | X^2*Y^{18} | |
| 77 | [1 0 0 0 0 1 2 1 1 0] | | |
| | [0 1 0 0 0 1 1 3 2 0] | | |
| | [0 0 1 0 0 3 1 2 1 1] | | III |
| | [0 0 0 1 0 2 1 1 2 0] | $X^{20} + 2*X^{17}*Y^3 + 12*X^{15}*Y^5 + 47*X^{14}*Y^6 +$ | |
| | [0 0 0 0 1 0 1 0 0 1] | $88*X^{13}*Y^7 + 117*X^{12}*Y^8 + 144*X^{11}*Y^9 +$ | |
| 78 | [1 0 0 0 0 1 2 1 1 2] | $174*X^{10}*Y^{10} + 170*X^9*Y^{11} + 134*X^8*Y^{12} +$ | |
| | [0 1 0 0 0 1 1 3 2 3] | $84*X^7*Y^{13} + 35*X^6*Y^{14} + 12*X^5*Y^{15} + 4*X^4*Y^{16}$ | |
| | [0 0 1 0 0 3 1 2 1 2] | | |
| | [0 0 0 1 0 2 1 1 2 3] | | |
| | [0 0 0 0 1 2 2 3 3 2] | | III |
| 79 | [1 0 0 0 0 1 2 1 1 0] | $X^{20} + 2*X^{17}*Y^3 + 10*X^{15}*Y^5 + 49*X^{14}*Y^6 +$ | |
| | [0 1 0 0 0 1 1 3 2 0] | $94*X^{13}*Y^7 + 111*X^{12}*Y^8 + 140*X^{11}*Y^9 +$ | |
| | [0 0 1 0 0 3 1 2 1 1] | $178*X^{10}*Y^{10} + 166*X^9*Y^{11} + 138*X^8*Y^{12} +$ | III |
| | [0 0 0 1 0 2 1 1 2 0] | $90*X^7*Y^{13} + 29*X^6*Y^{14} + 10*X^5*Y^{15} + 6*X^4*Y^{16}$ | |
| | [0 0 0 0 1 0 1 0 0 3] | | |

| | | | |
|----|---|--|-----|
| | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 0] [0 0 0 1 0 2 1 1 2 0] [0 0 0 0 1 0 0 1 0 1] | X^20 + 2*X^17*Y^3 + 14*X^15*Y^5 + 45*X^14*Y^6 + 82*X^13*Y^7 + 123*X^12*Y^8 + 148*X^11*Y^9 + | III |
| 80 | [1 0 0 0 0 1 2 1 1 1] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 2] [0 0 0 1 0 2 1 1 2 2] [0 0 0 0 1 1 2 1 2 1] | 170*X^10*Y^10 + 174*X^9*Y^11 + 130*X^8*Y^12 + 78*X^7*Y^13 + 41*X^6*Y^14 + 14*X^5*Y^15 + 2*X^4*Y^16 | |
| 81 | [1 0 0 0 0 1 2 1 1 1] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 2] [0 0 0 1 0 2 1 1 2 2] [0 0 0 0 1 1 2 1 2 1] | X^20 + 2*X^17*Y^3 + 2*X^16*Y^4 + 10*X^15*Y^5 + 47*X^14*Y^6 + 88*X^13*Y^7 + 111*X^12*Y^8 + 150*X^11*Y^9 + 174*X^10*Y^10 + 170*X^9*Y^11 + 140*X^8*Y^12 + 78*X^7*Y^13 + 35*X^6*Y^14 + 12*X^5*Y^15 + 2*X^4*Y^16 + 2*X^3*Y^17 | III |
| 82 | [1 0 0 0 0 1 2 1 1 1] [0 1 0 0 0 1 1 3 2 0] [0 0 1 0 0 3 1 2 1 0] [0 0 0 1 0 2 1 1 2 1] [0 0 0 0 1 1 0 0 1 0] | X^20 + 2*X^17*Y^3 + 2*X^16*Y^4 + 14*X^15*Y^5 + 42*X^14*Y^6 + 80*X^13*Y^7 + 118*X^12*Y^8 + 156*X^11*Y^9 + 180*X^10*Y^10 + 162*X^9*Y^11 + 130*X^8*Y^12 + 86*X^7*Y^13 + 34*X^6*Y^14 + 12*X^5*Y^15 + 5*X^4*Y^16 | III |
| 83 | [1 0 0 0 0 1 2 1 1 1] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 2 1] [0 0 0 0 1 1 1 1 1 1] | X^20 + 2*X^17*Y^3 + 2*X^16*Y^4 + 14*X^15*Y^5 + 42*X^14*Y^6 + 88*X^13*Y^7 + 130*X^12*Y^8 + 156*X^11*Y^9 + 180*X^10*Y^10 + 162*X^9*Y^11 + 130*X^8*Y^12 + 86*X^7*Y^13 + 34*X^6*Y^14 + 12*X^5*Y^15 + 5*X^4*Y^16 | III |
| 84 | [1 0 0 0 0 1 2 1 1 1] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 2 2] [0 0 0 0 1 1 1 1 2 2] | X^20 + 2*X^17*Y^3 + 2*X^16*Y^4 + 14*X^15*Y^5 + 38*X^14*Y^6 + 88*X^13*Y^7 + 130*X^12*Y^8 + 124*X^11*Y^9 + 172*X^10*Y^10 + 210*X^9*Y^11 + 122*X^8*Y^12 + 54*X^7*Y^13 + 46*X^6*Y^14 + 20*X^5*Y^15 + X^4*Y^16 | III |
| 85 | [1 0 0 0 0 1 2 1 1 1] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 3] [0 0 0 1 0 2 1 1 2 1] [0 0 0 0 1 1 3 1 1 1] | X^20 + 2*X^17*Y^3 + 10*X^15*Y^5 + 46*X^14*Y^6 + 100*X^13*Y^7 + 120*X^12*Y^8 + 116*X^11*Y^9 + 172*X^10*Y^10 + 202*X^9*Y^11 + 132*X^8*Y^12 + 66*X^7*Y^13 + 38*X^6*Y^14 + 16*X^5*Y^15 + 3*X^4*Y^16 | III |
| 86 | [1 0 0 0 0 1 2 1 1 1] [0 1 0 0 0 1 1 3 2 2] [0 0 1 0 0 3 1 2 1 3] [0 0 0 1 0 2 1 1 2 2] [0 0 0 0 1 1 3 2 2 1] | X^20 + 2*X^17*Y^3 + 14*X^15*Y^5 + 44*X^14*Y^6 + 84*X^13*Y^7 + 126*X^12*Y^8 + 140*X^11*Y^9 + 168*X^10*Y^10 + 186*X^9*Y^11 + 128*X^8*Y^12 + 70*X^7*Y^13 + 44*X^6*Y^14 + 16*X^5*Y^15 + X^4*Y^16 | III |
| 87 | [1 0 0 0 0 1 2 1 1 1] [0 1 0 0 0 1 1 3 2 3] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 2 1] [0 0 0 0 1 1 1 3 1 3] | X^20 + 2*X^17*Y^3 + 10*X^15*Y^5 + 48*X^14*Y^6 + 96*X^13*Y^7 + 114*X^12*Y^8 + 132*X^11*Y^9 + 176*X^10*Y^10 + 178*X^9*Y^11 + 136*X^8*Y^12 + 82*X^7*Y^13 + 32*X^6*Y^14 + 12*X^5*Y^15 + 5*X^4*Y^16 | III |

| | | | |
|----|---|--|-----|
| | [1 0 0 0 0 1 2 1 1 2] [0 1 0 0 0 1 1 3 2 2] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 2 1] [0 0 0 0 1 2 1 2 1 1] | $X^{20} + 2*X^{17*Y^3} + 4*X^{16*Y^4} + 12*X^{15*Y^5} + 44*X^{14*Y^6} + 72*X^{13*Y^7} + 123*X^{12*Y^8} + 160*X^{11*Y^9} + 165*X^{10*Y^{10}} + 186*X^{9*Y^{11}} + 126*X^{8*Y^{12}} + 68*X^{7*Y^{13}} + 46*X^{6*Y^{14}} + 12*X^{5*Y^{15}} + 2*X^{4*Y^{16}} + X^{2*Y^{18}}$ | |
| 88 | [1 0 0 0 0 1 2 1 1 2] [0 1 0 0 0 1 1 3 2 2] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 2 1] [0 0 0 0 1 2 1 2 1 1] | $X^{20} + 2*X^{17*Y^3} + 3*X^{16*Y^4} + 14*X^{15*Y^5} + 39*X^{14*Y^6} + 82*X^{13*Y^7} + 120*X^{12*Y^8} + 148*X^{11*Y^9} + 182*X^{10*Y^{10}} + 174*X^{9*Y^{11}} + 127*X^{8*Y^{12}} + 78*X^{7*Y^{13}} + 35*X^{6*Y^{14}} + 14*X^{5*Y^{15}} + 5*X^{4*Y^{16}}$ | III |
| 89 | [1 0 0 0 0 1 2 1 1 2] [0 1 0 0 0 1 1 3 2 2] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 2 2] [0 0 0 0 1 2 1 2 2 2] | $X^{20} + 2*X^{17*Y^3} + 4*X^{15*Y^5} + 44*X^{14*Y^6} + 134*X^{13*Y^7} + 126*X^{12*Y^8} + 40*X^{11*Y^9} + 168*X^{10*Y^{10}} + 286*X^{9*Y^{11}} + 128*X^{8*Y^{12}} + 20*X^{7*Y^{13}} + 44*X^{6*Y^{14}} + 26*X^{5*Y^{15}} + X^{4*Y^{16}}$ | III |
| 90 | [1 0 0 0 0 1 2 1 1 1] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 3 3] [0 0 0 0 1 1 1 1 3 3] | $X^{20} + 2*X^{17*Y^3} + 8*X^{15*Y^5} + 48*X^{14*Y^6} + 106*X^{13*Y^7} + 114*X^{12*Y^8} + 112*X^{11*Y^9} + 176*X^{10*Y^{10}} + 198*X^{9*Y^{11}} + 136*X^{8*Y^{12}} + 72*X^{7*Y^{13}} + 32*X^{6*Y^{14}} + 14*X^{5*Y^{15}} + 5*X^{4*Y^{16}}$ | III |
| 91 | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 0] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 3 1] [0 0 0 0 1 0 1 0 1 0] | $X^{20} + 2*X^{17*Y^3} + 8*X^{15*Y^5} + 48*X^{14*Y^6} + 106*X^{13*Y^7} + 114*X^{12*Y^8} + 112*X^{11*Y^9} + 176*X^{10*Y^{10}} + 198*X^{9*Y^{11}} + 136*X^{8*Y^{12}} + 72*X^{7*Y^{13}} + 32*X^{6*Y^{14}} + 14*X^{5*Y^{15}} + 5*X^{4*Y^{16}}$ | III |
| 92 | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 3 2] [0 0 0 0 1 0 1 1 2 3] | $X^{20} + 2*X^{17*Y^3} + 12*X^{15*Y^5} + 44*X^{14*Y^6} + 94*X^{13*Y^7} + 126*X^{12*Y^8} + 120*X^{11*Y^9} + 168*X^{10*Y^{10}} + 206*X^{9*Y^{11}} + 128*X^{8*Y^{12}} + 60*X^{7*Y^{13}} + 44*X^{6*Y^{14}} + 18*X^{5*Y^{15}} + X^{4*Y^{16}}$ | III |
| 93 | [1 0 0 0 0 1 2 1 1 1] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 3 1] [0 0 0 0 1 1 1 1 1 1] | $X^{20} + 23*X^{16*Y^4} + 40*X^{14*Y^6} + 32*X^{13*Y^7} + 119*X^{12*Y^8} + 224*X^{11*Y^9} + 150*X^{10*Y^{10}} + 224*X^{9*Y^{11}} + 105*X^{8*Y^{12}} + 32*X^{7*Y^{13}} + 60*X^{6*Y^{14}} + 8*X^{4*Y^{16}} + 6*X^{2*Y^{18}}$ | I-i |
| 94 | [1 0 0 0 0 1 2 2 2 2] [0 1 0 0 0 2 1 1 3 1] [0 0 1 0 0 2 1 3 1 1] [0 0 0 1 0 2 1 1 1 1] [0 0 0 0 1 2 1 1 3 3] | $X^{20} + 21*X^{16*Y^4} + 44*X^{14*Y^6} + 32*X^{13*Y^7} + 121*X^{12*Y^8} + 224*X^{11*Y^9} + 142*X^{10*Y^{10}} + 224*X^{9*Y^{11}} + 107*X^{8*Y^{12}} + 32*X^{7*Y^{13}} + 64*X^{6*Y^{14}} + 6*X^{4*Y^{16}} + 6*X^{2*Y^{18}}$ | I-i |
| 95 | [1 0 0 0 0 1 2 2 2 2] [0 1 0 0 0 2 1 1 1 3] [0 0 1 0 0 2 1 2 0 1] [0 0 0 1 0 2 1 1 1 1] [0 0 0 0 1 2 1 0 2 1] | $X^{20} + 21*X^{16*Y^4} + 44*X^{14*Y^6} + 32*X^{13*Y^7} + 121*X^{12*Y^8} + 224*X^{11*Y^9} + 142*X^{10*Y^{10}} + 224*X^{9*Y^{11}} + 107*X^{8*Y^{12}} + 32*X^{7*Y^{13}} + 64*X^{6*Y^{14}} + 6*X^{4*Y^{16}} + 6*X^{2*Y^{18}}$ | I-i |

| | | | |
|-----|---|--|-----|
| 96 | [1 0 0 0 0 1 0 0 0 2] [0 1 0 0 0 2 2 1 1 2] [0 0 1 0 0 0 1 2 1 1] [0 0 0 1 0 0 1 1 3 2] [0 0 0 0 1 0 3 1 2 1] | $X^{20} + 3*X^{16*Y^4} + 65*X^{14*Y^6} + 80*X^{13*Y^7} + 109*X^{12*Y^8} + 176*X^{11*Y^9} + 145*X^{10*Y^{10}} + 176*X^{9*Y^{11}} + 137*X^{8*Y^{12}} + 80*X^{7*Y^{13}} + 43*X^{6*Y^{14}} + 6*X^{4*Y^{16}} + 3*X^{2*Y^{18}}$ | I-i |
| 97 | [1 0 0 0 0 1 2 0 0 0] [0 1 0 0 0 1 1 1 3 0] [0 0 1 0 0 1 0 2 2 0] [0 0 0 1 0 3 0 2 1 1] [0 0 0 0 1 0 0 0 1 2] | $X^{20} + 14*X^{16*Y^4} + 8*X^{15*Y^5} + 36*X^{14*Y^6} + 54*X^{13*Y^7} + 119*X^{12*Y^8} + 200*X^{11*Y^9} + 175*X^{10*Y^{10}} + 180*X^{9*Y^{11}} + 112*X^{8*Y^{12}} + 64*X^{7*Y^{13}} + 42*X^{6*Y^{14}} + 6*X^{5*Y^{15}} + 10*X^{4*Y^{16}} + 3*X^{2*Y^{18}}$ | III |
| 98 | [1 0 0 0 0 1 2 0 0 0] [0 1 0 0 0 1 1 1 3 2] [0 0 1 0 0 1 0 2 2 2] [0 0 0 1 0 3 0 2 1 1] [0 0 0 0 1 0 2 2 1 2] | $X^{20} + 10*X^{16*Y^4} + 14*X^{15*Y^5} + 27*X^{14*Y^6} + 70*X^{13*Y^7} + 124*X^{12*Y^8} + 172*X^{11*Y^9} + 195*X^{10*Y^{10}} + 172*X^{9*Y^{11}} + 110*X^{8*Y^{12}} + 70*X^{7*Y^{13}} + 33*X^{6*Y^{14}} + 14*X^{5*Y^{15}} + 11*X^{4*Y^{16}} + X^{2*Y^{18}}$ | III |
| 99 | [1 0 0 0 0 1 2 0 0 0] [0 1 0 0 0 1 1 1 3 0] [0 0 1 0 0 1 0 2 2 0] [0 0 0 1 0 3 0 2 1 2] [0 0 0 0 1 0 0 0 2 1] | $X^{20} + 5*X^{16*Y^4} + 18*X^{15*Y^5} + 30*X^{14*Y^6} + 70*X^{13*Y^7} + 125*X^{12*Y^8} + 180*X^{11*Y^9} + 196*X^{10*Y^{10}} + 140*X^{9*Y^{11}} + 115*X^{8*Y^{12}} + 90*X^{7*Y^{13}} + 30*X^{6*Y^{14}} + 14*X^{5*Y^{15}} + 10*X^{4*Y^{16}} + 3*X^{2*Y^{18}}$ | III |
| 100 | [1 0 0 0 0 1 2 0 0 0] [0 1 0 0 0 1 1 1 3 0] [0 0 1 0 0 1 0 2 2 1] [0 0 0 1 0 3 0 2 1 1] [0 0 0 0 1 0 1 0 1 2] | $X^{20} + 5*X^{16*Y^4} + 18*X^{15*Y^5} + 30*X^{14*Y^6} + 70*X^{13*Y^7} + 125*X^{12*Y^8} + 180*X^{11*Y^9} + 196*X^{10*Y^{10}} + 140*X^{9*Y^{11}} + 115*X^{8*Y^{12}} + 90*X^{7*Y^{13}} + 30*X^{6*Y^{14}} + 14*X^{5*Y^{15}} + 10*X^{4*Y^{16}} + 3*X^{2*Y^{18}}$ | III |
| 101 | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 1] [0 0 0 1 0 3 0 2 1 0] [0 0 0 0 1 1 1 1 0 3] | $X^{20} + 14*X^{16*Y^4} + 10*X^{15*Y^5} + 34*X^{14*Y^6} + 48*X^{13*Y^7} + 125*X^{12*Y^8} + 204*X^{11*Y^9} + 171*X^{10*Y^{10}} + 184*X^{9*Y^{11}} + 108*X^{8*Y^{12}} + 58*X^{7*Y^{13}} + 48*X^{6*Y^{14}} + 8*X^{5*Y^{15}} + 8*X^{4*Y^{16}} + 3*X^{2*Y^{18}}$ | III |
| 102 | [1 0 0 0 0 1 2 0 0 0] [0 1 0 0 0 1 1 1 3 0] [0 0 1 0 0 1 0 2 2 2] [0 0 0 1 0 3 0 2 1 1] [0 0 0 0 1 0 2 0 1 0] | $X^{20} + 14*X^{16*Y^4} + 10*X^{15*Y^5} + 34*X^{14*Y^6} + 48*X^{13*Y^7} + 125*X^{12*Y^8} + 204*X^{11*Y^9} + 171*X^{10*Y^{10}} + 184*X^{9*Y^{11}} + 108*X^{8*Y^{12}} + 58*X^{7*Y^{13}} + 48*X^{6*Y^{14}} + 8*X^{5*Y^{15}} + 8*X^{4*Y^{16}} + 3*X^{2*Y^{18}}$ | III |

| | | | |
|-----|---|---|-----|
| | [1 0 0 0 0 1 2 0 0 0] [0 1 0 0 0 1 1 1 3 0] [0 0 1 0 0 1 0 2 2 2] [0 0 0 1 0 3 0 2 1 1] [0 0 0 0 1 0 2 0 1 2] | X^20 + 8*X^16*Y^4 + 8*X^15*Y^5 + 48*X^14*Y^6 + 54*X^13*Y^7 + 125*X^12*Y^8 + 200*X^11*Y^9 + 151*X^10*Y^10 + 180*X^9*Y^11 + 118*X^8*Y^12 + | III |
| 103 | [1 0 0 0 0 1 2 0 0 2] [0 1 0 0 0 1 1 1 3 2] [0 0 1 0 0 1 0 2 2 0] [0 0 0 1 0 3 0 2 1 1] [0 0 0 0 1 2 0 2 1 2] | 64*X^7*Y^13 + 54*X^6*Y^14 + 6*X^5*Y^15 + 4*X^4*Y^16 + 3*X^2*Y^18 | III |
| 104 | [1 0 0 0 0 1 2 0 0 0] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 1] [0 0 0 1 0 3 0 2 1 0] [0 0 0 0 1 0 1 1 0 3] | X^20 + 7*X^16*Y^4 + 14*X^15*Y^5 + 33*X^14*Y^6 + 72*X^13*Y^7 + 118*X^12*Y^8 + 184*X^11*Y^9 + 186*X^10*Y^10 + 152*X^9*Y^11 + 127*X^8*Y^12 + 70*X^7*Y^13 + 37*X^6*Y^14 + 16*X^5*Y^15 + 3*X^4*Y^16 + 4*X^3*Y^17 | III |
| 105 | [1 0 0 0 0 1 2 0 0 0] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 3] [0 0 0 1 0 3 0 2 1 0] [0 0 0 0 1 0 3 1 0 1] | X^20 + 9*X^16*Y^4 + 10*X^15*Y^5 + 33*X^14*Y^6 + 82*X^13*Y^7 + 112*X^12*Y^8 + 170*X^11*Y^9 + 186*X^10*Y^10 + 172*X^9*Y^11 + 133*X^8*Y^12 + 54*X^7*Y^13 + 37*X^6*Y^14 + 18*X^5*Y^15 + X^4*Y^16 + 6*X^3*Y^17 | III |
| 106 | [1 0 0 0 0 1 2 0 0 0] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 3] [0 0 0 1 0 3 0 2 1 2] [0 0 0 0 1 0 3 1 2 3] | X^20 + 5*X^16*Y^4 + 16*X^15*Y^5 + 31*X^14*Y^6 + 76*X^13*Y^7 + 130*X^12*Y^8 + 162*X^11*Y^9 + 182*X^10*Y^10 + 176*X^9*Y^11 + 117*X^8*Y^12 + 60*X^7*Y^13 + 43*X^6*Y^14 + 20*X^5*Y^15 + 3*X^4*Y^16 + 2*X^3*Y^17 | III |
| 107 | [1 0 0 0 0 1 2 0 0 0] [0 1 0 0 0 1 1 1 3 2] [0 0 1 0 0 1 0 2 2 0] [0 0 0 1 0 3 0 2 1 1] [0 0 0 0 1 0 0 2 1 2] | X^20 + 12*X^16*Y^4 + 8*X^15*Y^5 + 40*X^14*Y^6 + 54*X^13*Y^7 + 121*X^12*Y^8 + 200*X^11*Y^9 + 167*X^10*Y^10 + 180*X^9*Y^11 + 114*X^8*Y^12 + | III |
| 108 | [1 0 0 0 0 1 2 0 0 2] [0 1 0 0 0 1 1 1 3 0] [0 0 1 0 0 1 0 2 2 2] [0 0 0 1 0 3 0 2 1 1] [0 0 0 0 1 2 2 0 1 2] | 64*X^7*Y^13 + 46*X^6*Y^14 + 6*X^5*Y^15 + 8*X^4*Y^16 + 3*X^2*Y^18 | III |
| 109 | [1 0 0 0 0 1 2 0 0 0] [0 1 0 0 0 1 1 1 3 2] [0 0 1 0 0 1 0 2 2 1] [0 0 0 1 0 3 0 2 1 1] [0 0 0 0 1 0 1 2 1 0] | X^20 + 3*X^16*Y^4 + 18*X^15*Y^5 + 34*X^14*Y^6 + 70*X^13*Y^7 + 127*X^12*Y^8 + 180*X^11*Y^9 + 188*X^10*Y^10 + 140*X^9*Y^11 + 117*X^8*Y^12 + 90*X^7*Y^13 + 34*X^6*Y^14 + 14*X^5*Y^15 + 8*X^4*Y^16 | III |
| 110 | | | |

| | | | |
|-----|-----------------------|--|-----|
| | [1 0 0 0 0 1 2 0 0 0] | $X^{20} + 10*X^{16}*Y^4 + 6*X^{15}*Y^5 + 46*X^{14}*Y^6 +$ | |
| | [0 1 0 0 0 1 1 1 3 2] | $60*X^{13}*Y^7 + 117*X^{12}*Y^8 + 196*X^{11}*Y^9 +$ | |
| 111 | [0 0 1 0 0 1 0 2 2 2] | $163*X^{10}*Y^{10} + 176*X^9*Y^{11} + 120*X^8*Y^{12} +$ | III |
| | [0 0 0 1 0 3 0 2 1 1] | $70*X^7*Y^{13} + 44*X^6*Y^{14} + 4*X^5*Y^{15} + 8*X^4*Y^{16} +$ | |
| | [0 0 0 0 1 0 2 2 1 0] | $3*X^2*Y^{18}$ | |
| | [1 0 0 0 0 1 2 0 0 0] | $X^{20} + 7*X^{16}*Y^4 + 14*X^{15}*Y^5 + 30*X^{14}*Y^6 +$ | |
| | [0 1 0 0 0 1 1 1 3 2] | $80*X^{13}*Y^7 + 119*X^{12}*Y^8 + 166*X^{11}*Y^9 +$ | |
| 112 | [0 0 1 0 0 1 0 2 2 2] | $196*X^{10}*Y^{10} + 160*X^9*Y^{11} + 121*X^8*Y^{12} +$ | III |
| | [0 0 0 1 0 3 0 2 1 1] | $74*X^7*Y^{13} + 30*X^6*Y^{14} + 16*X^5*Y^{15} + 8*X^4*Y^{16} +$ | |
| | [0 0 0 0 1 0 2 2 1 3] | $2*X^3*Y^{17}$ | |
| | [1 0 0 0 0 1 2 0 0 1] | $X^{20} + 3*X^{16}*Y^4 + 18*X^{15}*Y^5 + 35*X^{14}*Y^6 +$ | |
| | [0 1 0 0 0 1 1 1 3 0] | $66*X^{13}*Y^7 + 132*X^{12}*Y^8 + 182*X^{11}*Y^9 +$ | |
| 113 | [0 0 1 0 0 1 0 2 2 1] | $174*X^{10}*Y^{10} + 156*X^9*Y^{11} + 119*X^8*Y^{12} +$ | III |
| | [0 0 0 1 0 3 0 2 1 1] | $70*X^7*Y^{13} + 47*X^6*Y^{14} + 18*X^5*Y^{15} + X^4*Y^{16} +$ | |
| | [0 0 0 0 1 1 1 0 1 1] | $2*X^3*Y^{17}$ | |
| | [1 0 0 0 0 1 2 0 0 1] | $X^{20} + 3*X^{16}*Y^4 + 14*X^{15}*Y^5 + 39*X^{14}*Y^6 +$ | |
| | [0 1 0 0 0 1 1 1 3 0] | $78*X^{13}*Y^7 + 120*X^{12}*Y^8 + 174*X^{11}*Y^9 +$ | |
| 114 | [0 0 1 0 0 1 0 2 2 1] | $182*X^{10}*Y^{10} + 148*X^9*Y^{11} + 127*X^8*Y^{12} +$ | III |
| | [0 0 0 1 0 3 0 2 1 2] | $82*X^7*Y^{13} + 35*X^6*Y^{14} + 14*X^5*Y^{15} + 5*X^4*Y^{16} +$ | |
| | [0 0 0 0 1 1 1 0 2 1] | $2*X^3*Y^{17}$ | |
| | [1 0 0 0 0 1 2 0 0 1] | $X^{20} + 5*X^{16}*Y^4 + 18*X^{15}*Y^5 + 31*X^{14}*Y^6 +$ | |
| | [0 1 0 0 0 1 1 1 3 0] | $66*X^{13}*Y^7 + 130*X^{12}*Y^8 + 182*X^{11}*Y^9 +$ | |
| 115 | [0 0 1 0 0 1 0 2 2 3] | $182*X^{10}*Y^{10} + 156*X^9*Y^{11} + 117*X^8*Y^{12} +$ | III |
| | [0 0 0 1 0 3 0 2 1 3] | $70*X^7*Y^{13} + 43*X^6*Y^{14} + 18*X^5*Y^{15} + 3*X^4*Y^{16} +$ | |
| | [0 0 0 0 1 1 3 0 3 1] | $2*X^3*Y^{17}$ | |
| | [1 0 0 0 0 1 2 0 0 1] | $X^{20} + 3*X^{16}*Y^4 + 16*X^{15}*Y^5 + 33*X^{14}*Y^6 +$ | |
| | [0 1 0 0 0 1 1 1 3 1] | $82*X^{13}*Y^7 + 130*X^{12}*Y^8 + 152*X^{11}*Y^9 +$ | |
| 116 | [0 0 1 0 0 1 0 2 2 0] | $186*X^{10}*Y^{10} + 172*X^9*Y^{11} + 115*X^8*Y^{12} +$ | III |
| | [0 0 0 1 0 3 0 2 1 1] | $72*X^7*Y^{13} + 37*X^6*Y^{14} + 18*X^5*Y^{15} + 7*X^4*Y^{16}$ | |
| | [0 0 0 0 1 1 0 1 1 1] | | |
| | [1 0 0 0 0 1 2 0 0 1] | $X^{20} + 3*X^{16}*Y^4 + 18*X^{15}*Y^5 + 33*X^{14}*Y^6 +$ | |
| | [0 1 0 0 0 1 1 1 3 1] | $72*X^{13}*Y^7 + 130*X^{12}*Y^8 + 172*X^{11}*Y^9 +$ | |
| 117 | [0 0 1 0 0 1 0 2 2 0] | $186*X^{10}*Y^{10} + 152*X^9*Y^{11} + 115*X^8*Y^{12} +$ | III |
| | [0 0 0 1 0 3 0 2 1 1] | $82*X^7*Y^{13} + 37*X^6*Y^{14} + 16*X^5*Y^{15} + 7*X^4*Y^{16}$ | |
| | [0 0 0 0 1 1 0 1 1 3] | | |
| | [1 0 0 0 0 1 2 0 0 1] | $X^{20} + 13*X^{16}*Y^4 + 14*X^{15}*Y^5 + 27*X^{14}*Y^6 +$ | |
| | [0 1 0 0 0 1 1 1 3 1] | $52*X^{13}*Y^7 + 128*X^{12}*Y^8 + 196*X^{11}*Y^9 +$ | |
| 118 | [0 0 1 0 0 1 0 2 2 1] | $184*X^{10}*Y^{10} + 176*X^9*Y^{11} + 105*X^8*Y^{12} +$ | III |
| | [0 0 0 1 0 3 0 2 1 0] | $62*X^7*Y^{13} + 43*X^6*Y^{14} + 12*X^5*Y^{15} + 9*X^4*Y^{16} +$ | |
| | [0 0 0 0 1 1 1 0 0 0] | $2*X^2*Y^{18}$ | |

| | | | |
|-----|---|--|-----|
| | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 1] [0 0 0 1 0 3 0 2 1 0] [0 0 0 0 1 1 1 1 0 2] | X^20 + 7*X^16*Y^4 + 12*X^15*Y^5 + 41*X^14*Y^6 + 58*X^13*Y^7 + 128*X^12*Y^8 + 192*X^11*Y^9 + 164*X^10*Y^10 + 172*X^9*Y^11 + 115*X^8*Y^12 + 68*X^7*Y^13 + 49*X^6*Y^14 + 10*X^5*Y^15 + 5*X^4*Y^16 + 2*X^2*Y^18 | III |
| 119 | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 1] [0 0 0 1 0 3 0 2 1 2] [0 0 0 0 1 1 1 1 2 2] | X^20 + 3*X^16*Y^4 + 16*X^15*Y^5 + 37*X^14*Y^6 + 72*X^13*Y^7 + 126*X^12*Y^8 + 178*X^11*Y^9 + 178*X^10*Y^10 + 152*X^9*Y^11 + 123*X^8*Y^12 + 76*X^7*Y^13 + 41*X^6*Y^14 + 16*X^5*Y^15 + 3*X^4*Y^16 + 2*X^3*Y^17 | III |
| 120 | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 1] [0 0 0 1 0 3 0 2 1 0] [0 0 0 0 1 1 1 2 0 1] | X^20 + 8*X^16*Y^4 + 14*X^15*Y^5 + 26*X^14*Y^6 + 86*X^13*Y^7 + 116*X^12*Y^8 + 156*X^11*Y^9 + 212*X^10*Y^10 + 156*X^9*Y^11 + 116*X^8*Y^12 + 86*X^7*Y^13 + 18*X^6*Y^14 + 14*X^5*Y^15 + 15*X^4*Y^16 | III |
| 121 | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 1] [0 0 0 1 0 3 0 2 1 1] [0 0 0 0 1 1 1 1 1 0] | X^20 + 3*X^16*Y^4 + 14*X^15*Y^5 + 37*X^14*Y^6 + 82*X^13*Y^7 + 126*X^12*Y^8 + 158*X^11*Y^9 + 178*X^10*Y^10 + 172*X^9*Y^11 + 123*X^8*Y^12 + 66*X^7*Y^13 + 41*X^6*Y^14 + 18*X^5*Y^15 + 3*X^4*Y^16 + 2*X^3*Y^17 | III |
| 122 | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 2] [0 0 1 0 0 1 0 2 2 1] [0 0 0 1 0 3 0 2 1 0] [0 0 0 0 1 1 1 2 0 1] | X^20 + 6*X^16*Y^4 + 18*X^15*Y^5 + 26*X^14*Y^6 + 74*X^13*Y^7 + 130*X^12*Y^8 + 164*X^11*Y^9 + 196*X^10*Y^10 + 164*X^9*Y^11 + 110*X^8*Y^12 + 74*X^7*Y^13 + 34*X^6*Y^14 + 18*X^5*Y^15 + 9*X^4*Y^16 | III |
| 123 | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 1] [0 0 0 1 0 3 0 2 1 1] [0 0 0 0 1 1 1 1 1 1] | X^20 + 11*X^16*Y^4 + 10*X^15*Y^5 + 35*X^14*Y^6 + 64*X^13*Y^7 + 118*X^12*Y^8 + 188*X^11*Y^9 + 184*X^10*Y^10 + 168*X^9*Y^11 + 115*X^8*Y^12 + 74*X^7*Y^13 + 35*X^6*Y^14 + 8*X^5*Y^15 + 11*X^4*Y^16 + 2*X^2*Y^18 | III |
| 124 | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 1] [0 0 0 1 0 3 0 2 1 1] [0 0 0 0 1 1 1 1 1 2] | X^20 + 11*X^16*Y^4 + 10*X^15*Y^5 + 35*X^14*Y^6 + 64*X^13*Y^7 + 118*X^12*Y^8 + 188*X^11*Y^9 + 184*X^10*Y^10 + 168*X^9*Y^11 + 115*X^8*Y^12 + 74*X^7*Y^13 + 35*X^6*Y^14 + 8*X^5*Y^15 + 11*X^4*Y^16 + 2*X^3*Y^17 | III |
| 125 | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 1] [0 0 0 1 0 3 0 2 1 1] [0 0 0 0 1 1 1 1 1 3] | X^20 + 6*X^16*Y^4 + 18*X^15*Y^5 + 26*X^14*Y^6 + 74*X^13*Y^7 + 130*X^12*Y^8 + 164*X^11*Y^9 + 196*X^10*Y^10 + 164*X^9*Y^11 + 110*X^8*Y^12 + 74*X^7*Y^13 + 34*X^6*Y^14 + 18*X^5*Y^15 + 9*X^4*Y^16 | III |
| 126 | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 1] [0 0 0 1 0 3 0 2 1 2] [0 0 0 0 1 1 1 1 2 0] | X^20 + 11*X^16*Y^4 + 10*X^15*Y^5 + 35*X^14*Y^6 + 64*X^13*Y^7 + 118*X^12*Y^8 + 188*X^11*Y^9 + 184*X^10*Y^10 + 168*X^9*Y^11 + 115*X^8*Y^12 + 74*X^7*Y^13 + 35*X^6*Y^14 + 8*X^5*Y^15 + 11*X^4*Y^16 + 2*X^2*Y^18 | III |

| | | | |
|-----|---|--|-----|
| 127 | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 1] [0 0 0 1 0 3 0 2 1 2] [0 0 0 0 1 1 1 1 2 3] | $X^{20} + 5*X^{16}*Y^4 + 14*X^{15}*Y^5 + 30*X^{14}*Y^6 + 90*X^{13}*Y^7 + 125*X^{12}*Y^8 + 140*X^{11}*Y^9 + 196*X^{10}*Y^{10} + 180*X^9*Y^{11} + 115*X^8*Y^{12} + 70*X^7*Y^{13} + 30*X^6*Y^{14} + 18*X^5*Y^{15} + 10*X^4*Y^{16}$ | III |
| 128 | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 3] [0 0 0 1 0 3 0 2 1 0] [0 0 0 0 1 1 3 1 0 0] | $X^{20} + 5*X^{16}*Y^4 + 18*X^{15}*Y^5 + 29*X^{14}*Y^6 + 72*X^{13}*Y^7 + 128*X^{12}*Y^8 + 172*X^{11}*Y^9 + 194*X^{10}*Y^{10} + 152*X^9*Y^{11} + 113*X^8*Y^{12} + 82*X^7*Y^{13} + 33*X^6*Y^{14} + 16*X^5*Y^{15} + 9*X^4*Y^{16}$ | III |
| 129 | [1 0 0 0 0 1 2 0 0 2] [0 1 0 0 0 1 1 1 3 2] [0 0 1 0 0 1 0 2 2 1] [0 0 0 1 0 3 0 2 1 1] [0 0 0 0 1 2 1 2 1 3] | $X^{20} + 5*X^{16}*Y^4 + 12*X^{15}*Y^5 + 48*X^{14}*Y^6 + 52*X^{13}*Y^7 + 121*X^{12}*Y^8 + 216*X^{11}*Y^9 + 162*X^{10}*Y^{10} + 136*X^9*Y^{11} + 123*X^8*Y^{12} + 92*X^7*Y^{13} + 44*X^6*Y^{14} + 4*X^5*Y^{15} + 6*X^4*Y^{16} + 2*X^2*Y^{18}$ | III |
| 130 | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 3] [0 0 0 1 0 3 0 2 1 0] [0 0 0 0 1 1 3 1 0 1] | $X^{20} + 5*X^{16}*Y^4 + 16*X^{15}*Y^5 + 35*X^{14}*Y^6 + 78*X^{13}*Y^7 + 124*X^{12}*Y^8 + 168*X^{11}*Y^9 + 190*X^{10}*Y^{10} + 148*X^9*Y^{11} + 119*X^8*Y^{12} + 88*X^7*Y^{13} + 31*X^6*Y^{14} + 14*X^5*Y^{15} + 9*X^4*Y^{16}$ | III |
| 131 | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 3] [0 0 0 1 0 3 0 2 1 0] [0 0 0 0 1 1 3 1 0 2] | $X^{20} + 3*X^{16}*Y^4 + 16*X^{15}*Y^5 + 35*X^{14}*Y^6 + 78*X^{13}*Y^7 + 124*X^{12}*Y^8 + 168*X^{11}*Y^9 + 190*X^{10}*Y^{10} + 148*X^9*Y^{11} + 119*X^8*Y^{12} + 88*X^7*Y^{13} + 31*X^6*Y^{14} + 14*X^5*Y^{15} + 9*X^4*Y^{16}$ | III |
| 132 | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 3] [0 0 0 1 0 3 0 2 1 2] [0 0 0 0 1 1 3 1 2 2] | $X^{20} + 5*X^{16}*Y^4 + 10*X^{15}*Y^5 + 48*X^{14}*Y^6 + 62*X^{13}*Y^7 + 121*X^{12}*Y^8 + 196*X^{11}*Y^9 + 162*X^{10}*Y^{10} + 156*X^9*Y^{11} + 123*X^8*Y^{12} + 82*X^7*Y^{13} + 44*X^6*Y^{14} + 6*X^5*Y^{15} + 6*X^4*Y^{16} + 2*X^2*Y^{18}$ | III |
| 133 | [1 0 0 0 0 1 2 0 0 1] [0 1 0 0 0 1 1 1 3 1] [0 0 1 0 0 1 0 2 2 3] [0 0 0 1 0 3 0 2 1 0] [0 0 0 0 1 1 3 1 0 3] | $X^{20} + 5*X^{16}*Y^4 + 10*X^{15}*Y^5 + 48*X^{14}*Y^6 + 62*X^{13}*Y^7 + 121*X^{12}*Y^8 + 196*X^{11}*Y^9 + 162*X^{10}*Y^{10} + 156*X^9*Y^{11} + 123*X^8*Y^{12} + 82*X^7*Y^{13} + 44*X^6*Y^{14} + 6*X^5*Y^{15} + 6*X^4*Y^{16} + 2*X^2*Y^{18}$ | III |

| | | | |
|-----|---|---|-----|
| | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 0] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 3 1] [0 0 0 0 1 0 1 0 1 2] | | |
| 134 | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 3 2] [0 0 0 0 1 0 1 1 2 1] | X^20 + 6*X^15*Y^5 + 48*X^14*Y^6 + 112*X^13*Y^7 + 114*X^12*Y^8 + 118*X^11*Y^9 + 176*X^10*Y^10 + 192*X^9*Y^11 + 136*X^8*Y^12 + 66*X^7*Y^13 + 32*X^6*Y^14 + 16*X^5*Y^15 + 5*X^4*Y^16 + 2*X^3*Y^17 | III |
| 135 | [1 0 0 0 0 1 2 1 1 2] [0 1 0 0 0 1 1 3 2 2] [0 0 1 0 0 3 1 2 1 3] [0 0 0 1 0 2 1 1 3 1] [0 0 0 0 1 2 3 2 1 1] | | III |
| 136 | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 0] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 3 2] [0 0 0 0 1 0 1 0 2 1] | | III |
| 137 | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 3 2] [0 0 0 0 1 0 1 0 2 1] | X^20 + 6*X^15*Y^5 + 51*X^14*Y^6 + 102*X^13*Y^7 + 122*X^12*Y^8 + 124*X^11*Y^9 + 163*X^10*Y^10 + | III |
| 138 | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 3 1] [0 0 0 0 1 0 1 1 1 2] | 204*X^9*Y^11 + 128*X^8*Y^12 + 62*X^7*Y^13 + 41*X^6*Y^14 + 14*X^5*Y^15 + 5*X^4*Y^16 + X^2*Y^18 | III |
| 139 | [1 0 0 0 0 1 2 1 1 1] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 3 1] [0 0 0 0 1 1 1 1 1 3] | X^20 + 2*X^15*Y^5 + 44*X^14*Y^6 + 140*X^13*Y^7 + 126*X^12*Y^8 + 46*X^11*Y^9 + 168*X^10*Y^10 + 280*X^9*Y^11 + 128*X^8*Y^12 + 14*X^7*Y^13 + 44*X^6*Y^14 + 28*X^5*Y^15 + X^4*Y^16 + 2*X^3*Y^17 | III |
| 140 | [1 0 0 0 0 1 2 1 1 1] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 3 3] [0 0 0 0 1 1 1 1 1 3] | X^20 + 10*X^15*Y^5 + 44*X^14*Y^6 + 100*X^13*Y^7 + 126*X^12*Y^8 + 126*X^11*Y^9 + 168*X^10*Y^10 + 200*X^9*Y^11 + 128*X^8*Y^12 + 54*X^7*Y^13 + 44*X^6*Y^14 + 20*X^5*Y^15 + X^4*Y^16 + 2*X^3*Y^17 | III |

| | | | |
|-----|---|---|-----|
| | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 0] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 2 2] [0 0 0 0 1 0 1 0 2 1] | | |
| 141 | [1 0 0 0 0 1 2 1 1 1] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 2] [0 0 0 1 0 2 1 1 2 3] [0 0 0 0 1 1 2 1 3 0] | X^20 + 10*X^15*Y^5 + 47*X^14*Y^6 + 94*X^13*Y^7 + 117*X^12*Y^8 + 150*X^11*Y^9 + 174*X^10*Y^10 + 164*X^9*Y^11 + 134*X^8*Y^12 + 78*X^7*Y^13 + 35*X^6*Y^14 + 14*X^5*Y^15 + 4*X^4*Y^16 + 2*X^3*Y^17 | III |
| 142 | [1 0 0 0 0 1 2 1 1 1] [0 1 0 0 0 1 1 3 2 2] [0 0 1 0 0 3 1 2 1 2] [0 0 0 1 0 2 1 1 2 3] [0 0 0 0 1 1 2 2 3 0] | | III |
| 143 | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 0] [0 0 1 0 0 3 1 2 1 2] [0 0 0 1 0 2 1 1 2 3] [0 0 0 0 1 1 2 2 3 0] | | III |
| 144 | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 0] [0 0 1 0 0 3 1 2 1 2] [0 0 0 1 0 2 1 1 2 1] [0 0 0 0 1 0 2 0 1 1] | X^20 + 14*X^15*Y^5 + 47*X^14*Y^6 + 70*X^13*Y^7 + 134*X^12*Y^8 + 172*X^11*Y^9 + 55*X^10*Y^10 + 172*X^9*Y^11 + 120*X^8*Y^12 + 70*X^7*Y^13 + 53*X^6*Y^14 + 14*X^5*Y^15 + X^4*Y^16 + X^2*Y^18 | III |
| 145 | [1 0 0 0 0 1 2 1 1 2] [0 1 0 0 0 1 1 3 2 0] [0 0 1 0 0 3 1 2 1 2] [0 0 0 1 0 2 1 1 2 1] [0 0 0 0 1 2 2 0 1 1] | | III |
| 146 | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 0] [0 0 0 1 0 2 1 1 2 2] [0 0 0 0 1 0 0 1 2 1] | X^20 + 6*X^15*Y^5 + 53*X^14*Y^6 + 100*X^13*Y^7 + 107*X^12*Y^8 + 152*X^11*Y^9 + 70*X^10*Y^10 + 160*X^9*Y^11 + 146*X^8*Y^12 + 78*X^7*Y^13 + 33*X^6*Y^14 + 12*X^5*Y^15 + 2*X^4*Y^16 + 4*X^3*Y^17 | III |
| 147 | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 2 1] [0 0 0 0 1 0 1 1 1 2] | X^20 + 12*X^15*Y^5 + 42*X^14*Y^6 + 96*X^13*Y^7 + 124*X^12*Y^8 + 136*X^11*Y^9 + 180*X^10*Y^10 + 176*X^9*Y^11 + 124*X^8*Y^12 + 76*X^7*Y^13 + 34*X^6*Y^14 + 16*X^5*Y^15 + 7*X^4*Y^16 | III |

| | | | |
|-----|---|---|-----|
| | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 2 2] [0 0 0 0 1 0 1 1 2 1] | X^20 + 14*X^15*Y^5 + 42*X^14*Y^6 + 86*X^13*Y^7 + 124*X^12*Y^8 + 156*X^11*Y^9 + 180*X^10*Y^10 + | III |
| 148 | [1 0 0 0 0 1 2 1 1 1] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 2 3] [0 0 0 0 1 1 1 1 3 1] | 156*X^9*Y^11 + 124*X^8*Y^12 + 86*X^7*Y^13 + 34*X^6*Y^14 + 14*X^5*Y^15 + 7*X^4*Y^16 | III |
| 149 | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 2 3] [0 0 0 0 1 1 1 1 3 1] | X^20 + 12*X^15*Y^5 + 43*X^14*Y^6 + 94*X^13*Y^7 + 121*X^12*Y^8 + 144*X^11*Y^9 + 182*X^10*Y^10 + 164*X^9*Y^11 + 126*X^8*Y^12 + 84*X^7*Y^13 + 31*X^6*Y^14 + 14*X^5*Y^15 + 8*X^4*Y^16 | III |
| 150 | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 2] [0 0 0 1 0 2 1 1 2 1] [0 0 0 0 1 0 2 1 1 2] | X^20 + 10*X^15*Y^5 + 50*X^14*Y^6 + 84*X^13*Y^7 + 125*X^12*Y^8 + 156*X^11*Y^9 + 161*X^10*Y^10 + 176*X^9*Y^11 + 126*X^8*Y^12 + 74*X^7*Y^13 + 44*X^6*Y^14 + 12*X^5*Y^15 + 4*X^4*Y^16 + X^2*Y^18 | III |
| 151 | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 2] [0 0 0 1 0 2 1 1 2 3] [0 0 0 0 1 0 2 1 3 1] | X^20 + 8*X^15*Y^5 + 49*X^14*Y^6 + 100*X^13*Y^7 + 111*X^12*Y^8 + 146*X^11*Y^9 + 178*X^10*Y^10 + 160*X^9*Y^11 + 138*X^8*Y^12 + 84*X^7*Y^13 + 29*X^6*Y^14 + 12*X^5*Y^15 + 6*X^4*Y^16 + 2*X^3*Y^17 | III |
| 152 | [1 0 0 0 0 1 2 1 1 0] [0 1 0 0 0 1 1 3 2 0] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 2 3] [0 0 0 0 1 0 1 0 3 2] | X^20 + 10*X^15*Y^5 + 47*X^14*Y^6 + 90*X^13*Y^7 + 134*X^12*Y^8 + 132*X^11*Y^9 + 155*X^10*Y^10 + 212*X^9*Y^11 + 120*X^8*Y^12 + 50*X^7*Y^13 + 53*X^6*Y^14 + 18*X^5*Y^15 + X^4*Y^16 + X^2*Y^18 | III |
| 153 | [1 0 0 0 0 1 2 1 1 2] [0 1 0 0 0 1 1 3 2 2] [0 0 1 0 0 3 1 2 1 2] [0 0 0 1 0 2 1 1 2 1] [0 0 0 0 1 2 2 2 1 3] | X^20 + 18*X^15*Y^5 + 47*X^14*Y^6 + 50*X^13*Y^7 + 134*X^12*Y^8 + 212*X^11*Y^9 + 155*X^10*Y^10 + 132*X^9*Y^11 + 120*X^8*Y^12 + 90*X^7*Y^13 + 53*X^6*Y^14 + 10*X^5*Y^15 + X^4*Y^16 + X^2*Y^18 | III |
| 154 | [1 0 0 0 0 1 2 1 1 2] [0 1 0 0 0 1 1 3 2 2] [0 0 1 0 0 3 1 2 1 2] [0 0 0 1 0 2 1 1 2 1] [0 0 0 0 1 2 2 2 1 1] | X^20 + 12*X^15*Y^5 + 40*X^14*Y^6 + 100*X^13*Y^7 + 130*X^12*Y^8 + 120*X^11*Y^9 + 176*X^10*Y^10 + 200*X^9*Y^11 + 120*X^8*Y^12 + 60*X^7*Y^13 + 40*X^6*Y^14 + 20*X^5*Y^15 + 5*X^4*Y^16 | III |
| 155 | [1 0 0 0 0 1 2 1 1 2] [0 1 0 0 0 1 1 3 2 1] [0 0 1 0 0 3 1 2 1 3] [0 0 0 1 0 2 1 1 2 1] [0 0 0 0 1 2 3 1 1 0] | | III |

| | | | |
|-----|---|---|-----|
| 156 | [1 0 0 0 0 1 2 1 1 2] [0 1 0 0 0 1 1 3 2 2] [0 0 1 0 0 3 1 2 1 1] [0 0 0 1 0 2 1 1 2 3] [0 0 0 0 1 2 1 2 3 1] | $X^{20} + 8*X^{15}*Y^5 + 52*X^{14}*Y^6 + 90*X^{13}*Y^7 + 119*X^{12}*Y^8 + 152*X^{11}*Y^9 + 165*X^{10}*Y^{10} + 172*X^9*Y^{11} + 130*X^8*Y^{12} + 80*X^7*Y^{13} + 38*X^6*Y^{14} + 10*X^5*Y^{15} + 6*X^4*Y^{16} + X^2*Y^{18}$ | III |
| 157 | [1 0 0 0 0 2 1 1 1 0] [0 1 0 0 0 1 2 3 1 2] [0 0 1 0 0 1 1 2 0 1] [0 0 0 1 0 1 0 1 2 3] [0 0 0 0 1 0 1 2 1 3] | | III |
| 158 | [1 0 0 0 0 2 1 1 1 2] [0 1 0 0 0 1 2 3 1 2] [0 0 1 0 0 1 1 2 0 1] [0 0 0 1 0 1 0 1 2 3] [0 0 0 0 1 0 1 2 1 3] | | III |
| 159 | [1 0 0 0 0 1 2 1 0 1] [0 1 0 0 0 1 1 3 2 2] [0 0 1 0 0 3 1 2 1 2] [0 0 0 1 0 2 0 1 3 3] [0 0 0 0 1 2 1 2 3 1] | | III |
| 160 | [1 0 0 0 0 1 2 1 0 3] [0 1 0 0 0 1 1 3 2 0] [0 0 1 0 0 3 1 2 1 2] [0 0 0 1 0 2 0 1 3 1] [0 0 0 0 1 2 1 2 3 1] | $X^{20} + 90X^{14}Y^6 + 255X^{12}Y^8 + 332X^{10}Y^{10} + 255X^8Y^{12} + 90X^6Y^{14} + Y^{20}$ | III |
| 161 | [1 0 0 0 0 1 1 1 1 3] [0 1 0 0 0 0 1 2 3 1] [0 0 1 0 0 2 1 3 2 3] [0 0 0 1 0 3 1 2 1 2] [0 0 0 0 1 1 3 3 2 0] | | III |
| 162 | [1 0 0 0 0 1 1 1 1 3] [0 1 0 0 0 0 1 2 3 1] [0 0 1 0 0 2 1 3 2 3] [0 0 0 1 0 3 1 2 1 0] [0 0 0 0 1 1 3 3 0 2] | | III |
| 163 | [1 0 0 0 0 1 2 1 1 2] [0 1 0 0 0 1 1 2 2 1] [0 0 1 0 0 2 1 0 3 3] [0 0 0 1 0 2 1 3 1 2] [0 0 0 0 1 1 2 3 2 3] | | III |

Table 10. Non-free formally self-dual codes over Z_4 of length 10

| No. | Generator matrix | Lee weight enumerator | Const. |
|-----|--|--|--------|
| 1 | $[1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 2 \ 2]$ $[0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0 \ 0]$ | $X^{20} + 2*X^{19*Y} + 9*X^{18*Y^2} + 24*X^{17*Y^3} + 39*X^{16*Y^4} + 62*X^{15*Y^5} + 81*X^{14*Y^6} + 92*X^{13*Y^7} + 113*X^{12*Y^8} + 126*X^{11*Y^9} + 131*X^{10*Y^{10}} + 128*X^{9*Y^{11}} + 101*X^{8*Y^{12}} + 66*X^{7*Y^{13}} + 35*X^{6*Y^{14}} + 12*X^{5*Y^{15}} + 2*X^{4*Y^{16}}$ | II |
| 2 | $[1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0]$ $[0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 2 \ 2]$ $[0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0 \ 0]$ | $X^{20} + 9*X^{18*Y^2} + 10*X^{17*Y^3} + 23*X^{16*Y^4} + 48*X^{15*Y^5} + 49*X^{14*Y^6} + 86*X^{13*Y^7} + 97*X^{12*Y^8} + 100*X^{11*Y^9} + 131*X^{10*Y^{10}} + 118*X^{9*Y^{11}} + 117*X^{8*Y^{12}} + 104*X^{7*Y^{13}} + 67*X^{6*Y^{14}} + 42*X^{5*Y^{15}} + 18*X^{4*Y^{16}} + 4*X^{3*Y^{17}}$ | II |
| 3 | $[1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0]$ $[0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 2 \ 2]$ $[0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0 \ 0]$ | $X^{20} + 10*X^{18*Y^2} + 8*X^{17*Y^3} + 32*X^{16*Y^4} + 40*X^{15*Y^5} + 56*X^{14*Y^6} + 88*X^{13*Y^7} + 82*X^{12*Y^8} + 120*X^{11*Y^9} + 116*X^{10*Y^{10}} + 120*X^{9*Y^{11}} + 120*X^{8*Y^{12}} + 88*X^{7*Y^{13}} + 72*X^{6*Y^{14}} + 40*X^{5*Y^{15}} + 21*X^{4*Y^{16}} + 8*X^{3*Y^{17}} + 2*X^{2*Y^{18}}$ | II |
| 4 | $[1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0]$ $[0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 2 \ 2]$ $[0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0 \ 0]$ | $X^{20} + 2*X^{19*Y} + 10*X^{18*Y^2} + 22*X^{17*Y^3} + 39*X^{16*Y^4} + 66*X^{15*Y^5} + 80*X^{14*Y^6} + 102*X^{13*Y^7} + 119*X^{12*Y^8} + 118*X^{11*Y^9} + 130*X^{10*Y^{10}} + 114*X^{9*Y^{11}} + 89*X^{8*Y^{12}} + 70*X^{7*Y^{13}} + 36*X^{6*Y^{14}} + 18*X^{5*Y^{15}} + 8*X^{4*Y^{16}}$ | II |
| 5 | $[1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0]$ $[0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0]$ $[0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 2 \ 2]$ $[0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0 \ 0]$ | $X^{20} + 10*X^{18*Y^2} + 6*X^{17*Y^3} + 31*X^{16*Y^4} + 40*X^{15*Y^5} + 52*X^{14*Y^6} + 102*X^{13*Y^7} + 75*X^{12*Y^8} + 128*X^{11*Y^9} + 122*X^{10*Y^{10}} + 98*X^{9*Y^{11}} + 137*X^{8*Y^{12}} + 72*X^{7*Y^{13}} + 72*X^{6*Y^{14}} + 50*X^{5*Y^{15}} + 12*X^{4*Y^{16}} + 16*X^{3*Y^{17}}$ | II |
| 6 | $[1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0]$ $[0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0]$ $[0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 2 \ 2]$ $[0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0 \ 0 \ 0]$ $[0 \ 0 \ 0 \ 0 \ 0 \ 2 \ 0 \ 0 \ 0 \ 0]$ | $X^{20} + 11*X^{18*Y^2} + 4*X^{17*Y^3} + 41*X^{16*Y^4} + 26*X^{15*Y^5} + 75*X^{14*Y^6} + 80*X^{13*Y^7} + 83*X^{12*Y^8} + 142*X^{11*Y^9} + 81*X^{10*Y^{10}} + 148*X^{9*Y^{11}} + 91*X^{8*Y^{12}} + 86*X^{7*Y^{13}} + 81*X^{6*Y^{14}} + 24*X^{5*Y^{15}} + 40*X^{4*Y^{16}} + 2*X^{3*Y^{17}} + 8*X^{2*Y^{18}}$ | II |

| | | | |
|----|--|---|----|
| 7 | [1 0 0 0 0 0 0 0 0 0] [0 1 0 0 0 0 0 2 2 2] [0 0 1 0 0 0 0 0 2 2] [0 0 0 1 0 0 0 2 2 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 2*X^{19*Y} + 10*X^{18*Y^2} + 18*X^{17*Y^3} + 39*X^{16*Y^4} + 62*X^{15*Y^5} + 80*X^{14*Y^6} + 114*X^{13*Y^7} + 119*X^{12*Y^8} + 130*X^{11*Y^9} + 130*X^{10*Y^10} + 102*X^{9*Y^11} + 89*X^{8*Y^12} + 58*X^{7*Y^13} + 36*X^{6*Y^14} + 22*X^{5*Y^15} + 8*X^{4*Y^16} + 4*X^{3*Y^17}$ | II |
| 8 | [1 0 0 0 0 0 2 0 0 0] [0 1 0 0 0 0 0 2 2 2] [0 0 1 0 0 0 0 0 2 2] [0 0 0 1 0 0 0 2 2 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 10*X^{18*Y^2} + 2*X^{17*Y^3} + 39*X^{16*Y^4} + 20*X^{15*Y^5} + 76*X^{14*Y^6} + 82*X^{13*Y^7} + 83*X^{12*Y^8} + 156*X^{11*Y^9} + 82*X^{10*Y^10} + 150*X^{9*Y^11} + 97*X^{8*Y^12} + 76*X^{7*Y^13} + 80*X^{6*Y^14} + 22*X^{5*Y^15} + 36*X^{4*Y^16} + 4*X^{3*Y^17} + 8*X^{2*Y^18}$ | II |
| 9 | [1 0 0 0 0 0 1 0 0 0] [0 1 0 0 0 0 0 2 2 2] [0 0 1 0 0 0 0 0 2 2] [0 0 0 1 0 0 0 2 2 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 11*X^{18*Y^2} + 49*X^{16*Y^4} + 2*X^{15*Y^5} + 115*X^{14*Y^6} + 24*X^{13*Y^7} + 155*X^{12*Y^8} + 86*X^{11*Y^9} + 121*X^{10*Y^10} + 148*X^{9*Y^11} + 51*X^{8*Y^12} + 142*X^{7*Y^13} + 9*X^{6*Y^14} + 80*X^{5*Y^15} + 26*X^{3*Y^17} + 4*X*Y^19$ | II |
| 10 | [1 0 0 0 0 0 0 0 0 0] [0 1 0 0 0 0 0 2 2 2] [0 0 1 0 0 0 0 2 0 0] [0 0 0 1 0 0 0 2 0 0] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 2*X^{19*Y} + 10*X^{18*Y^2} + 22*X^{17*Y^3} + 39*X^{16*Y^4} + 64*X^{15*Y^5} + 84*X^{14*Y^6} + 102*X^{13*Y^7} + 115*X^{12*Y^8} + 124*X^{11*Y^9} + 122*X^{10*Y^10} + 114*X^{9*Y^11} + 97*X^{8*Y^12} + 64*X^{7*Y^13} + 40*X^{6*Y^14} + 18*X^{5*Y^15} + 4*X^{4*Y^16} + 2*X^{3*Y^17}$ | II |
| 11 | [1 0 0 0 0 0 2 0 0 0] [0 1 0 0 0 0 0 2 2 2] [0 0 1 0 0 0 0 2 0 0] [0 0 0 1 0 0 0 2 0 0] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 10*X^{18*Y^2} + 6*X^{17*Y^3} + 31*X^{16*Y^4} + 38*X^{15*Y^5} + 60*X^{14*Y^6} + 86*X^{13*Y^7} + 95*X^{12*Y^8} + 118*X^{11*Y^9} + 110*X^{10*Y^10} + 130*X^{9*Y^11} + 97*X^{8*Y^12} + 98*X^{7*Y^13} + 72*X^{6*Y^14} + 34*X^{5*Y^15} + 32*X^{4*Y^16} + 2*X^{3*Y^17} + 4*X^{2*Y^18}$ | II |
| 12 | [1 0 0 0 0 0 1 0 0 0] [0 1 0 0 0 0 0 2 2 2] [0 0 1 0 0 0 0 2 0 0] [0 0 0 1 0 0 0 2 0 0] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 11*X^{18*Y^2} + 4*X^{17*Y^3} + 41*X^{16*Y^4} + 24*X^{15*Y^5} + 83*X^{14*Y^6} + 62*X^{13*Y^7} + 115*X^{12*Y^8} + 100*X^{11*Y^9} + 121*X^{10*Y^10} + 122*X^{9*Y^11} + 91*X^{8*Y^12} + 112*X^{7*Y^13} + 41*X^{6*Y^14} + 66*X^{5*Y^15} + 8*X^{4*Y^16} + 20*X^{3*Y^17} + 2*X*Y^19$ | II |

| | | | |
|----|--|--|----|
| 13 | [1 0 0 0 0 0 0 0 0 0] [0 1 0 0 0 0 0 2 2 2] [0 0 1 0 0 0 0 2 2 2] [0 0 0 1 0 0 0 2 2 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 2*X^{19*Y} + 18*X^{18*Y^2} + 34*X^{17*Y^3} + 63*X^{16*Y^4} + 92*X^{15*Y^5} + 92*X^{14*Y^6} + 98*X^{13*Y^7} + 75*X^{12*Y^8} + 72*X^{11*Y^9} + 82*X^{10*Y^10} + 86*X^{9*Y^11} + 105*X^{8*Y^12} + 84*X^{7*Y^13} + 4*X^{6*Y^14} + 38*X^{5*Y^15} + 12*X^{4*Y^16} + 6*X^{3*Y^17}$ | II |
| 14 | [1 0 0 0 0 0 2 0 0 0] [0 1 0 0 0 0 0 2 2 2] [0 0 1 0 0 0 0 2 2 2] [0 0 0 1 0 0 0 2 2 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 18*X^{18*Y^2} + 2*X^{17*Y^3} + 63*X^{16*Y^4} + 34*X^{15*Y^5} + 92*X^{14*Y^6} + 98*X^{13*Y^7} + 63*X^{12*Y^8} + 130*X^{11*Y^9} + 30*X^{10*Y^10} + 118*X^{9*Y^11} + 65*X^{8*Y^12} + 86*X^{7*Y^13} + 104*X^{6*Y^14} + 38*X^{5*Y^15} + 64*X^{4*Y^16} + 6*X^{3*Y^17} + 12*X^{2*Y^18}$ | II |
| 15 | [1 0 0 0 0 0 1 0 0 0] [0 1 0 0 0 0 0 2 2 2] [0 0 1 0 0 0 0 2 2 2] [0 0 0 1 0 0 0 2 2 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 19*X^{18*Y^2} + 81*X^{16*Y^4} + 155*X^{14*Y^6} + 6*X^{13*Y^7} + 155*X^{12*Y^8} + 44*X^{11*Y^9} + 81*X^{10*Y^10} + 122*X^{9*Y^11} + 19*X^{8*Y^12} + 168*X^{7*Y^13} + X^{6*Y^14} + 122*X^{5*Y^15} + 44*X^{3*Y^17} + 6*X*Y^19$ | II |
| 16 | [1 0 0 0 0 0 0 0 0 0] [0 1 0 0 0 0 0 1 2 0] [0 0 1 0 0 0 0 2 0 0] [0 0 0 1 0 0 0 0 0 1] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 2*X^{19*Y} + 6*X^{18*Y^2} + 14*X^{17*Y^3} + 26*X^{16*Y^4} + 50*X^{15*Y^5} + 78*X^{14*Y^6} + 110*X^{13*Y^7} + 140*X^{12*Y^8} + 150*X^{11*Y^9} + 146*X^{10*Y^10} + 122*X^{9*Y^11} + 86*X^{8*Y^12} + 54*X^{7*Y^13} + 26*X^{6*Y^14} + 10*X^{5*Y^15} + 3*X^{4*Y^16}$ | II |
| 17 | [1 0 0 0 0 0 2 0 0 0] [0 1 0 0 0 0 0 1 2 0] [0 0 1 0 0 0 0 2 0 0] [0 0 0 1 0 0 0 0 0 1] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 6*X^{18*Y^2} + 6*X^{17*Y^3} + 18*X^{16*Y^4} + 34*X^{15*Y^5} + 46*X^{14*Y^6} + 86*X^{13*Y^7} + 100*X^{12*Y^8} + 130*X^{11*Y^9} + 146*X^{10*Y^10} + 130*X^{9*Y^11} + 126*X^{8*Y^12} + 86*X^{7*Y^13} + 58*X^{6*Y^14} + 34*X^{5*Y^15} + 11*X^{4*Y^16} + 6*X^{3*Y^17}$ | II |

| | | | |
|----|--|--|--------------|
| | | | |
| 18 | [1 0 0 0 0 0 1 2 2 2] [0 1 0 0 0 0 2 2 0 0] [0 0 1 0 0 0 2 2 2 0] [0 0 0 1 0 0 2 2 2 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $\begin{aligned} X^{20} + 5*X^{18*Y^2} + 4*X^{17*Y^3} + 19*X^{16*Y^4} + \\ 24*X^{15*Y^5} + 51*X^{14*Y^6} + 80*X^{13*Y^7} + 101*X^{12*Y^8} \\ + 148*X^{11*Y^9} + 141*X^{10*Y^10} + 148*X^{9*Y^11} + \\ 121*X^{8*Y^12} + 80*X^{7*Y^13} + 57*X^{6*Y^14} + 24*X^{5*Y^15} \\ + 14*X^{4*Y^16} + 4*X^{3*Y^17} + 2*X^{2*Y^18} \end{aligned}$ | I-i |
| 19 | [1 0 0 0 0 0 1 2 2 2] [0 1 0 0 0 0 2 0 0 2] [0 0 1 0 0 0 2 0 0 0] [0 0 0 1 0 0 2 0 2 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | | |
| 20 | [1 0 0 0 0 0 0 2 2 0 0] [0 1 0 0 0 0 0 2 2 2] [0 0 1 0 0 0 2 2 2 0] [0 0 0 1 0 0 2 2 2 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $\begin{aligned} X^{20} + 6*X^{18*Y^2} + 27*X^{16*Y^4} + 10*X^{15*Y^5} + \\ 76*X^{14*Y^6} + 54*X^{13*Y^7} + 139*X^{12*Y^8} + 122*X^{11*Y^9} \\ + 150*X^{10*Y^10} + 150*X^{9*Y^11} + 85*X^{8*Y^12} + \\ 110*X^{7*Y^13} + 24*X^{6*Y^14} + 50*X^{5*Y^15} + 4*X^{4*Y^16} + \\ 14*X^{3*Y^17} + 2*X*Y^19 \end{aligned}$ | I- ii,iii |
| 21 | [1 0 0 0 0 0 0 2 0 2 2] [0 1 0 0 0 0 0 2 2 2] [0 0 1 0 0 0 2 0 0 2] [0 0 0 1 0 0 2 0 0 0] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $\begin{aligned} X^{20} + 6*X^{18*Y^2} + 2*X^{17*Y^3} + 23*X^{16*Y^4} + \\ 20*X^{15*Y^5} + 60*X^{14*Y^6} + 82*X^{13*Y^7} + 99*X^{12*Y^8} + \\ 156*X^{11*Y^9} + 122*X^{10*Y^10} + 150*X^{9*Y^11} + \\ 113*X^{8*Y^12} + 76*X^{7*Y^13} + 64*X^{6*Y^14} + 22*X^{5*Y^15} \\ + 20*X^{4*Y^16} + 4*X^{3*Y^17} + 4*X^{2*Y^18} \end{aligned}$ | I- ii,iii |
| 22 | [1 0 0 0 0 0 0 2 2 2 2] [0 1 0 0 0 0 2 2 0 0] [0 0 1 0 0 0 2 2 2 0] [0 0 0 1 0 0 2 2 2 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $\begin{aligned} X^{20} + 10*X^{18*Y^2} + 43*X^{16*Y^4} + 2*X^{15*Y^5} + \\ 116*X^{14*Y^6} + 20*X^{13*Y^7} + 167*X^{12*Y^8} + 82*X^{11*Y^9} \\ + 122*X^{10*Y^10} + 156*X^{9*Y^11} + 45*X^{8*Y^12} + \\ 150*X^{7*Y^13} + 8*X^{6*Y^14} + 76*X^{5*Y^15} + 22*X^{3*Y^17} + \\ 4*X*Y^19 \end{aligned}$ | I- iv,v |
| 23 | [1 0 0 0 0 0 0 2 0 2 2] [0 1 0 0 0 0 0 2 2 2 2] [0 0 1 0 0 0 0 2 0 0 2] [0 0 0 1 0 0 0 2 0 0 0] [0 0 0 0 2 0 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0 0] | $\begin{aligned} X^{20} + 6*X^{18*Y^2} + 2*X^{17*Y^3} + 27*X^{16*Y^4} + \\ 12*X^{15*Y^5} + 76*X^{14*Y^6} + 48*X^{13*Y^7} + 139*X^{12*Y^8} \\ + 116*X^{11*Y^9} + 150*X^{10*Y^10} + 156*X^{9*Y^11} + \\ 85*X^{8*Y^12} + 116*X^{7*Y^13} + 24*X^{6*Y^14} + 48*X^{5*Y^15} \\ + 4*X^{4*Y^16} + 12*X^{3*Y^17} + 2*X*Y^19 \end{aligned}$ | I- iv,v |

| | | | |
|----|--|---|-------|
| 24 | [1 0 0 0 0 0 1 0 2 2] [0 1 0 0 0 0 2 2 2 2] [0 0 1 0 0 0 0 1 2 2] [0 0 0 1 0 0 2 2 0 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 4*X^{18}*Y^2 + 16*X^{16}*Y^4 + 16*X^{15}*Y^5 + 56*X^{14}*Y^6 + 80*X^{13}*Y^7 + 114*X^{12}*Y^8 + 160*X^{11}*Y^9 + 136*X^{10}*Y^{10} + 160*X^9*Y^{11} + 104*X^8*Y^{12} + 80*X^7*Y^{13} + 56*X^6*Y^{14} + 16*X^5*Y^{15} + 21*X^4*Y^{16} + 4*X^2*Y^{18}$ | I-i |
| 25 | [1 0 0 0 0 0 2 2 2 2] [0 1 0 0 0 0 0 0 2 2] [0 0 1 0 0 0 0 1 2 2] [0 0 0 1 0 0 2 2 0 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 5*X^{18}*Y^2 + 4*X^{17}*Y^3 + 15*X^{16}*Y^4 + 30*X^{15}*Y^5 + 45*X^{14}*Y^6 + 88*X^{13}*Y^7 + 105*X^{12}*Y^8 + 138*X^{11}*Y^9 + 151*X^{10}*Y^{10} + 132*X^9*Y^{11} + 125*X^8*Y^{12} + 82*X^7*Y^{13} + 55*X^6*Y^{14} + 32*X^5*Y^{15} + 10*X^4*Y^{16} + 6*X^3*Y^{17}$ | I-ii |
| 26 | [1 0 0 0 0 0 2 2 0 0] [0 1 0 0 0 0 0 0 2 2] [0 0 1 0 0 0 0 1 2 2] [0 0 0 1 0 0 2 2 0 0] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | | I-iii |
| 27 | [1 0 0 0 0 0 2 0 2 2] [0 1 0 0 0 0 2 2 2 2] [0 0 1 0 0 0 0 1 2 2] [0 0 0 1 0 0 2 2 0 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 5*X^{18}*Y^2 + 23*X^{16}*Y^4 + 8*X^{15}*Y^5 + 77*X^{14}*Y^6 + 50*X^{13}*Y^7 + 145*X^{12}*Y^8 + 124*X^{11}*Y^9 + 151*X^{10}*Y^{10} + 158*X^9*Y^{11} + 85*X^8*Y^{12} + 112*X^7*Y^{13} + 23*X^6*Y^{14} + 46*X^5*Y^{15} + 2*X^4*Y^{16} + 12*X^3*Y^{17} + 2*X^2*Y^{19}$ | I-iv |
| 28 | [1 0 0 0 0 0 2 2 0 0] [0 1 0 0 0 0 2 0 2 2] [0 0 1 0 0 0 0 1 2 2] [0 0 0 1 0 0 2 2 0 0] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | | I-v |

| | | | |
|----|--|--|--------------|
| | | | |
| 29 | [1 0 0 0 0 0 1 2 0 0] [0 1 0 0 0 0 2 0 0 0] [0 0 1 0 0 0 0 0 1 0] [0 0 0 1 0 0 0 0 0 1] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $\begin{aligned} X^{20} + 7*X^{18*Y^2} + 4*X^{17*Y^3} + 24*X^{16*Y^4} + \\ 28*X^{15*Y^5} + 56*X^{14*Y^6} + 84*X^{13*Y^7} + 98*X^{12*Y^8} + \\ 140*X^{11*Y^9} + 126*X^{10*Y^10} + 140*X^9*Y^11 + \\ 112*X^8*Y^12 + 84*X^7*Y^13 + 64*X^6*Y^14 + 28*X^5*Y^15 \\ + 21*X^4*Y^16 + 4*X^3*Y^17 + 3*X^2*Y^18 \end{aligned}$ | I-i |
| 30 | [1 0 0 0 0 0 3 2 0 0] [0 1 0 0 0 0 2 2 0 0] [0 0 1 0 0 0 0 0 1 0] [0 0 0 1 0 0 0 0 0 1] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | | |
| 31 | [1 0 0 0 0 0 0 2 0 0 0] [0 1 0 0 0 0 0 2 0 0] [0 0 1 0 0 0 0 0 1 0] [0 0 0 1 0 0 0 0 0 1] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $\begin{aligned} X^{20} + 8*X^{18*Y^2} + 4*X^{17*Y^3} + 28*X^{16*Y^4} + \\ 28*X^{15*Y^5} + 60*X^{14*Y^6} + 84*X^{13*Y^7} + 94*X^{12*Y^8} + \\ 140*X^{11*Y^9} + 116*X^{10*Y^10} + 140*X^9*Y^11 + \\ 108*X^8*Y^12 + 84*X^7*Y^13 + 68*X^6*Y^14 + 28*X^5*Y^15 \\ + 25*X^4*Y^16 + 4*X^3*Y^17 + 4*X^2*Y^18 \end{aligned}$ | I-ii |
| 32 | [1 0 0 0 0 0 0 2 2 0 0] [0 1 0 0 0 0 0 2 0 0] [0 0 1 0 0 0 0 0 1 0] [0 0 0 1 0 0 0 0 0 1] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $\begin{aligned} X^{20} + 8*X^{18*Y^2} + 2*X^{17*Y^3} + 32*X^{16*Y^4} + \\ 16*X^{15*Y^5} + 80*X^{14*Y^6} + 56*X^{13*Y^7} + 130*X^{12*Y^8} \\ + 112*X^{11*Y^9} + 136*X^{10*Y^10} + 140*X^9*Y^11 + \\ 88*X^8*Y^12 + 112*X^7*Y^13 + 32*X^6*Y^14 + 56*X^5*Y^15 \\ + 5*X^4*Y^16 + 16*X^3*Y^17 + 2*X^2*Y^19 \end{aligned}$ | I- iii,iv |
| 33 | [1 0 0 0 0 0 0 2 2 0 0] [0 1 0 0 0 0 2 2 0 0] [0 0 1 0 0 0 0 0 1 0] [0 0 0 1 0 0 0 0 0 1] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $\begin{aligned} X^{20} + 12*X^{18*Y^2} + 52*X^{16*Y^4} + 4*X^{15*Y^5} + \\ 116*X^{14*Y^6} + 28*X^{13*Y^7} + 150*X^{12*Y^8} + 84*X^{11*Y^9} \\ + 116*X^{10*Y^10} + 140*X^9*Y^11 + 52*X^8*Y^12 + \\ 140*X^7*Y^13 + 12*X^6*Y^14 + 84*X^5*Y^15 + X^4*Y^16 + \\ 28*X^3*Y^17 + 4*X^2*Y^19 \end{aligned}$ | I-v |
| 34 | [1 0 0 0 0 0 1 2 2 2] [0 1 0 0 0 0 2 0 0 2] [0 0 1 0 0 0 2 0 0 0] [0 0 0 1 0 0 2 0 2 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $\begin{aligned} X^{20} + 5*X^{18*Y^2} + 4*X^{17*Y^3} + 19*X^{16*Y^4} + \\ 24*X^{15*Y^5} + 51*X^{14*Y^6} + 80*X^{13*Y^7} + \\ 101*X^{12*Y^8} + 148*X^{11*Y^9} + \\ 141*X^{10*Y^10} + 148*X^9*Y^11 + 121*X^8*Y^12 + \\ 80*X^7*Y^13 + 57*X^6*Y^14 \\ + 24*X^5*Y^15 + 14*X^4*Y^16 + 4*X^3*Y^17 + \\ 2*X^2*Y^18 \end{aligned}$ | I-i |

| | | | |
|----|--|--|-------|
| 35 | [1 0 0 0 0 0 1 2 0 2] [0 1 0 0 0 0 2 0 2 2] [0 0 1 0 0 0 2 0 0 0] [0 0 0 1 0 0 0 0 1 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 4*X^{18}*Y^2 + 4*X^{17}*Y^3 + 18*X^{16}*Y^4 + 20*X^{15}*Y^5 + 50*X^{14}*Y^6 + 76*X^{13}*Y^7 + 100*X^{12}*Y^8 + 156*X^{11}*Y^9 + 146*X^{10}*Y^{10} + 156*X^9*Y^{11} + 126*X^8*Y^{12} + 76*X^7*Y^{13} + 54*X^6*Y^{14} + 20*X^5*Y^{15} + 11*X^4*Y^{16} + 4*X^3*Y^{17} + 2*X^2*Y^{18}$ | I-i |
| 36 | [1 0 0 0 0 0 2 0 2 2] [0 1 0 0 0 0 0 2 0 2] [0 0 1 0 0 0 2 0 0 0] [0 0 0 1 0 0 0 0 1 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 5*X^{18}*Y^2 + 2*X^{17}*Y^3 + 21*X^{16}*Y^4 + 18*X^{15}*Y^5 + 57*X^{14}*Y^6 + 78*X^{13}*Y^7 + 103*X^{12}*Y^8 + 158*X^{11}*Y^9 + 131*X^{10}*Y^{10} + 158*X^9*Y^{11} + 111*X^8*Y^{12} + 78*X^7*Y^{13} + 59*X^6*Y^{14} + 18*X^5*Y^{15} + 20*X^4*Y^{16} + 2*X^3*Y^{17} + 4*X^2*Y^{18}$ | I-ii |
| 37 | [1 0 0 0 0 0 0 2 2 2 0] [0 1 0 0 0 0 0 2 0 2] [0 0 1 0 0 0 2 2 0 2] [0 0 0 1 0 0 0 0 1 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 5*X^{18}*Y^2 + 25*X^{16}*Y^4 + 6*X^{15}*Y^5 + 77*X^{14}*Y^6 + 50*X^{13}*Y^7 + 139*X^{12}*Y^8 + 130*X^{11}*Y^9 + 151*X^{10}*Y^{10} + 158*X^9*Y^{11} + 91*X^8*Y^{12} + 106*X^7*Y^{13} + 23*X^6*Y^{14} + 46*X^5*Y^{15} + 14*X^3*Y^{17} + 2*X*Y^{19}$ | I-iii |
| 38 | [1 0 0 0 0 0 0 2 2 0 2] [0 1 0 0 0 0 2 0 2 2] [0 0 1 0 0 0 2 0 0 0] [0 0 0 1 0 0 0 0 1 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 5*X^{18}*Y^2 + 2*X^{17}*Y^3 + 21*X^{16}*Y^4 + 12*X^{15}*Y^5 + 77*X^{14}*Y^6 + 44*X^{13}*Y^7 + 151*X^{12}*Y^8 + 112*X^{11}*Y^9 + 151*X^{10}*Y^{10} + 164*X^9*Y^{11} + 79*X^8*Y^{12} + 124*X^7*Y^{13} + 23*X^6*Y^{14} + 4*X^5*Y^{15} + 4*X^4*Y^{16} + 8*X^3*Y^{17} + 2*X*Y^{19}$ | I-iv |
| 39 | [1 0 0 0 0 0 0 2 2 2 0] [0 1 0 0 0 0 2 2 0 2] [0 0 1 0 0 0 2 2 0 2] [0 0 0 1 0 0 0 0 1 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 9*X^{18}*Y^2 + 41*X^{16}*Y^4 + 113*X^{14}*Y^6 + 16*X^{13}*Y^7 + 171*X^{12}*Y^8 + 84*X^{11}*Y^9 + 131*X^{10}*Y^{10} + 164*X^9*Y^{11} + 43*X^8*Y^{12} + 152*X^7*Y^{13} + 3*X^6*Y^{14} + 72*X^5*Y^{15} + 20*X^3*Y^{17} + 4*X*Y^{19}$ | I-v |

| | | | |
|----|--|--|--------|
| | | | |
| 40 | [1 0 0 0 0 0 1 0 0 2] [0 1 0 0 0 0 2 2 2 2] [0 0 1 0 0 0 0 1 0 2] [0 0 0 1 0 0 0 0 1 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $\begin{aligned} X^{20} + 3*X^{18}*Y^2 + 24*X^{16}*Y^4 + 64*X^{14}*Y^6 + \\ 64*X^{13}*Y^7 + 98*X^{12}*Y^8 + 192*X^{11}*Y^9 + \\ 126*X^{10}*Y^{10} + 192*X^9*Y^{11} + 112*X^8*Y^{12} + \\ 64*X^7*Y^{13} + 56*X^6*Y^{14} + 21*X^4*Y^{16} + 7*X^2*Y^{18} \end{aligned}$ | I-i,ii |
| 41 | [1 0 0 0 0 0 3 0 0 2] [0 1 0 0 0 0 2 2 2 0] [0 0 1 0 0 0 0 1 0 2] [0 0 0 1 0 0 0 0 1 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | | |
| 42 | [1 0 0 0 0 0 0 2 2 2 0] [0 1 0 0 0 0 0 0 0 2] [0 0 1 0 0 0 0 1 0 2] [0 0 0 1 0 0 0 0 1 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | | I-iv |
| 43 | [1 0 0 0 0 0 0 2 0 0 2] [0 1 0 0 0 0 0 2 2 2 2] [0 0 1 0 0 0 0 1 0 2] [0 0 0 1 0 0 0 0 1 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $\begin{aligned} X^{20} + 4*X^{18}*Y^2 + 10*X^{17}*Y^3 + 16*X^{16}*Y^4 + \\ 30*X^{15}*Y^5 + 44*X^{14}*Y^6 + 66*X^{13}*Y^7 + 98*X^{12}*Y^8 + \\ 134*X^{11}*Y^9 + 156*X^{10}*Y^{10} + 158*X^9*Y^{11} + \\ 136*X^8*Y^{12} + 90*X^7*Y^{13} + 52*X^6*Y^{14} + 22*X^5*Y^{15} + \\ 5*X^4*Y^{16} + 2*X^3*Y^{17} \end{aligned}$ | I-ii |
| 44 | [1 0 0 0 0 0 0 2 2 2 0] [0 1 0 0 0 0 2 0 0 2] [0 0 1 0 0 0 0 1 0 2] [0 0 0 1 0 0 0 0 1 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | | I-iii |

| | | | |
|----|--|--|-------|
| 45 | [1 0 0 0 0 0 1 2 2 2] [0 1 0 0 0 0 2 2 0 0] [0 0 1 0 0 0 2 2 2 0] [0 0 0 1 0 0 2 0 2 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 5*X^{18}*Y^2 + 23*X^{16}*Y^4 + 12*X^{15}*Y^5 + 63*X^{14}*Y^6 + 76*X^{13}*Y^7 + 105*X^{12}*Y^8 + 168*X^{11}*Y^9 + 121*X^{10}*Y^{10} + 168*X^9*Y^{11} + 101*X^8*Y^{12} + 76*X^7*Y^{13} + 61*X^6*Y^{14} + 12*X^5*Y^{15} + 26*X^4*Y^{16} + 6*X^2*Y^{18}$ | I-i |
| 46 | [1 0 0 0 0 0 3 2 2 2] [0 1 0 0 0 0 2 0 2 2] [0 0 1 0 0 0 2 0 0 2] [0 0 0 1 0 0 2 2 0 0] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | | I-ii |
| 47 | [1 0 0 0 0 0 0 2 2 0 0] [0 1 0 0 0 0 0 2 2 2] [0 0 1 0 0 0 2 2 2 0] [0 0 0 1 0 0 2 0 2 2] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 6*X^{18}*Y^2 + 8*X^{17}*Y^3 + 19*X^{16}*Y^4 + 34*X^{15}*Y^5 + 48*X^{14}*Y^6 + 80*X^{13}*Y^7 + 95*X^{12}*Y^8 + 130*X^{11}*Y^9 + 142*X^{10}*Y^{10} + 136*X^9*Y^{11} + 133*X^8*Y^{12} + 86*X^7*Y^{13} + 60*X^6*Y^{14} + 32*X^5*Y^{15} + 8*X^4*Y^{16} + 6*X^3*Y^{17}$ | I-iii |
| 48 | [1 0 0 0 0 0 0 2 0 2 2] [0 1 0 0 0 0 0 2 2 2] [0 0 1 0 0 0 2 0 0 2] [0 0 0 1 0 0 2 2 0 0] [0 0 0 0 2 0 0 0 0 0] [0 0 0 0 0 2 0 0 0 0] | $X^{20} + 6*X^{18}*Y^2 + 8*X^{17}*Y^3 + 19*X^{16}*Y^4 + 36*X^{15}*Y^5 + 44*X^{14}*Y^6 + 80*X^{13}*Y^7 + 99*X^{12}*Y^8 + 124*X^{11}*Y^9 + 150*X^{10}*Y^{10} + 136*X^9*Y^{11} + 125*X^8*Y^{12} + 92*X^7*Y^{13} + 56*X^6*Y^{14} + 32*X^5*Y^{15} + 12*X^4*Y^{16} + 4*X^3*Y^{17}$ | I-iv |

2. BINARY FORMALLY SELF-DUAL CODES BY THE GRAY MAP

We list up the binary formally self-dual codes of lengths 4 and 8 by the Gray map.

Table 11. Binary formally self-dual codes of length 4 by the Gray map

| Code | Generator matrix of $\phi(C_{2,i})$ | Hamming weight enumerator | SD | Extremal code |
|-----------------|--|---------------------------|----|---------------|
| $\phi(C_{2,1})$ | $\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$ | $X^4 + 2X^3Y + X^2Y^2$ | | |
| $\phi(C_{2,2})$ | $\begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \end{bmatrix}$ | $X^4 + 2X^2Y^2 + Y^4$ | ○ | ○ |
| $\phi(C_{2,3})$ | $\begin{bmatrix} 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 1 \end{bmatrix}$ | $X^4 + X^2Y^2 + 2XY^3$ | | ○ |

Table 12. Binary formally self-dual codes of length 8 by the Gray map

| Code | Generator matrix of $\phi(C_{4,i})$ | Hamming weight enumerator | SD |
|------------------|-------------------------------------|--|----|
| $\phi(C_{4,1})$ | I_4 | $X^8 + 4X^7Y + 6X^6Y^2 + 4X^5Y^3 + X^4Y^4$ | |
| $\phi(C_{4,2})$ | I_4 | $X^8 + 2X^7Y + 3X^6Y^2 + 4X^5Y^3 + 3X^4Y^4 + 2X^3Y^5 + X^2Y^6$ | |
| $\phi(C_{4,3})$ | I_4 | $X^8 + 2X^7Y + 2X^6Y^2 + 4X^5Y^3 + 5X^4Y^4 + 2X^3Y^5$ | |
| $\phi(C_{4,4})$ | I_4 | $X^8 + 6X^6Y^2 + X^4Y^4 + 4X^3Y^5 + 4XY^7$ | |
| $\phi(C_{4,5})$ | I_4 | $X^8 + 4X^6Y^2 + 6X^4Y^4 + 4X^2Y^6 + Y^8$ | ○ |
| $\phi(C_{4,6})$ | I_4 | $X^8 + 3X^6Y^2 + 2X^5Y^3 + 3X^4Y^4 + 4X^3Y^5 + X^2Y^6 + 2XY^7$ | |
| $\phi(C_{4,7})$ | Non-linear | $X^8 + 2X^6Y^2 + 4X^5Y^3 + X^4Y^4 + 4X^3Y^5 + 4X^2Y^6$ | |
| $\phi(C_{4,8})$ | I_4 | $X^8 + 2X^6Y^2 + 2X^5Y^3 + 5X^4Y^4 + 4X^3Y^5 + 2XY^7$ | |
| $\phi(C_{4,9})$ | Non-linear | | |
| $\phi(C_{4,10})$ | I_4 | $X^8 + 2X^6Y^2 + 2X^5Y^3 + 5X^4Y^4 + 4X^3Y^5 + 2XY^7$ | |
| $\phi(C_{4,11})$ | I_4 | $X^8 + 2X^6Y^2 + 10X^4Y^4 + 2X^2Y^6 + Y^8$ | |
| $\phi(C_{4,12})$ | I_4 | $X^8 + X^6Y^2 + 4X^5Y^3 + 3X^4Y^4 + 4X^3Y^5 + 3X^2Y^6$ | |
| $\phi(C_{4,13})$ | I_4 | $X^8 + 4X^5Y^3 + 5X^4Y^4 + 4X^3Y^5 + 2X^2Y^6$ | |
| $\phi(C_{4,14})$ | Non-linear | | |
| $\phi(C_{4,15})$ | Non-linear | | |
| $\phi(C_{4,16})$ | I_4 | $X^8 + 14X^4Y^4 + Y^8$ | ○ |

We note that $\phi(C_{4,16})$ is the only extremal formally self-dual code over \mathbb{F}_2 of length 8.

3. LARGER MINIMUM LEE WEIGHT THAN THAT OF THE SELF-DUAL CODES OF THE SAME LENGTH

We put formally self-dual codes whose minimum Lee weights are larger than those of self-dual codes of the same length.

Table 13. Free formally self-dual codes with minimum Lee weights larger than the upper bound of the minimum Lee weights of self-dual codes (where SD denotes self-dual codes)

| Code | A_i of generator Matrix $G_i = [I_n \mid A_i]$ | Lee Weight Enumerator | d_L | Upper bound of SD code |
|-----------------------|---|--|-------|------------------------|
| $\mathcal{C}_{10,1}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 \\ 1 & 2 & 3 & 1 & 0 \\ 1 & 1 & 2 & 0 & 1 \\ 1 & 0 & 1 & 2 & 1 \\ 0 & 1 & 0 & 1 & 2 \end{bmatrix}$ | $X^{20} + 8X^{15}Y^5 + 54X^{14}Y^6 + 84X^{13}Y^7 + 121X^{12}Y^8 + 162X^{11}Y^9 + 153X^{10}Y^{10} + 176X^9Y^{11} + 134X^8Y^{12} + 68X^7Y^{13} + 48X^6Y^{14} + 12X^5Y^{15} + 2X^3Y^{17} + X^2Y^{18}$ | | |
| $\mathcal{C}_{10,2}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 1 \\ 1 & 2 & 3 & 1 & 0 \\ 1 & 1 & 2 & 0 & 3 \\ 1 & 0 & 1 & 2 & 1 \\ 1 & 3 & 0 & 1 & 2 \end{bmatrix}$ | | | |
| $\mathcal{C}_{10,3}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 1 \\ 1 & 2 & 3 & 1 & 3 \\ 1 & 1 & 2 & 0 & 1 \\ 1 & 0 & 1 & 2 & 2 \\ 1 & 1 & 3 & 2 & 1 \end{bmatrix}$ | | | |
| $\mathcal{C}_{10,4}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 \\ 1 & 2 & 3 & 1 & 0 \\ 1 & 1 & 2 & 0 & 1 \\ 1 & 0 & 1 & 2 & 2 \\ 0 & 1 & 0 & 2 & 1 \end{bmatrix}$ | $X^{20} + 8X^{15}Y^5 + 52X^{14}Y^6 + 92X^{13}Y^7 + 110X^{12}Y^8 + 164X^{11}Y^9 + 168X^{10}Y^{10} + 152X^9Y^{11} + 144X^8Y^{12} + 80X^7Y^{13} + 36X^6Y^{14} + 12X^5Y^{15} + X^4Y^{16} + 4X^3Y^{17}$ | | |
| $\mathcal{C}_{10,5}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 2 \\ 1 & 0 & 1 & 2 & 1 \\ 0 & 2 & 1 & 1 & 2 \end{bmatrix}$ | | | |
| $\mathcal{C}_{10,6}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 0 \\ 1 & 0 & 1 & 2 & 1 \\ 0 & 0 & 1 & 1 & 2 \end{bmatrix}$ | $X^{20} + 14X^{15}Y^5 + 42X^{14}Y^6 + 86X^{13}Y^7 + 124X^{12}Y^8 + 156X^{11}Y^9 + 180X^{10}Y^{10} + 156X^9Y^{11} + 124X^8Y^{12} + 86X^7Y^{13} + 34X^6Y^{14} + 14X^5Y^{15} + 7X^4Y^{16}$ | 5 | 4 |
| $\mathcal{C}_{10,7}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 1 \\ 1 & 2 & 3 & 1 & 3 \\ 1 & 1 & 2 & 0 & 2 \\ 1 & 0 & 1 & 2 & 3 \\ 1 & 2 & 3 & 3 & 0 \end{bmatrix}$ | | | |
| $\mathcal{C}_{10,8}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 2 \\ 1 & 0 & 1 & 2 & 1 \\ 2 & 2 & 1 & 1 & 0 \end{bmatrix}$ | $X^{20} + 14X^{15}Y^5 + 44X^{14}Y^6 + 80X^{13}Y^7 + 126X^{12}Y^8 + 166X^{11}Y^9 + 168X^{10}Y^{10} + 160X^9Y^{11} + 128X^8Y^{12} + 74X^7Y^{13} + 44X^6Y^{14} + 16X^5Y^{15} + X^4Y^{16} + 2X^3Y^{17}$ | | |
| $\mathcal{C}_{10,9}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 1 \\ 1 & 0 & 1 & 2 & 0 \\ 0 & 1 & 1 & 0 & 2 \end{bmatrix}$ | $X^{20} + 12X^{15}Y^5 + 46X^{14}Y^6 + 86X^{13}Y^7 + 120X^{12}Y^8 + 162X^{11}Y^9 + 172X^{10}Y^{10} + 156X^9Y^{11} + 132X^8Y^{12} + 80X^7Y^{13} + 38X^6Y^{14} + 14X^5Y^{15} + 3X^4Y^{16} + 2X^3Y^{17}$ | | |
| $\mathcal{C}_{10,10}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 \\ 1 & 2 & 3 & 1 & 2 \\ 1 & 1 & 2 & 0 & 1 \\ 1 & 0 & 1 & 2 & 2 \\ 0 & 1 & 2 & 2 & 1 \end{bmatrix}$ | | | |
| $\mathcal{C}_{10,11}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 1 \\ 1 & 0 & 1 & 2 & 2 \\ 0 & 1 & 1 & 2 & 1 \end{bmatrix}$ | | | |
| $\mathcal{C}_{10,12}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 1 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 1 \\ 1 & 0 & 1 & 2 & 1 \\ 1 & 1 & 1 & 1 & 3 \end{bmatrix}$ | $X^{20} + 12X^{15}Y^5 + 43X^{14}Y^6 + 94X^{13}Y^7 + 121X^{12}Y^8 + 144X^{11}Y^9 + 182X^{10}Y^{10} + 164X^9Y^{11} + 126X^8Y^{12} + 84X^7Y^{13} + 31X^6Y^{14} + 14X^5Y^{15} + 8X^4Y^{16}$ | | |
| $\mathcal{C}_{10,13}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 1 \\ 1 & 2 & 3 & 1 & 2 \\ 1 & 1 & 2 & 0 & 2 \\ 1 & 0 & 1 & 2 & 1 \\ 1 & 2 & 2 & 1 & 0 \end{bmatrix}$ | | | |
| $\mathcal{C}_{10,14}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 3 \\ 1 & 0 & 1 & 2 & 2 \\ 2 & 3 & 1 & 2 & 1 \end{bmatrix}$ | | | |

Table 13. Free formally self-dual codes with minimum Lee weights larger than the upper bound of the minimum Lee weights of self-dual codes (where SD denotes self-dual codes; cont'd)

| Code | A_i of generator Matrix $G_i = [I_n \mid A_i]$ | Lee Weight Enumerator | d_L | Upper bound of SD code |
|-----------------------|---|--|-------|------------------------|
| $\mathcal{C}_{10,15}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 1 \\ 1 & 0 & 1 & 2 & 3 \\ 0 & 1 & 1 & 3 & 1 \end{bmatrix}$ | $X^{20} + 18X^{15}Y^5 + 39X^{14}Y^6 + 72X^{13}Y^7 + 133X^{12}Y^8 + 172X^{11}Y^9 + 174X^{10}Y^{10} + 152X^9Y^{11} + 118X^8Y^{12} + 82X^7Y^{13} + 43X^6Y^{14} + 16X^5Y^{15} + 4X^4Y^{16}$ | | |
| $\mathcal{C}_{10,16}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 0 \\ 1 & 0 & 1 & 2 & 0 \\ 2 & 0 & 1 & 0 & 1 \end{bmatrix}$ | | | |
| $\mathcal{C}_{10,17}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 2 \\ 1 & 0 & 1 & 2 & 2 \\ 2 & 2 & 1 & 2 & 1 \end{bmatrix}$ | | | |
| $\mathcal{C}_{10,18}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 2 \\ 1 & 0 & 1 & 2 & 0 \\ 0 & 2 & 1 & 0 & 1 \end{bmatrix}$ | | | |
| $\mathcal{C}_{10,19}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 3 \\ 1 & 0 & 1 & 2 & 3 \\ 0 & 3 & 1 & 3 & 1 \end{bmatrix}$ | $X^{20} + 14X^{15}Y^5 + 43X^{14}Y^6 + 84X^{13}Y^7 + 121X^{12}Y^8 + 164X^{11}Y^9 + 182X^{10}Y^{10} + 144X^9Y^{11} + 126X^8Y^{12} + 94X^7Y^{13} + 31X^6Y^{14} + 12X^5Y^{15} + 8X^4Y^{16}$ | 5 | 4 |
| $\mathcal{C}_{10,20}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 \\ 1 & 2 & 3 & 1 & 3 \\ 1 & 1 & 2 & 0 & 3 \\ 1 & 0 & 1 & 2 & 1 \\ 2 & 3 & 3 & 1 & 1 \end{bmatrix}$ | | | |
| $\mathcal{C}_{10,21}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 2 \\ 1 & 0 & 1 & 2 & 0 \\ 2 & 2 & 1 & 0 & 1 \end{bmatrix}$ | | | |
| $\mathcal{C}_{10,22}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 1 \\ 1 & 0 & 1 & 2 & 0 \\ 0 & 1 & 1 & 0 & 2 \end{bmatrix}$ | $X^{20} + 12X^{15}Y^5 + 46X^{14}Y^6 + 86X^{13}Y^7 + 120X^{12}Y^8 + 162X^{11}Y^9 + 172X^{10}Y^{10} + 156X^9Y^{11} + 132X^8Y^{12} + 80X^7Y^{13} + 38X^6Y^{14} + 14X^5Y^{15} + 3X^4Y^{16} + 2X^3Y^{17}$ | | |
| $\mathcal{C}_{10,23}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 2 \\ 1 & 0 & 1 & 2 & 1 \\ 0 & 2 & 1 & 1 & 1 \end{bmatrix}$ | $X^{20} + 12X^{15}Y^5 + 47X^{14}Y^6 + 84X^{13}Y^7 + 117X^{12}Y^8 + 170X^{11}Y^9 + 174X^{10}Y^{10} + 144X^9Y^{11} + 134X^8Y^{12} + 88X^7Y^{13} + 35X^6Y^{14} + 12X^5Y^{15} + 4X^4Y^{16} + 2X^3Y^{17}$ | | |
| $\mathcal{C}_{10,24}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 3 \\ 1 & 0 & 1 & 2 & 3 \\ 2 & 3 & 1 & 3 & 1 \end{bmatrix}$ | | | |
| $\mathcal{C}_{10,25}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 \\ 1 & 2 & 3 & 1 & 1 \\ 1 & 1 & 2 & 0 & 3 \\ 1 & 0 & 1 & 2 & 0 \\ 0 & 3 & 1 & 0 & 2 \end{bmatrix}$ | $X^{20} + 16X^{15}Y^5 + 40X^{14}Y^6 + 80X^{13}Y^7 + 130X^{12}Y^8 + 160X^{11}Y^9 + 176X^{10}Y^{10} + 160X^9Y^{11} + 120X^8Y^{12} + 80X^7Y^{13} + 40X^6Y^{14} + 16X^5Y^{15} + 5X^4Y^{16}$ | | |
| $\mathcal{C}_{10,26}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 \\ 1 & 2 & 3 & 1 & 2 \\ 1 & 1 & 2 & 0 & 2 \\ 1 & 0 & 1 & 2 & 1 \\ 0 & 2 & 2 & 1 & 1 \end{bmatrix}$ | | | |

Table 13. Free formally self-dual codes with minimum Lee weights larger than the upper bound of the minimum Lee weights of self-dual codes (where SD denotes self-dual codes; cont'd)

| Code | A_i of generator Matrix $G_i = [I_n \mid A_i]$ | Lee Weight Enumerator | d_L | Upper bound of SD code |
|-----------------------|--|--|-------|------------------------|
| $\mathcal{C}_{10,27}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 \\ 1 & 2 & 3 & 1 & 2 \\ 1 & 1 & 2 & 0 & 1 \\ 1 & 0 & 1 & 2 & 3 \\ 0 & 1 & 2 & 1 & 3 \end{bmatrix}$ | $X^{20} + 90X^{14}Y^6 + 255X^{12}Y^8 + 332X^{10}Y^{10} + 255X^8Y^{12} + 90X^6Y^{14} + Y^{20}$ | 6 | 4 |
| $\mathcal{C}_{10,28}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 \\ 1 & 1 & 2 & 0 & 1 \\ 1 & 0 & 1 & 2 & 3 \\ 0 & 1 & 2 & 1 & 3 \end{bmatrix}$ | $X^{20} + 90X^{14}Y^6 + 255X^{12}Y^8 + 332X^{10}Y^{10} + 255X^8Y^{12} + 90X^6Y^{14} + Y^{20}$ | 6 | 4 |
| $\mathcal{C}_{10,29}$ | $\begin{bmatrix} 1 & 2 & 1 & 0 & 1 \\ 1 & 1 & 3 & 2 & 2 \\ 3 & 1 & 2 & 1 & 2 \\ 2 & 0 & 1 & 3 & 3 \\ 2 & 1 & 2 & 3 & 1 \end{bmatrix}$ | $X^{24} + 37X^{18}Y^6 + 102X^{17}Y^7 + 180X^{16}Y^8 + 326X^{15}Y^9 + 483X^{14}Y^{10} + 582X^{13}Y^{11} + 628X^{12}Y^{12} + 630X^{11}Y^{13} + 507X^{10}Y^{14} + 322X^9Y^{15} + 183X^8Y^{16} + 66X^7Y^{17} + 29X^6Y^{18} + 18X^5Y^{19} + 2X^3Y^{21}$ | 6 | 4 |
| $\mathcal{C}_{10,30}$ | $\begin{bmatrix} 1 & 2 & 1 & 0 & 3 \\ 1 & 1 & 3 & 2 & 0 \\ 3 & 1 & 2 & 1 & 2 \\ 2 & 0 & 1 & 3 & 1 \\ 0 & 3 & 2 & 1 & 3 \end{bmatrix}$ | $X^{24} + 37X^{18}Y^6 + 102X^{17}Y^7 + 180X^{16}Y^8 + 326X^{15}Y^9 + 483X^{14}Y^{10} + 582X^{13}Y^{11} + 628X^{12}Y^{12} + 630X^{11}Y^{13} + 507X^{10}Y^{14} + 322X^9Y^{15} + 183X^8Y^{16} + 66X^7Y^{17} + 29X^6Y^{18} + 18X^5Y^{19} + 2X^3Y^{21}$ | 6 | 4 |
| $\mathcal{C}_{10,31}$ | $\begin{bmatrix} 1 & 1 & 1 & 1 & 3 \\ 0 & 1 & 2 & 3 & 1 \\ 2 & 1 & 3 & 2 & 3 \\ 3 & 1 & 2 & 1 & 2 \\ 1 & 3 & 3 & 2 & 0 \end{bmatrix}$ | $X^{24} + 37X^{18}Y^6 + 102X^{17}Y^7 + 180X^{16}Y^8 + 326X^{15}Y^9 + 483X^{14}Y^{10} + 582X^{13}Y^{11} + 628X^{12}Y^{12} + 630X^{11}Y^{13} + 507X^{10}Y^{14} + 322X^9Y^{15} + 183X^8Y^{16} + 66X^7Y^{17} + 29X^6Y^{18} + 18X^5Y^{19} + 2X^3Y^{21}$ | 6 | 4 |
| $\mathcal{C}_{10,32}$ | $\begin{bmatrix} 1 & 1 & 1 & 1 & 3 \\ 0 & 1 & 2 & 3 & 1 \\ 2 & 1 & 3 & 2 & 3 \\ 3 & 1 & 2 & 1 & 0 \\ 1 & 3 & 3 & 0 & 2 \end{bmatrix}$ | $X^{24} + 37X^{18}Y^6 + 102X^{17}Y^7 + 180X^{16}Y^8 + 326X^{15}Y^9 + 483X^{14}Y^{10} + 582X^{13}Y^{11} + 628X^{12}Y^{12} + 630X^{11}Y^{13} + 507X^{10}Y^{14} + 322X^9Y^{15} + 183X^8Y^{16} + 66X^7Y^{17} + 29X^6Y^{18} + 18X^5Y^{19} + 2X^3Y^{21}$ | 6 | 4 |
| $\mathcal{C}_{10,33}$ | $\begin{bmatrix} 1 & 2 & 1 & 1 & 2 \\ 1 & 1 & 2 & 2 & 1 \\ 2 & 1 & 0 & 3 & 3 \\ 2 & 1 & 3 & 1 & 2 \\ 1 & 2 & 3 & 2 & 3 \end{bmatrix}$ | $X^{24} + 37X^{18}Y^6 + 102X^{17}Y^7 + 180X^{16}Y^8 + 326X^{15}Y^9 + 483X^{14}Y^{10} + 582X^{13}Y^{11} + 628X^{12}Y^{12} + 630X^{11}Y^{13} + 507X^{10}Y^{14} + 322X^9Y^{15} + 183X^8Y^{16} + 66X^7Y^{17} + 29X^6Y^{18} + 18X^5Y^{19} + 2X^3Y^{21}$ | 6 | 4 |
| $\mathcal{C}_{12,1}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 & 0 \\ 1 & 2 & 3 & 1 & 1 & 0 \\ 1 & 1 & 2 & 0 & 2 & 2 \\ 1 & 0 & 1 & 2 & 1 & 2 \\ 2 & 2 & 1 & 1 & 0 & 1 \\ 0 & 2 & 0 & 2 & 1 & 3 \end{bmatrix}$ | $X^{24} + 37X^{18}Y^6 + 102X^{17}Y^7 + 180X^{16}Y^8 + 326X^{15}Y^9 + 483X^{14}Y^{10} + 582X^{13}Y^{11} + 628X^{12}Y^{12} + 630X^{11}Y^{13} + 507X^{10}Y^{14} + 322X^9Y^{15} + 183X^8Y^{16} + 66X^7Y^{17} + 29X^6Y^{18} + 18X^5Y^{19} + 2X^3Y^{21}$ | 6 | 4 |
| $\mathcal{C}_{12,2}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 & 2 \\ 1 & 2 & 3 & 1 & 1 & 3 \\ 1 & 1 & 2 & 0 & 2 & 3 \\ 1 & 0 & 1 & 2 & 1 & 0 \\ 2 & 2 & 1 & 1 & 0 & 3 \\ 2 & 3 & 3 & 0 & 3 & 0 \end{bmatrix}$ | $X^{24} + 60X^{18}Y^6 + 399X^{16}Y^8 + 900X^{14}Y^{10} + 1376X^{12}Y^{12} + 900X^{10}Y^{14} + 399X^8Y^{16} + 60X^6Y^{18} + Y^{24}$ | 6 | 4 |
| $\mathcal{C}_{12,3}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 & 0 \\ 1 & 2 & 3 & 1 & 1 & 1 \\ 1 & 1 & 2 & 0 & 2 & 1 \\ 1 & 0 & 1 & 2 & 1 & 0 \\ 2 & 2 & 1 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 & 1 & 2 \end{bmatrix}$ | $X^{24} + 39X^{18}Y^6 + 88X^{17}Y^7 + 212X^{16}Y^8 + 312X^{15}Y^9 + 442X^{14}Y^{10} + 624X^{13}Y^{11} + 634X^{12}Y^{12} + 624X^{11}Y^{13} + 504X^{10}Y^{14} + 312X^9Y^{15} + 171X^8Y^{16} + 88X^7Y^{17} + 38X^6Y^{18} + 6X^4Y^{20} + X^2Y^{22}$ | 6 | 4 |
| $\mathcal{C}_{12,4}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 & 2 \\ 1 & 2 & 3 & 1 & 1 & 2 \\ 1 & 1 & 2 & 0 & 2 & 0 \\ 1 & 0 & 1 & 2 & 1 & 1 \\ 2 & 2 & 1 & 1 & 0 & 1 \\ 2 & 0 & 2 & 1 & 1 & 3 \end{bmatrix}$ | $X^{24} + 39X^{18}Y^6 + 88X^{17}Y^7 + 212X^{16}Y^8 + 312X^{15}Y^9 + 442X^{14}Y^{10} + 624X^{13}Y^{11} + 634X^{12}Y^{12} + 624X^{11}Y^{13} + 504X^{10}Y^{14} + 312X^9Y^{15} + 171X^8Y^{16} + 88X^7Y^{17} + 38X^6Y^{18} + 6X^4Y^{20} + X^2Y^{22}$ | 6 | 4 |
| $\mathcal{C}_{12,5}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 & 2 \\ 1 & 2 & 3 & 1 & 1 & 2 \\ 1 & 1 & 2 & 0 & 2 & 0 \\ 1 & 0 & 1 & 2 & 1 & 1 \\ 2 & 2 & 1 & 1 & 0 & 1 \\ 2 & 1 & 2 & 1 & 1 & 0 \end{bmatrix}$ | $X^{24} + 32X^{18}Y^6 + 114X^{17}Y^7 + 177X^{16}Y^8 + 316X^{15}Y^9 + 498X^{14}Y^{10} + 558X^{13}Y^{11} + 637X^{12}Y^{12} + 648X^{11}Y^{13} + 492X^{10}Y^{14} + 334X^9Y^{15} + 174X^8Y^{16} + 60X^7Y^{17} + 34X^6Y^{18} + 18X^5Y^{19} + 3X^4Y^{20}$ | 6 | 4 |
| $\mathcal{C}_{12,6}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 & 1 \\ 1 & 2 & 3 & 1 & 1 & 3 \\ 1 & 1 & 2 & 0 & 2 & 2 \\ 1 & 0 & 1 & 2 & 1 & 2 \\ 2 & 2 & 1 & 1 & 0 & 2 \\ 1 & 2 & 3 & 2 & 2 & 1 \end{bmatrix}$ | $X^{24} + 32X^{18}Y^6 + 110X^{17}Y^7 + 188X^{16}Y^8 + 320X^{15}Y^9 + 464X^{14}Y^{10} + 574X^{13}Y^{11} + 666X^{12}Y^{12} + 624X^{11}Y^{13} + 496X^{10}Y^{14} + 330X^9Y^{15} + 163X^8Y^{16} + 80X^7Y^{17} + 32X^6Y^{18} + 10X^5Y^{19} + 6X^4Y^{20}$ | 6 | 4 |
| $\mathcal{C}_{12,7}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 & 1 \\ 1 & 2 & 3 & 1 & 1 & 3 \\ 1 & 1 & 2 & 0 & 2 & 3 \\ 1 & 0 & 1 & 2 & 1 & 1 \\ 2 & 2 & 1 & 1 & 0 & 3 \\ 1 & 3 & 1 & 1 & 3 & 2 \end{bmatrix}$ | $X^{24} + 30X^{18}Y^6 + 112X^{17}Y^7 + 195X^{16}Y^8 + 316X^{15}Y^9 + 452X^{14}Y^{10} + 572X^{13}Y^{11} + 683X^{12}Y^{12} + 632X^{11}Y^{13} + 478X^{10}Y^{14} + 328X^9Y^{15} + 172X^8Y^{16} + 76X^7Y^{17} + 32X^6Y^{18} + 12X^5Y^{19} + 5X^4Y^{20}$ | 6 | 4 |
| $\mathcal{C}_{12,8}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 & 1 \\ 1 & 2 & 3 & 1 & 1 & 3 \\ 1 & 1 & 2 & 0 & 2 & 3 \\ 1 & 0 & 1 & 2 & 1 & 2 \\ 2 & 2 & 1 & 1 & 0 & 0 \\ 1 & 3 & 3 & 2 & 0 & 1 \end{bmatrix}$ | $X^{24} + 30X^{18}Y^6 + 112X^{17}Y^7 + 195X^{16}Y^8 + 316X^{15}Y^9 + 452X^{14}Y^{10} + 572X^{13}Y^{11} + 683X^{12}Y^{12} + 632X^{11}Y^{13} + 478X^{10}Y^{14} + 328X^9Y^{15} + 172X^8Y^{16} + 76X^7Y^{17} + 32X^6Y^{18} + 12X^5Y^{19} + 5X^4Y^{20}$ | 6 | 4 |

Table 13. Free formally self-dual codes with minimum Lee weights larger than the upper bound of the minimum Lee weights of self-dual codes (where SD denotes self-dual codes; cont'd)

| Code | A_i of generator Matrix $G_i = [I_n \mid A_i]$ | Lee Weight Enumerator | d_L | Upper bound of SD code |
|-----------------------|---|--|-------|------------------------|
| $\mathcal{C}_{12,9}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 & 1 \\ 1 & 2 & 3 & 1 & 1 & 0 \\ 1 & 1 & 2 & 0 & 2 & 2 \\ 1 & 0 & 1 & 2 & 1 & 0 \\ 2 & 2 & 1 & 1 & 0 & 3 \\ 1 & 2 & 0 & 0 & 3 & 1 \end{bmatrix}$ | $X^{24} + 32X^{18}Y^6 + 112X^{17}Y^7 + 183X^{16}Y^8 + 316X^{15}Y^9 + 482X^{14}Y^{10} + 572X^{13}Y^{11} + 643X^{12}Y^{12} + 632X^{11}Y^{13} + 508X^{10}Y^{14} + 328X^9Y^{15} + 160X^8Y^{16} + 76X^7Y^{17} + 34X^6Y^{18} + 12X^5Y^{19} + 5X^4Y^{20}$ | 6 | 4 |
| $\mathcal{C}_{12,10}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 & 1 \\ 1 & 2 & 3 & 1 & 1 & 0 \\ 1 & 1 & 2 & 0 & 2 & 0 \\ 1 & 0 & 1 & 2 & 1 & 1 \\ 2 & 2 & 1 & 1 & 0 & 2 \\ 1 & 0 & 0 & 1 & 2 & 3 \end{bmatrix}$ | $X^{24} + 36X^{18}Y^6 + 108X^{17}Y^7 + 167X^{16}Y^8 + 332X^{15}Y^9 + 502X^{14}Y^{10} + 552X^{13}Y^{11} + 643X^{12}Y^{12} + 632X^{11}Y^{13} + 488X^{10}Y^{14} + 348X^9Y^{15} + 176X^8Y^{16} + 60X^7Y^{17} + 30X^6Y^{18} + 16X^5Y^{19} + 5X^4Y^{20}$ | | |
| $\mathcal{C}_{14,1}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 0 & 0 & 1 \\ 1 & 2 & 3 & 1 & 0 & 3 & 0 \\ 1 & 1 & 2 & 0 & 1 & 2 & 0 \\ 1 & 0 & 1 & 2 & 2 & 0 & 1 \\ 0 & 1 & 0 & 2 & 1 & 3 & 2 \\ 0 & 2 & 3 & 0 & 3 & 1 & 3 \\ 1 & 0 & 0 & 1 & 2 & 3 & 3 \end{bmatrix}$ | $X^{28} + 84X^{21}Y^7 + 253X^{20}Y^8 + 438X^{19}Y^9 + 770X^{18}Y^{10} + 1258X^{17}Y^{11} + 1782X^{16}Y^{12} + 2310X^{15}Y^{13} + 2546X^{14}Y^{14} + 2322X^{13}Y^{15} + 1849X^{12}Y^{16} + 1266X^{11}Y^{17} + 758X^{10}Y^{18} + 430X^9Y^{19} + 210X^8Y^{20} + 82X^7Y^{21} + 22X^6Y^{22} + 2X^5Y^{23} + X^4Y^{24}$ | 7 | 6 |
| $\mathcal{C}_{14,2}$ | $\begin{bmatrix} 2 & 1 & 1 & 1 & 2 & 1 & 0 \\ 1 & 2 & 3 & 1 & 1 & 2 & 2 \\ 1 & 1 & 2 & 0 & 2 & 0 & 1 \\ 1 & 0 & 1 & 2 & 1 & 3 & 0 \\ 2 & 2 & 1 & 1 & 0 & 3 & 1 \\ 1 & 0 & 2 & 3 & 3 & 3 & 2 \\ 0 & 1 & 2 & 0 & 1 & 2 & 3 \end{bmatrix}$ | $X^{28} + 72X^{21}Y^7 + 281X^{20}Y^8 + 448X^{19}Y^9 + 704X^{18}Y^{10} + 1312X^{17}Y^{11} + 1768X^{16}Y^{12} + 2240X^{15}Y^{13} + 2688X^{14}Y^{14} + 2288X^{13}Y^{15} + 1763X^{12}Y^{16} + 1344X^{11}Y^{17} + 704X^{10}Y^{18} + 416X^9Y^{19} + 280X^8Y^{20} + 64X^7Y^{21} + 8X^5Y^{23} + 3X^4Y^{24}$ | | |